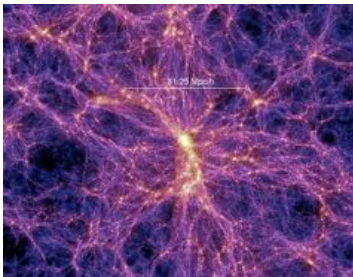
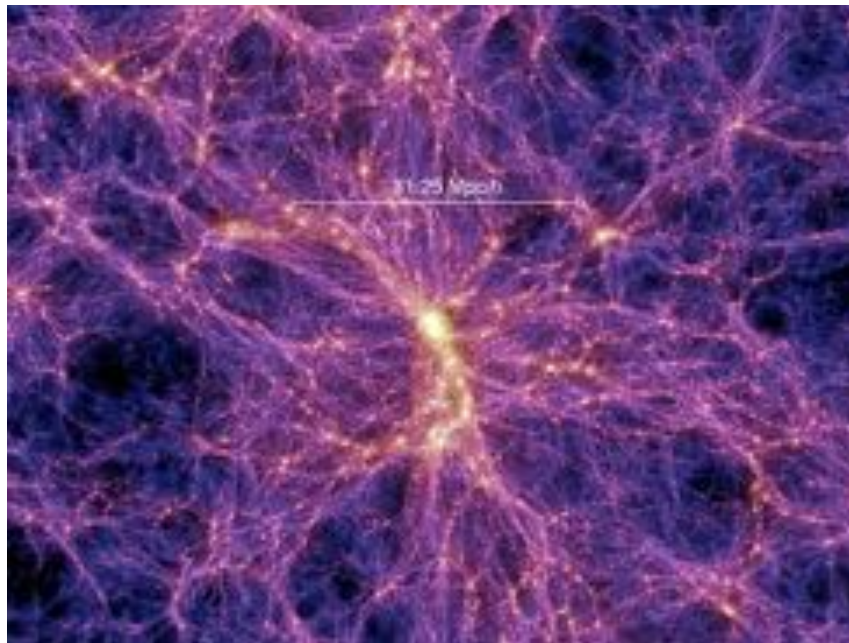




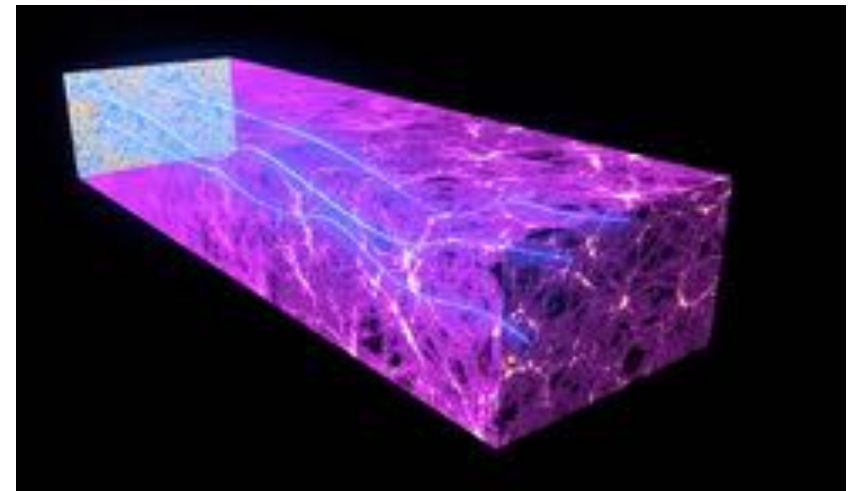
O Universo em grande escala: das flutuações primordiais à formação das estruturas



What
Why
How

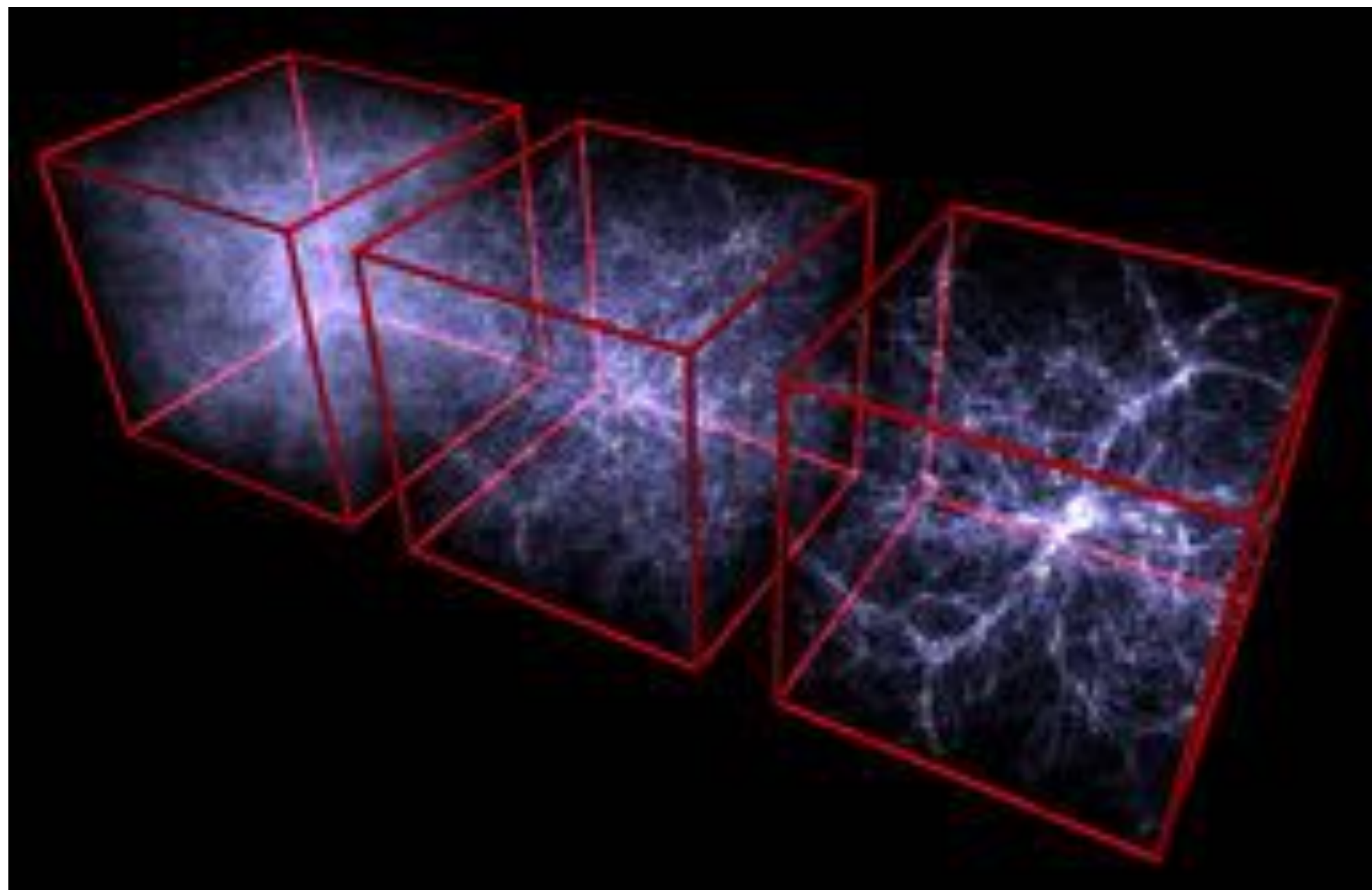


Armando Bernui



LESSON 3

The observed Universe:
modern cosmological probes



How to measure matter clustering?

2-point correlation function

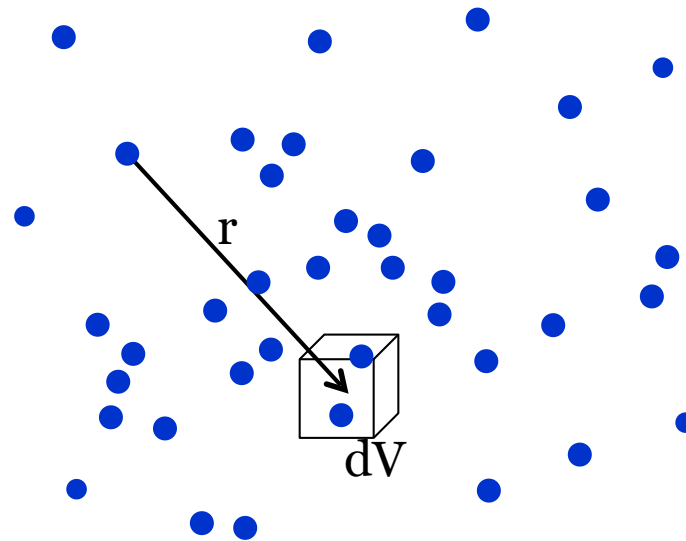
The 2-point statistics $(P(k), \xi(r))$ provide a complete statistical description of the density field under Gaussian initial conditions and linear growth of fluctuations

2-p correlation function (2PCF): $\xi(r)$

If you are sitting on a galaxy, the probability dP that you will find another galaxy in a volume dV a distance r away from you is given by

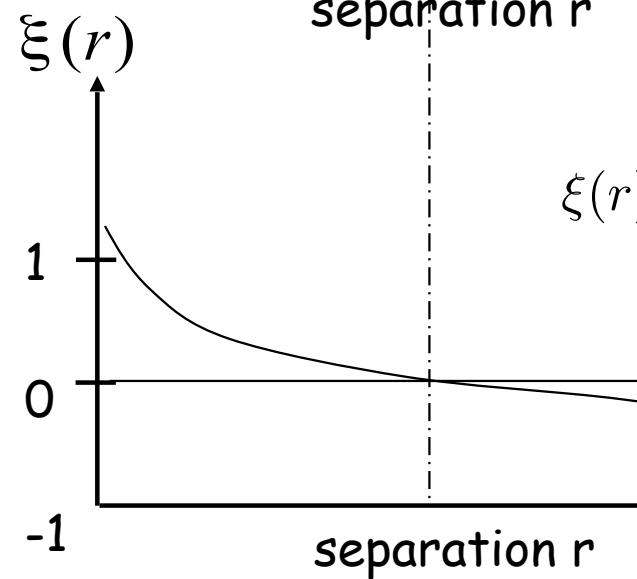
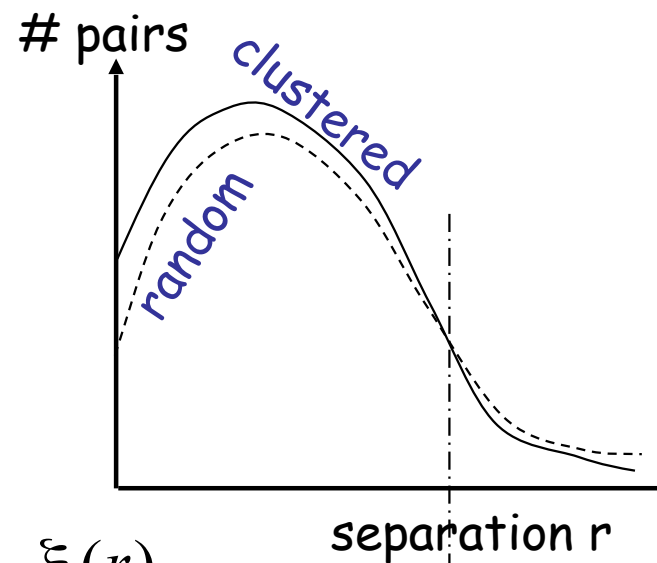
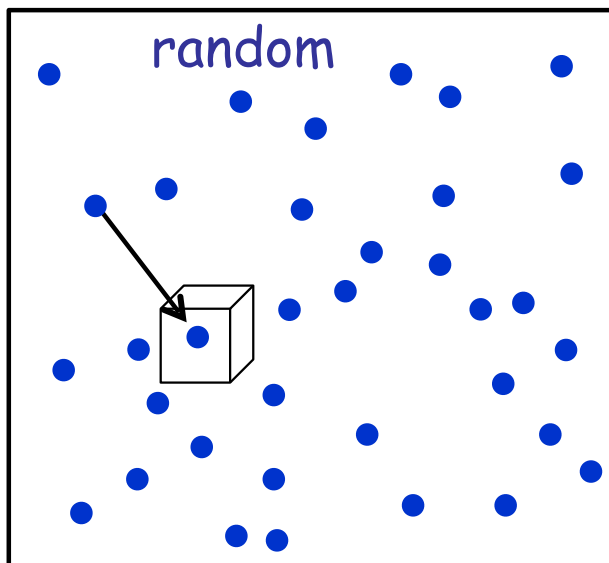
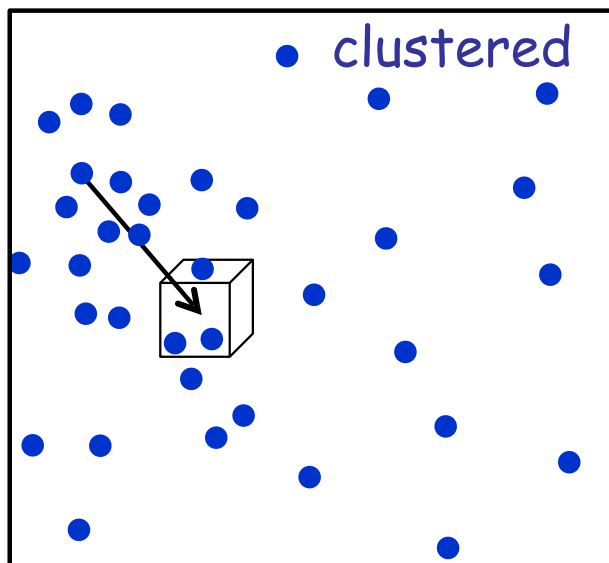
$$dP = n dV [1 + \xi(r)]$$

where n is the average number density of galaxies.



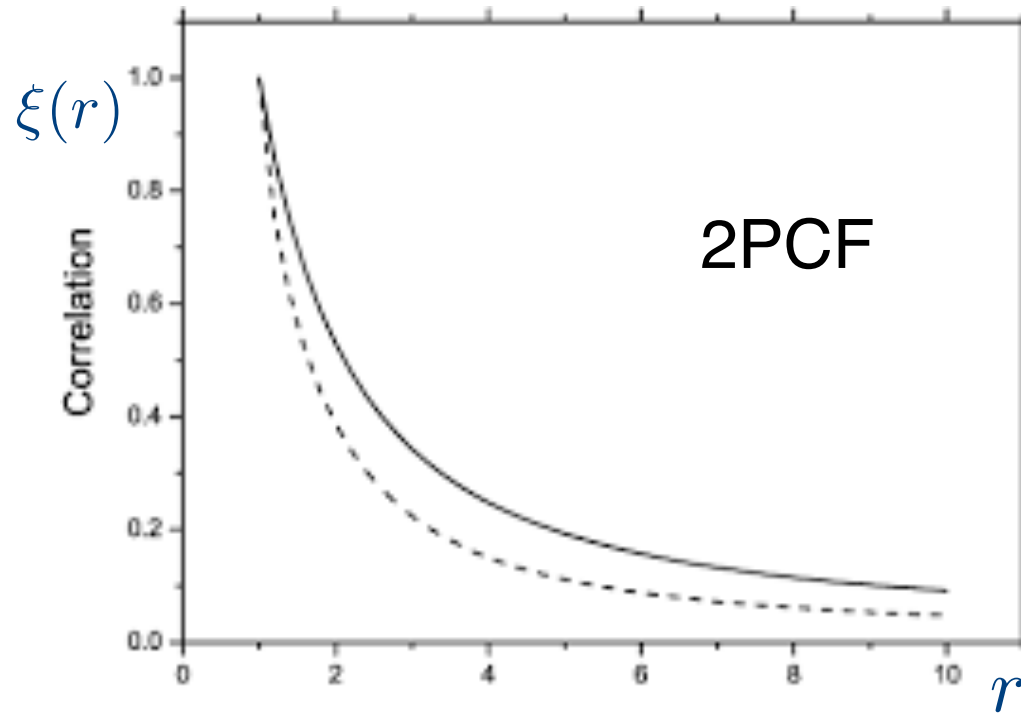
dP is the number of galaxies you expect to find in a volume dV .

What does the 2PCF measures?



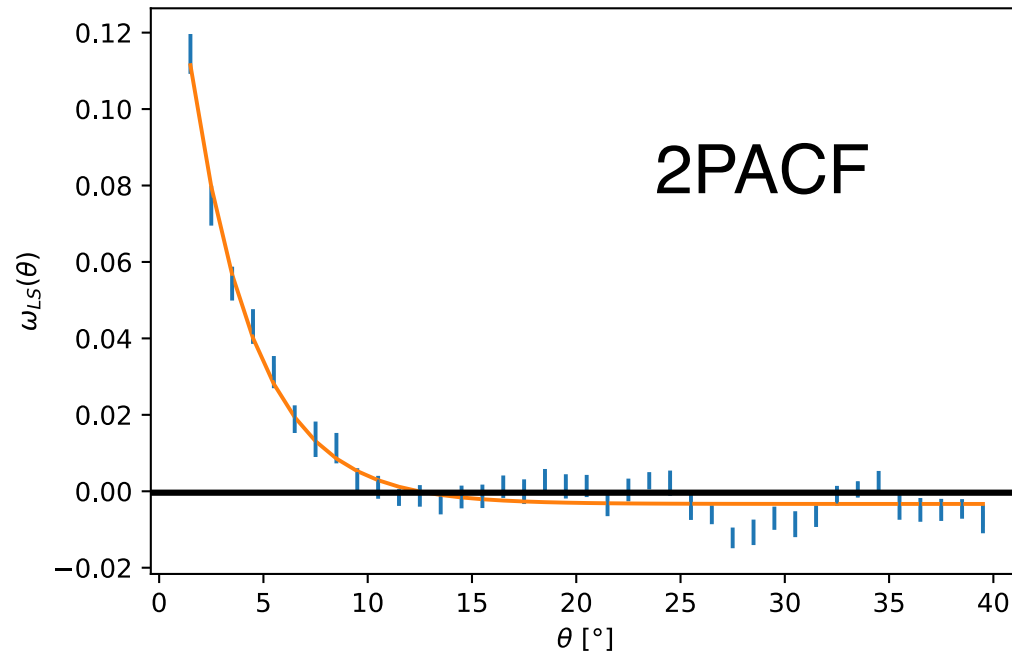
$$\xi(r) = \frac{DD(r)}{RR(r)} - 1$$

2-point correlation function



$$\xi(r) \propto r^{-\alpha}$$

$$\xi(r) = \left(\frac{r_0}{r} \right)^\alpha$$



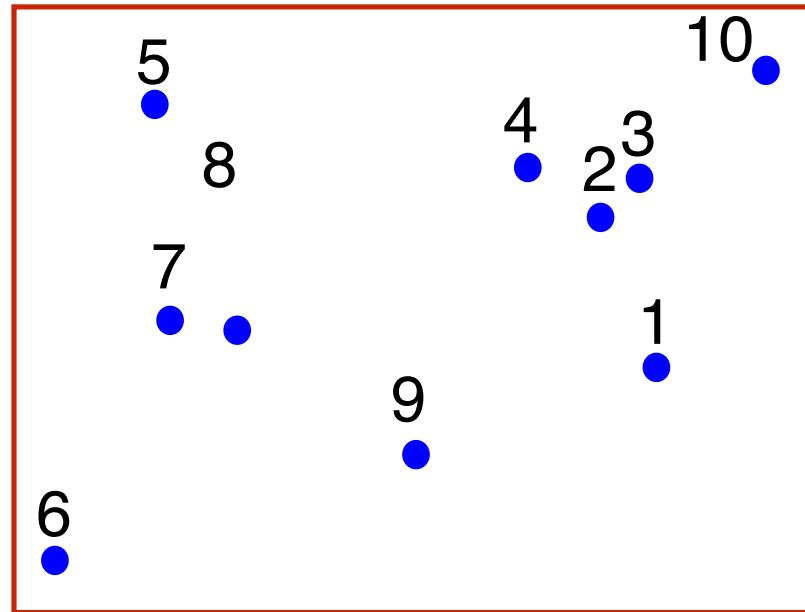
$$\omega(\theta) \propto \theta^{-\beta}$$

$$\omega(\theta) = \left(\frac{\theta_0}{\theta} \right)^\beta$$

How to count pairs in a data catalogue?

D

pairs distances
D_{12}
D_{13}
$\dots$
$D_{1,10}$
$D_{21}?$ X
D_{23}
$\dots$
$D_{2,10}$
D_{34}
$\dots$
$D_{9,10}$



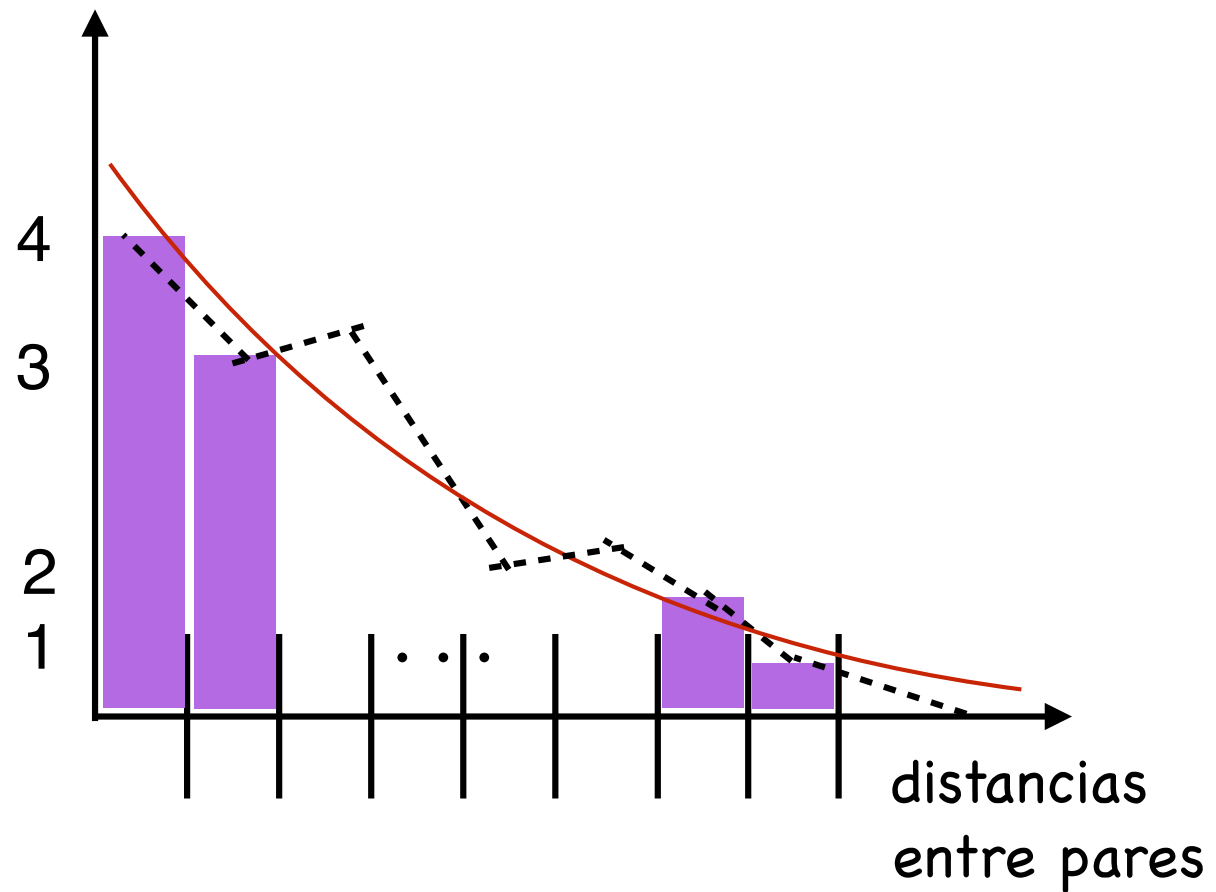
$$\{D_{23}, D_{24}, D_{34}, D_{58}\} \in \text{bin}_1$$

$$\{D_{12}, D_{39}, D_{78}\} \in \text{bin}_2$$

$$\{D_{26}, D_{36}\} \in \text{bin}_{n-1} \cdots \{D_{6,10}\} \in \text{bin}_n$$

How many data pairs did we get?

pairs distances
D_{12}
D_{13}
...
$D_{1,10}$
D_{21} ? X
D_{23}
...
$D_{2,10}$
D_{34}
...
$D_{9,10}$



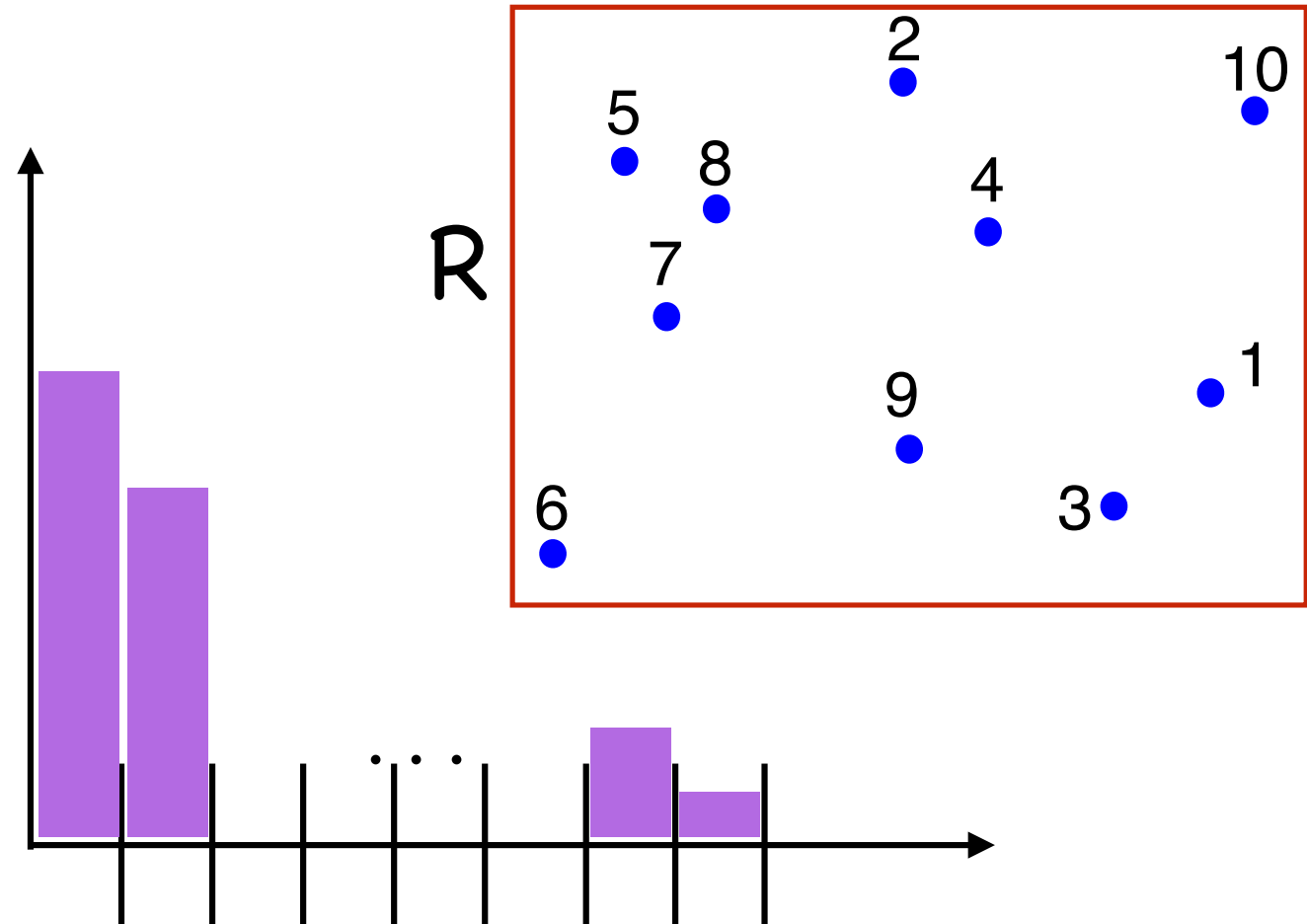
**Histograma de contagem de
distancias entre pares $\mathbf{D}$**

$$= DD(r)$$

$$\neq \xi(r)$$

Now, we generate a random catalogue
in the same region of the data sample

pairs distances
R_{12}
R_{13}
...
$R_{1,10}$
$R_{21}?$ X
R_{23}
...
$R_{2,10}$
R_{34}
...
$R_{9,10}$



Histograma de contagem de
distancias entre pares $R = RR(r)$

2-point correlation function

Landy-Szalay

$$\xi(r) = \frac{DD(r) - 2DR(r) + RR(r)}{RR(r)}$$

Peebles-Hauser

$$\xi(r) = \frac{DD(r)}{RR(r)} - 1$$

$$\xi(r) = \frac{1}{N} \sum_{i=1}^N \frac{DD(r) - RR_i(r)}{RR_i(r)}$$

Homework

2-point angular correlation function

Landy-Szalay

$$\omega(\gamma) = \frac{DD(\gamma) - 2DR(\gamma) + RR(\gamma)}{RR(\gamma)}$$

Peebles-Hauser

$$\omega(\gamma) = \frac{DD(\gamma) - RR(\gamma)}{RR(\gamma)}$$

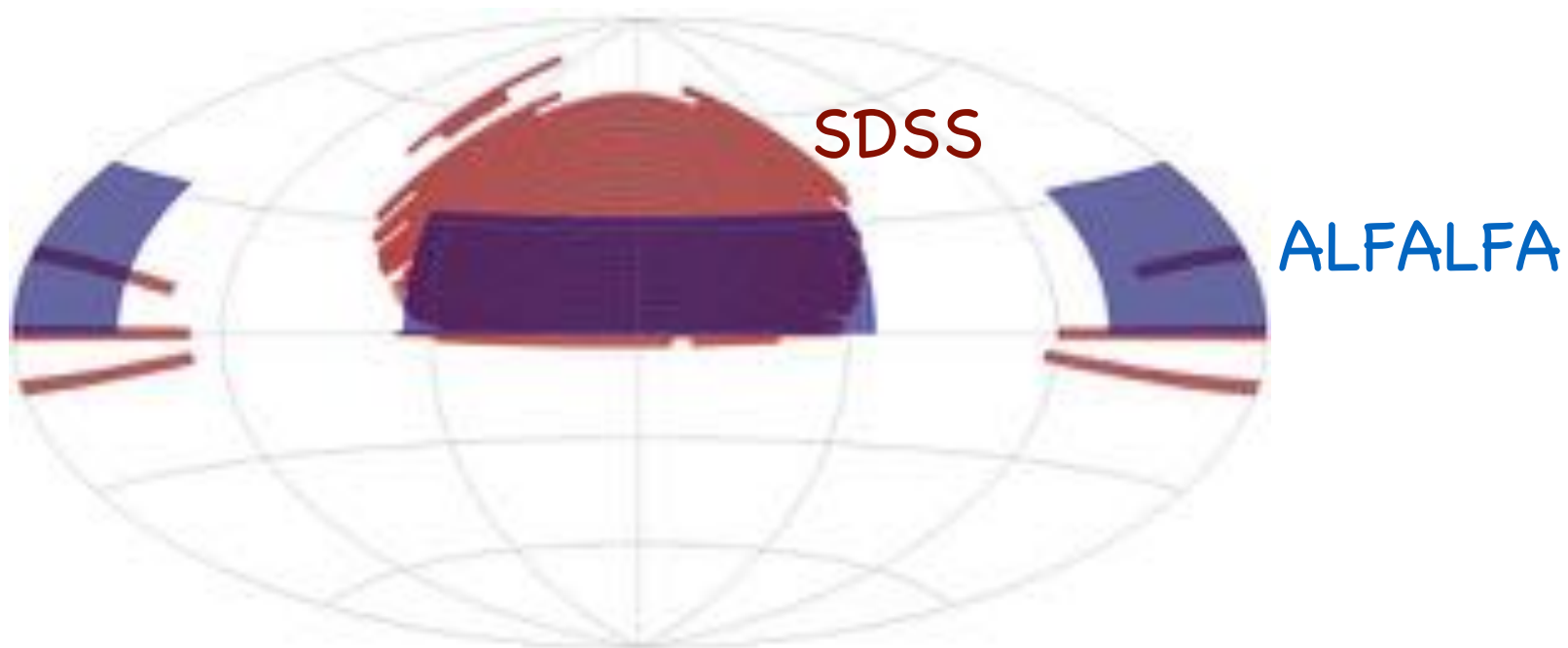
$$\omega(\gamma) = \frac{1}{N} \sum_{i=1}^N \frac{DD(\gamma) - RR_i(\gamma)}{RR_i(\gamma)}$$

Compute $\omega(\gamma)$ for a sample of HI sources from ALFALFA survey

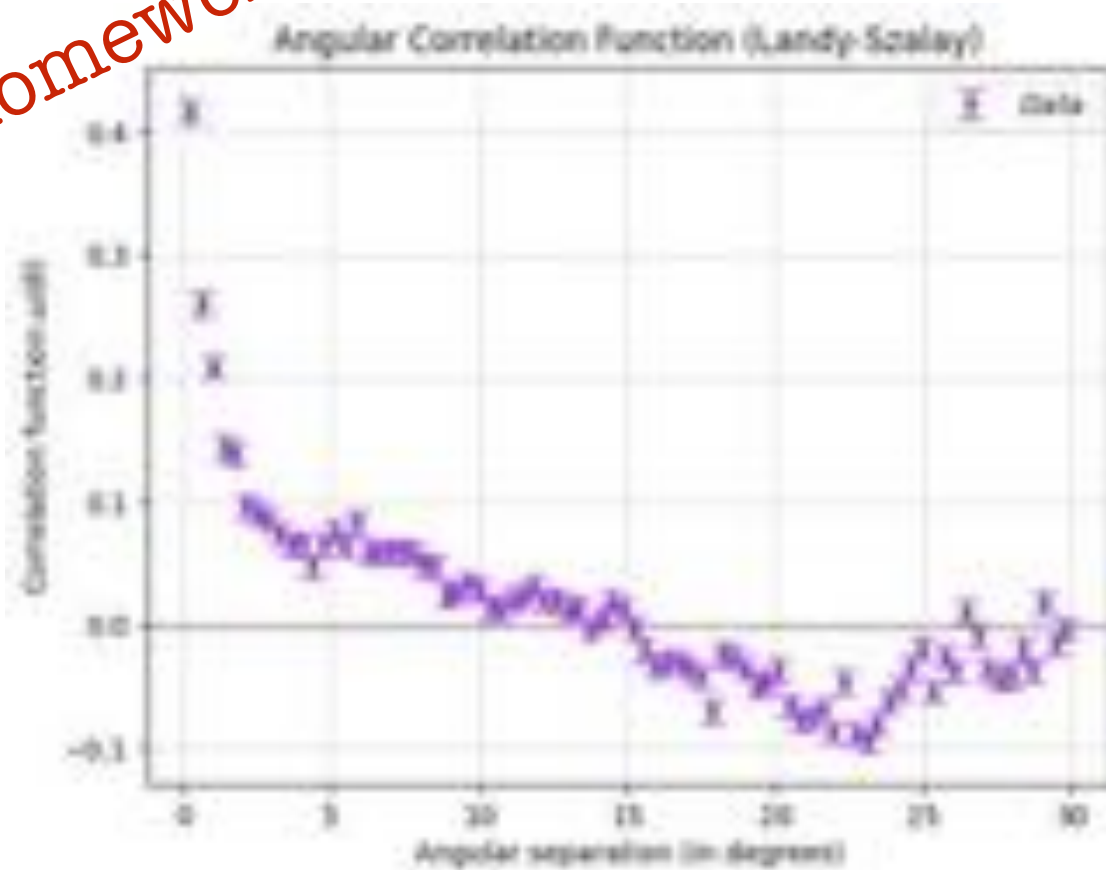
- 2D with data on a sphere with: $\theta \in [\theta_1, \theta_2]$, $\phi \in [\phi_1, \phi_2]$

$$\gamma = \cos^{-1}[\cos(\theta_1) \cos(\theta_2) + \sin(\theta_1) \sin(\theta_2) \cos(\phi_1 - \phi_2)]$$

Survey ALFALFA



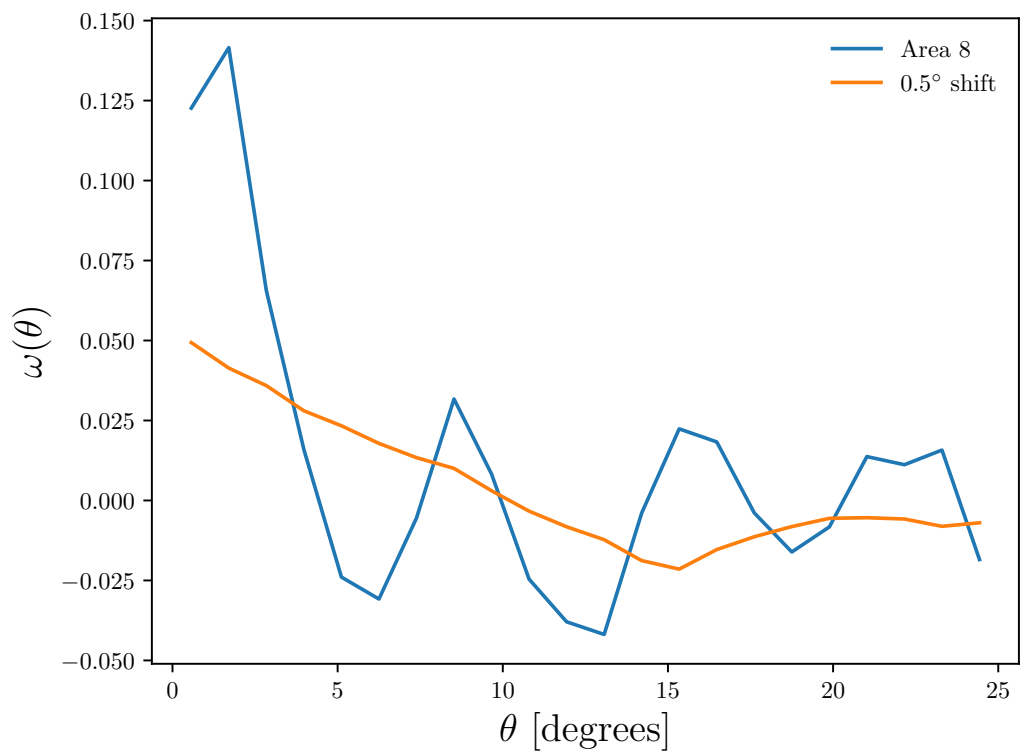
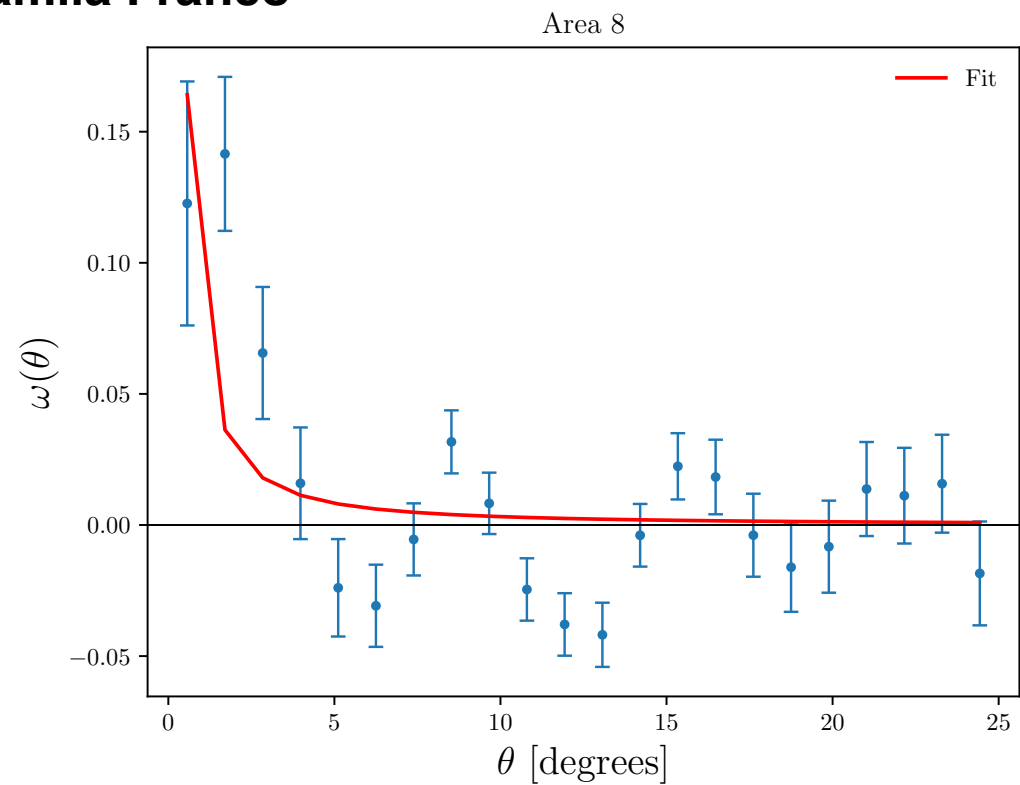
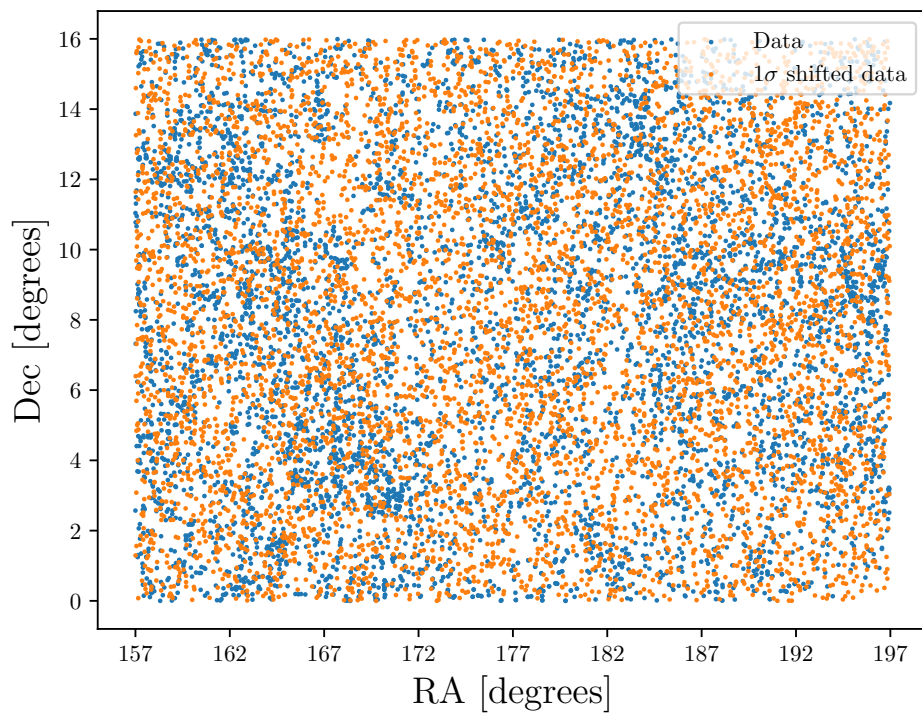
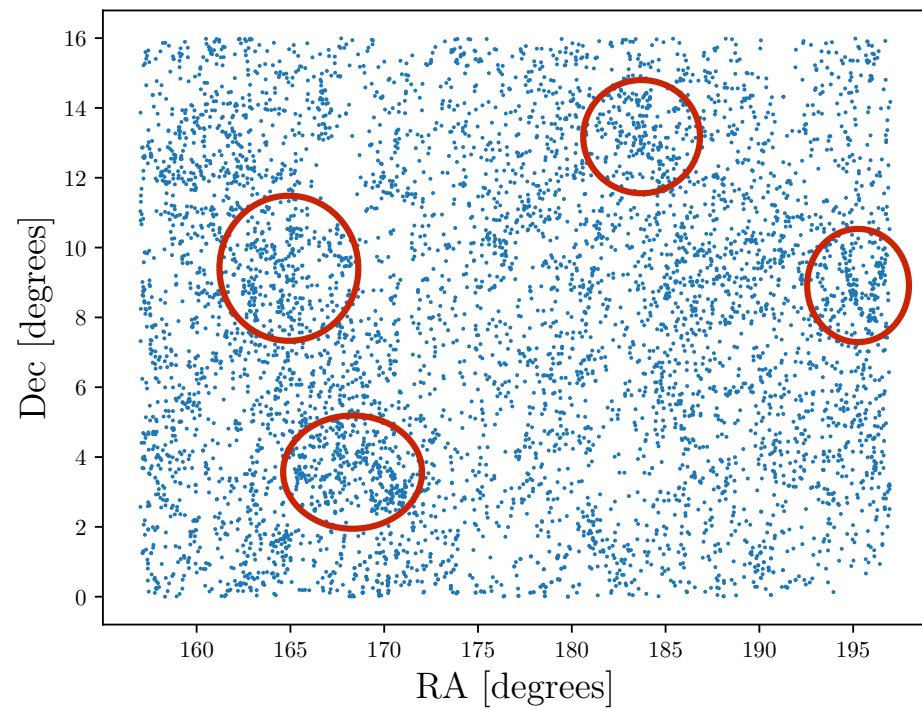
Homework



GitHub: 2PACF

https://github.com/mavipoppi/wsON_correlationfunction

Gentileza de: **Maria Vitoria Lazarin**





The cosmological model of the Universe

stands on:

- ▶ Metric theory, e.g., General Relativity
- ▶ Cosmological principle
- ▶ **Observational probes**

Traditional Observational Probes:

① **Expansion of the Universe**



1929-1931



1945-1960

② **Nucleosynthesis of primordial nuclei**



1964- ...

③ **Cosmic Microwave Background Radiation**

①

“Grande debate de 1920”: *universo de estrelas x universo de galáxias*

Harlow Shapley	Heber D. Curtis
Via Láctea muito grande Sol a 15 kpc do centro Nebulosas fazem parte da galáxia	Via Láctea pequena Sol está no centro Nebulosas são “universos ilhas”



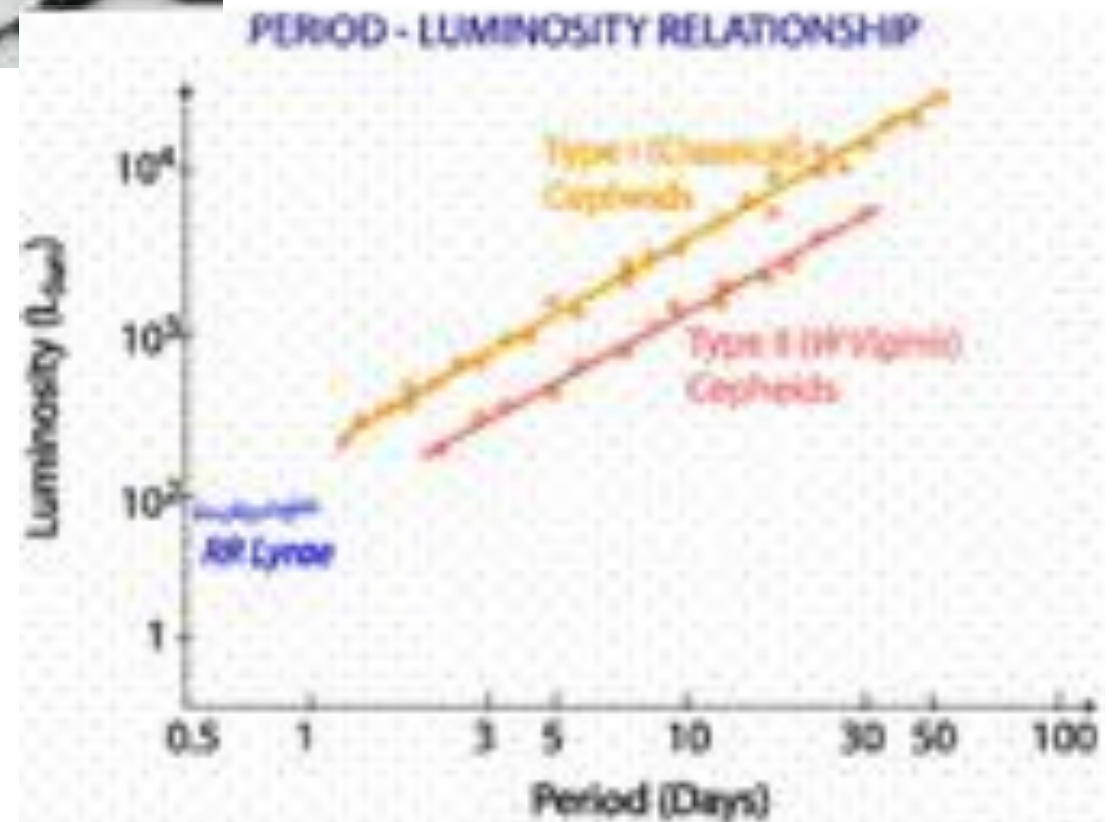
- O grande problema era a determinação de distâncias das nebulosas.

①



Henrietta Leavitt 1867-1921

She studied variable stars and discovered the **period-luminosity** relationship





distância Via Láctea-Andrômeda:

$$d_L(\text{M31}) = 760 \pm 50 \text{ kpc}$$

diâmetro da VL: 32Kpc



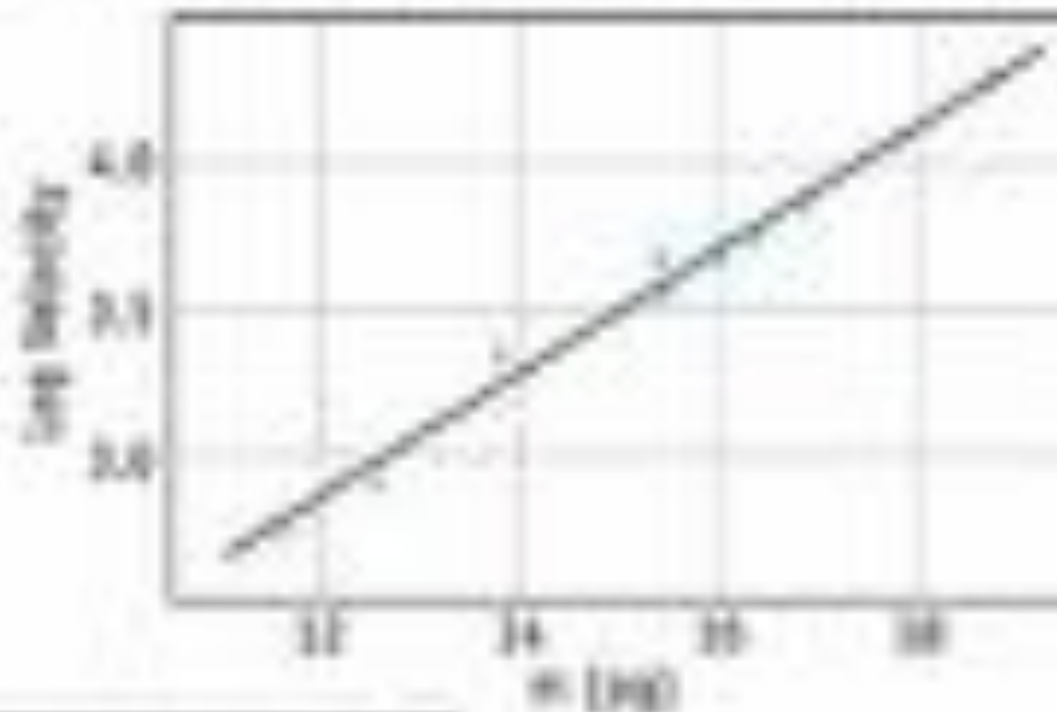
IMPRESSA COSMICA, uma longa fotografia de galáxia de Andrômeda, obtida em 1943 pelo astrônomo Edwin Hubble, foi a primeira comprovação de que havia outras galáxias além da Via Láctea. O instrumento "200" analisava uma região de linha vertical, usada como instrumento de medida para mostrar que Andrômeda estava fora do nosso galáxia.

①

DISCOVERY OF EXPANDING UNIVERSE



Edwin Hubble

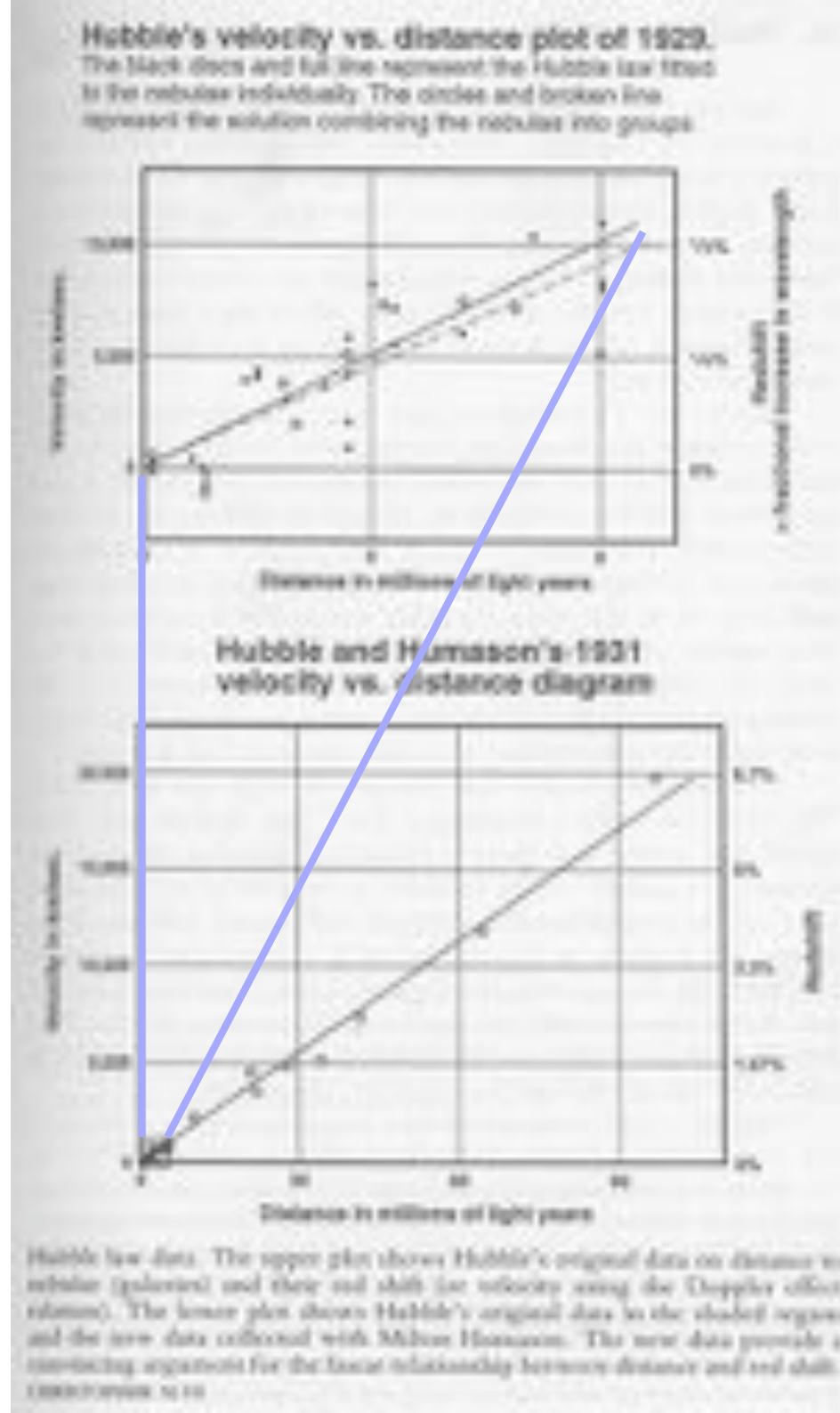


HST, Hubble
Space
Telescope



Hubble, **1929**

Hubble &
Humason, **1931**

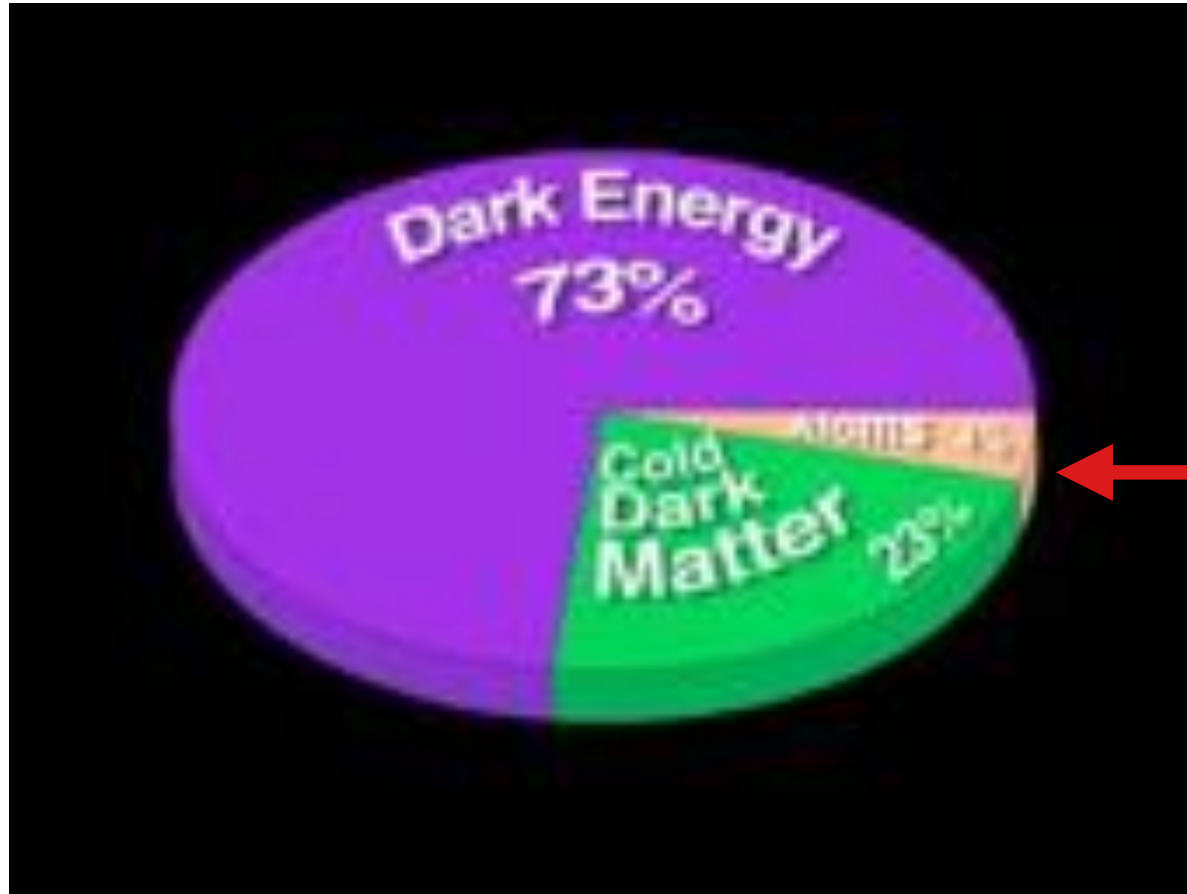


Traditional Observational Probes:

- ① Expansion of the Universe  1929-1931
-  1945-1960
② Nucleosynthesis of primordial nuclei
-  1964- ...
③ Cosmic Microwave Background Radiation

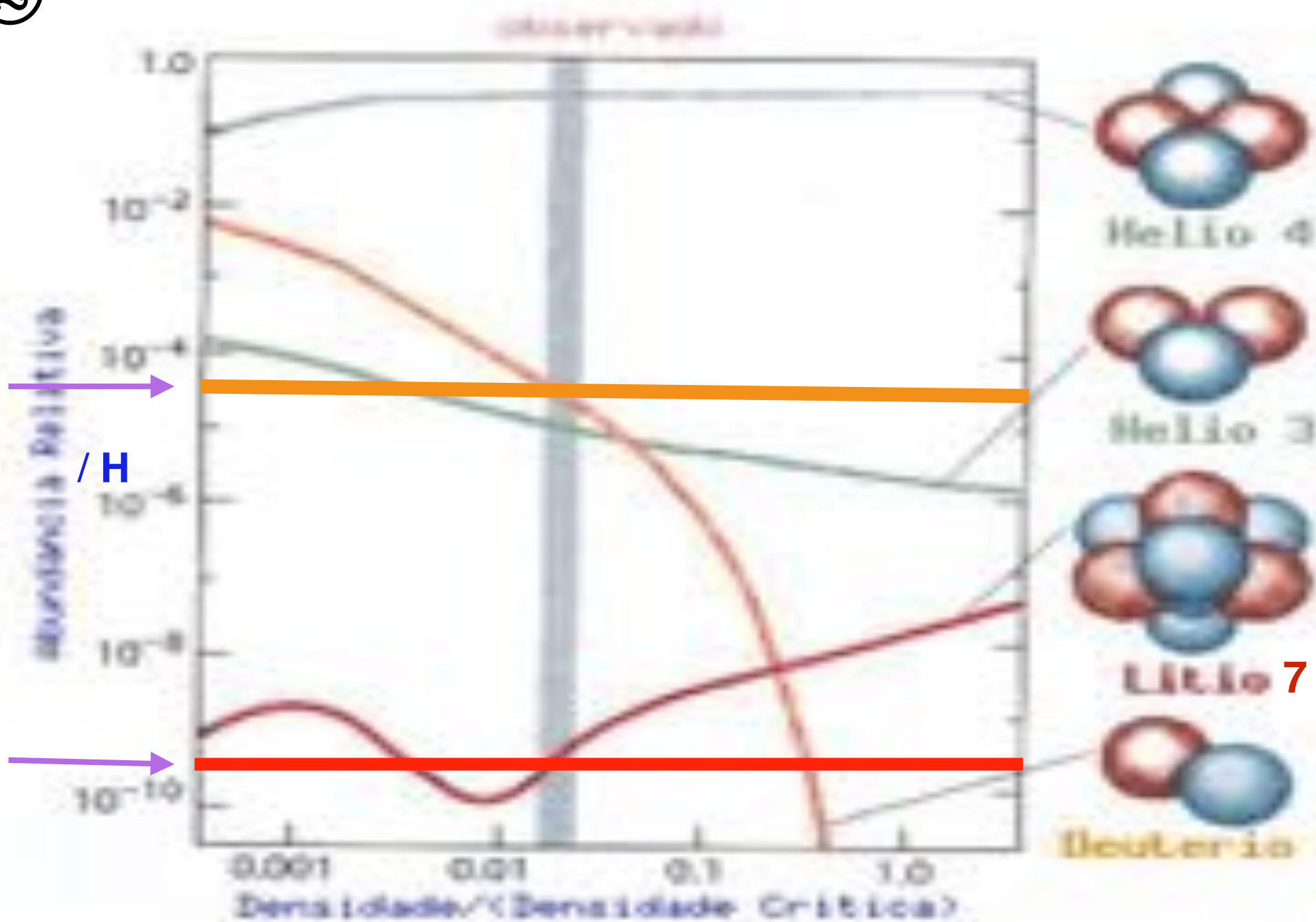
②

What is the universe made of?



← Matéria
Bariônica

22



Matéria Bariônica

The Origin of the Solar System Elements

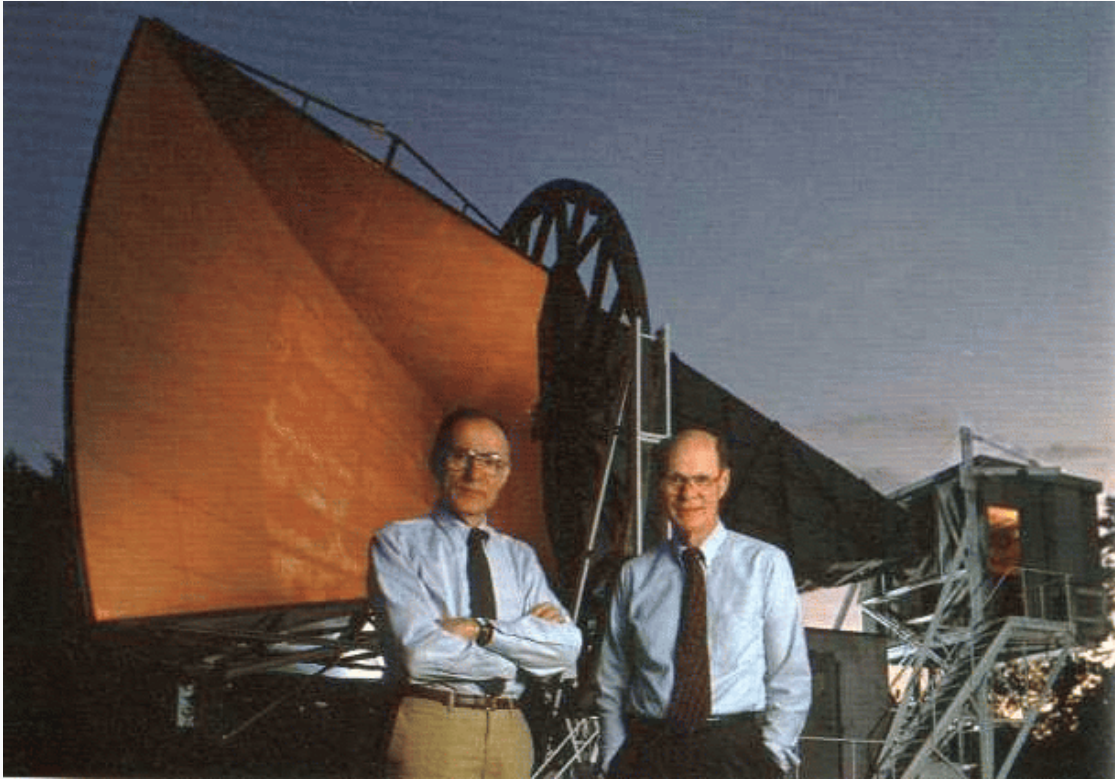


Traditional Observational Probes:

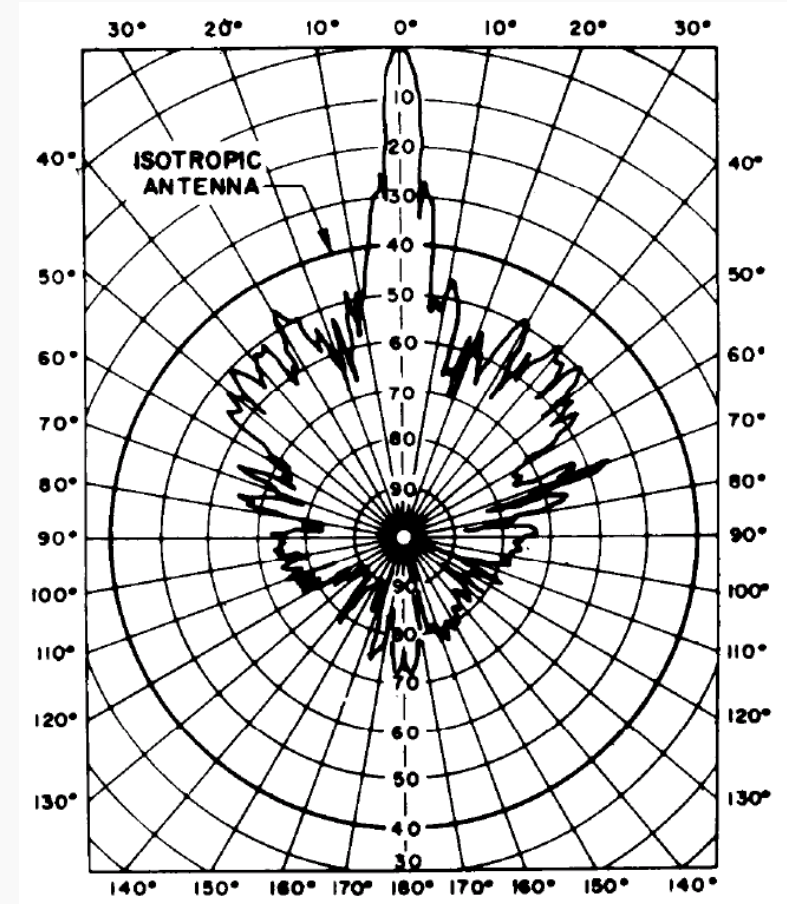
- ① Expansion of the Universe  1929-1931
- ② Nucleosynthesis of primordial nuclei  1945-1960
- ③ Cosmic Microwave Background Radiation  1964- ...

③

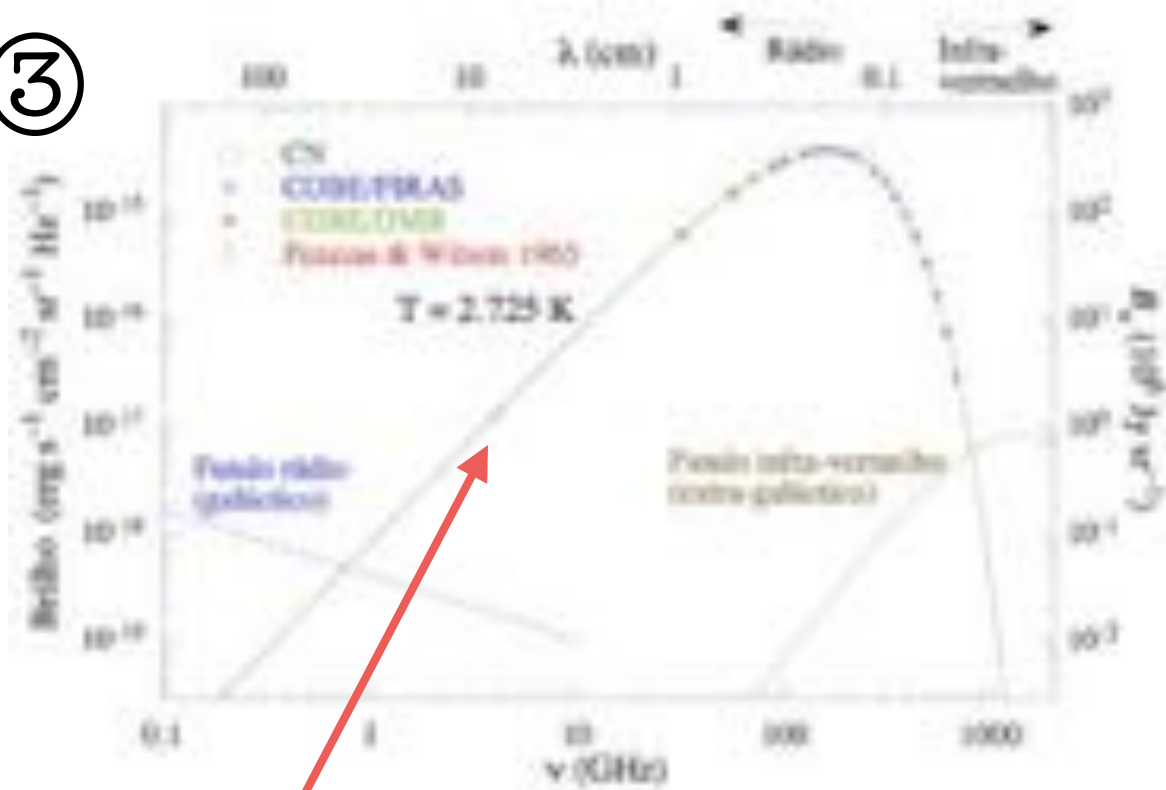
A descoberta da RCF (1964)



- Antena projetada em 1960 para testes de comunicação de baixo ruído com o satélite echo.
- Sistema direcional de baixo ruído (< 0.05 K) operando em $\lambda = 7.35$ cm.



③



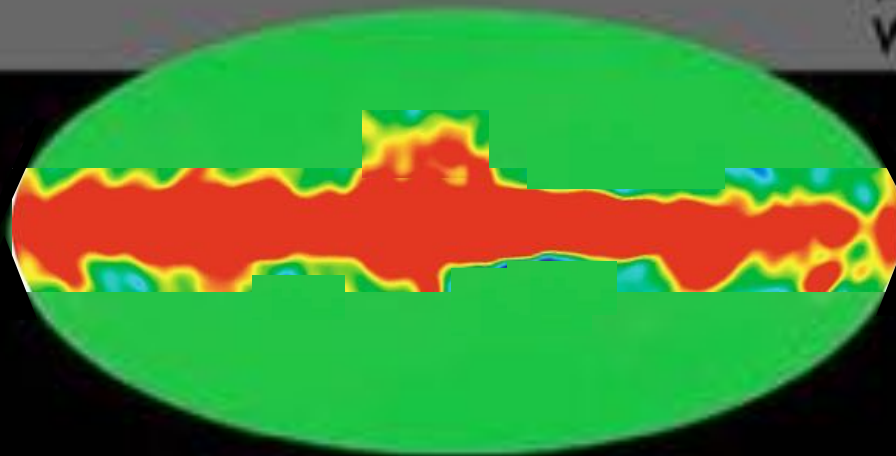
cosmic noise?



1965

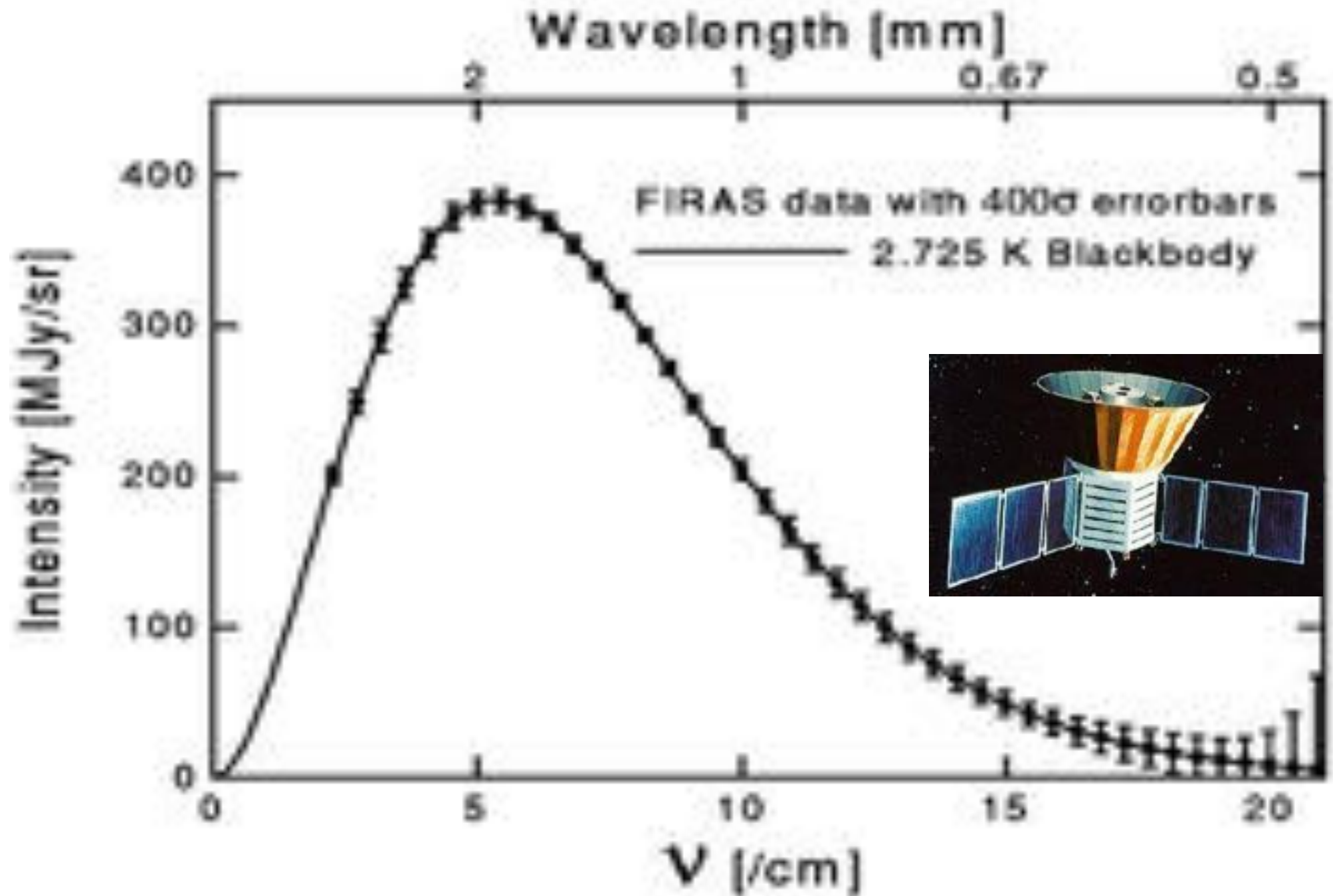


Penzias and
Wilson

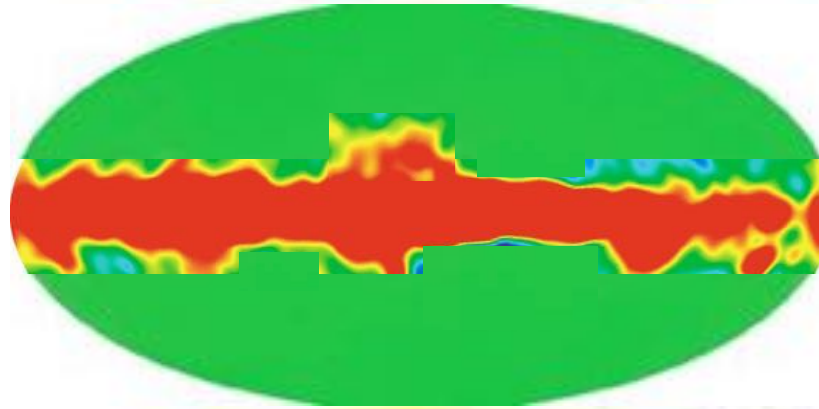
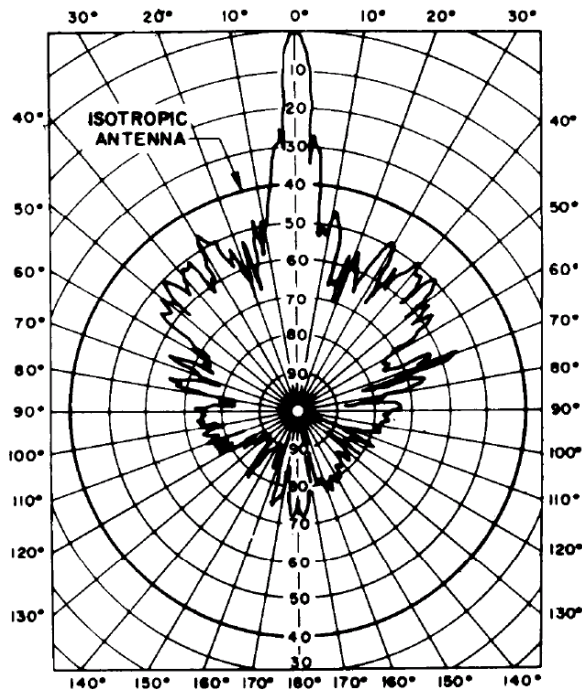


③

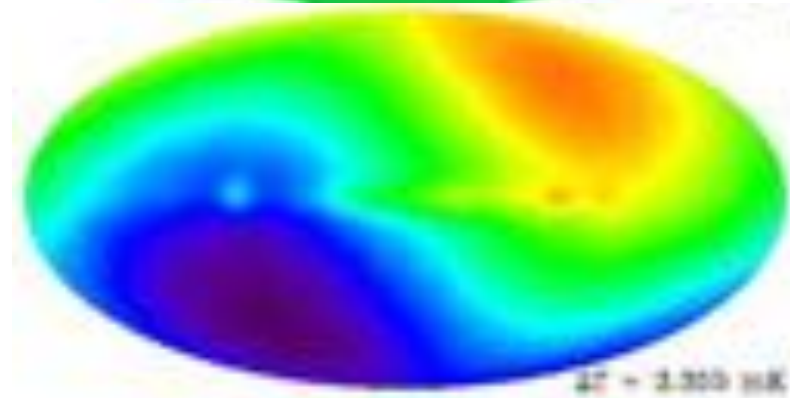
Black-body radiation



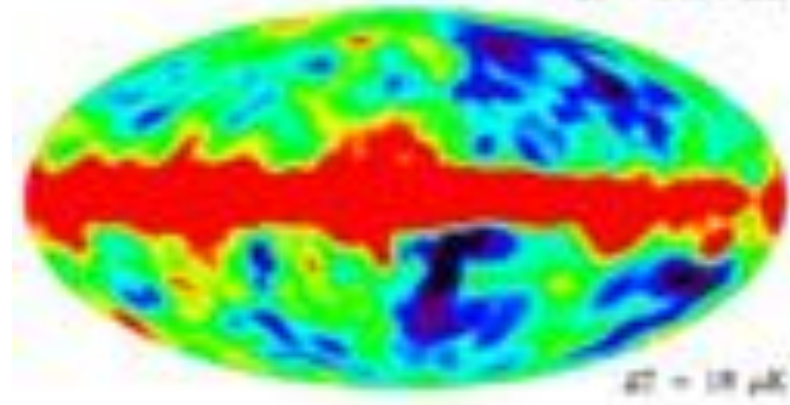
COBE's maps



Monopole



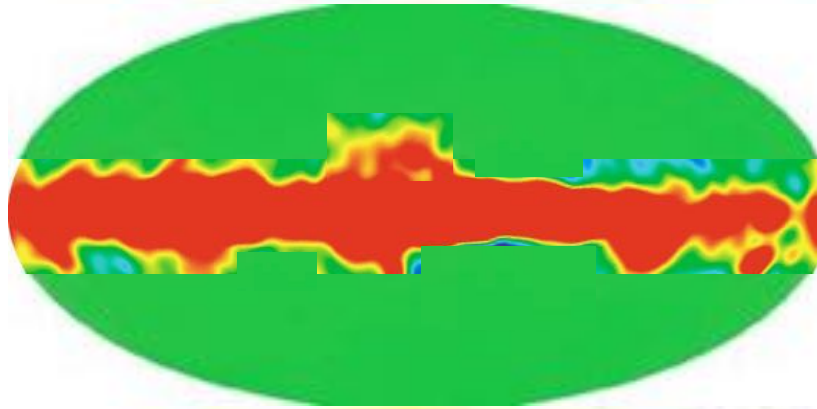
Dipole



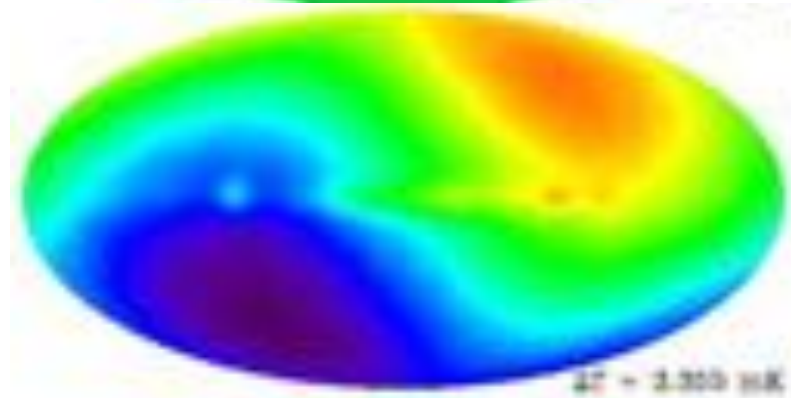
??

③

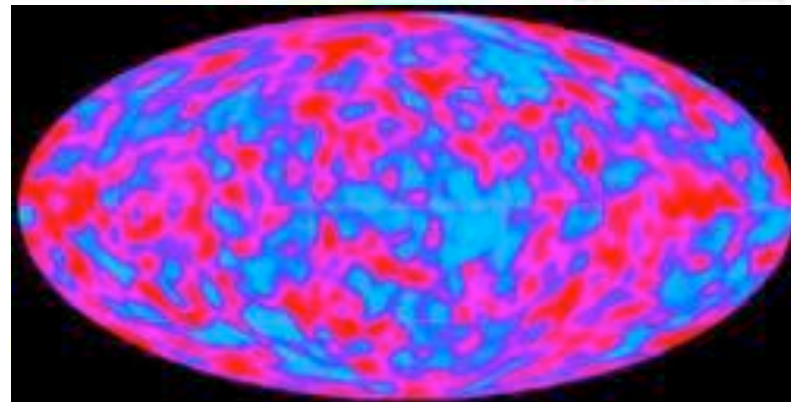
COBE's maps



Monopole



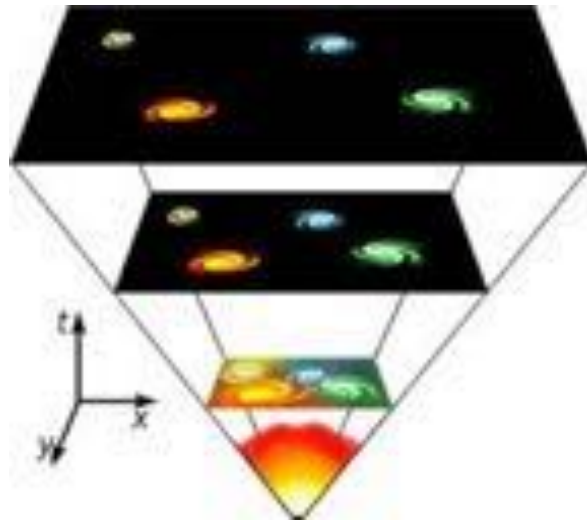
Dipole



- se houve um passado denso e quente, então matéria e radiação acoplaram-se —em equilíbrio termodinâmico— até o Universo esfriar o suficiente; depois desacoplaram e os fótons formam uma radiação relíquia que viaja (quase) livre
- em aproximação zero (= background), mostra-se que o Universo que expande esfria (isto pressupõe condições adiabáticas e a 1ra. lei da termodinâmica)



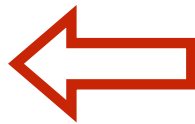
Hubble, 1929



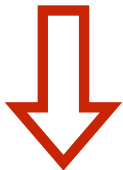
Expansion of the Universe
implies a dense and hot past!



A hot gas of photons in thermodynamic equilibrium in an expanding Universe implies (dQ=0 + 1st. law):



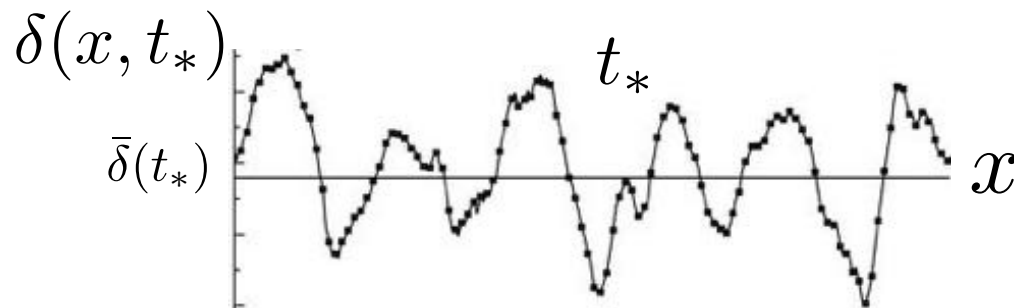
$$T(t) = \frac{a_0 T_0}{a(t)}$$



Thermal history of the Universe

Corollary: A cosmic time t exists
and is well defined

- se houve um passado denso e quente, então matéria e radiação acoplaram-se —em equilíbrio termodinâmico— até o Universo esfriar o suficiente; depois desacoplaram e os fótons formam uma radiação relíquia que viaja (quase) livre
- em aproximação zero (= background), mostra-se que o Universo que expande esfria (isto pressupõe condições adiabáticas e a 1ra. lei da termodinâmica)
- a ordem zero não explica a formação de estruturas: precisamos perturbações do campo de densidade de matéria (equivalentemente, do potencial gravitacional)



$$\delta(x, t_*) \equiv \frac{\rho(x, t_*) - \bar{\rho}(t_*)}{\bar{\rho}(t_*)}$$

- se houve um passado denso e quente, então matéria e radiação acoplaram-se —em equilíbrio termodinâmico— até o Universo esfriar o suficiente; depois desacoplaram e os fótons formam uma radiação relíquia que viaja (quase) livre
- em aproximação zero (= background), mostra-se que o Universo que expande esfria (isto pressupõe condições adiabáticas e a 1ra. lei da termodinâmica)
- a ordem zero não explica a formação de estruturas: precisamos perturbações do campo de densidade de matéria (equivalentemente, do potencial gravitacional)
- perturbações na matéria geram flutuações no campo da radiação (devido ao acoplamento fótons-bárions)

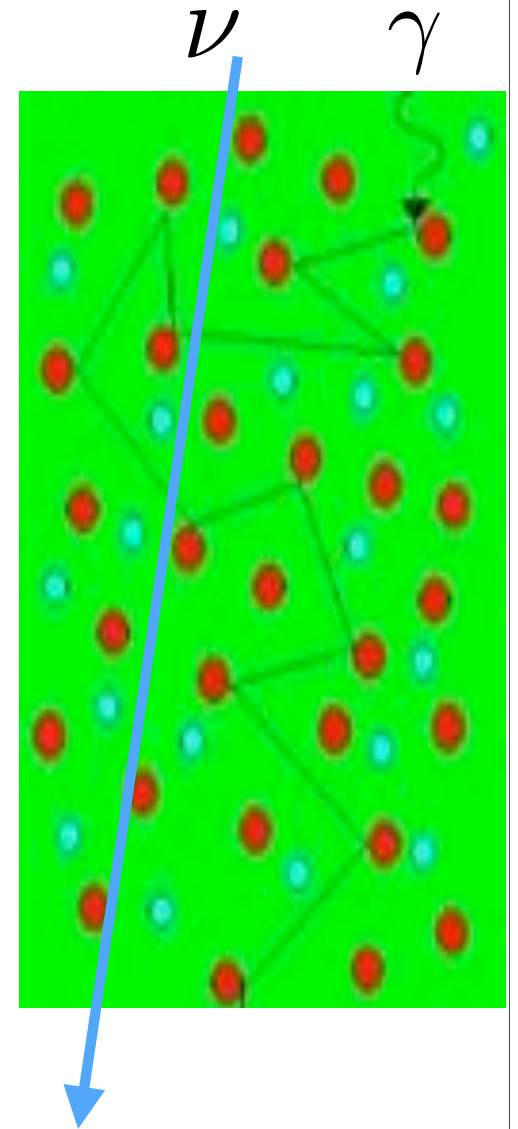
a história do Universo: passado denso e quente

- Houve uma fase onde o fluido **matéria–radiação** (composto por bárions e fótons interagindo via espalhamento Thomson) estava em **equilíbrio termodinâmico**, e agia como se fosse um fluido só (photon-baryon fluid); $\eta \equiv \frac{n_\gamma}{n_b} \simeq 10^9$.

$$1K = 8.6 \times 10^{-5} \text{ eV}$$

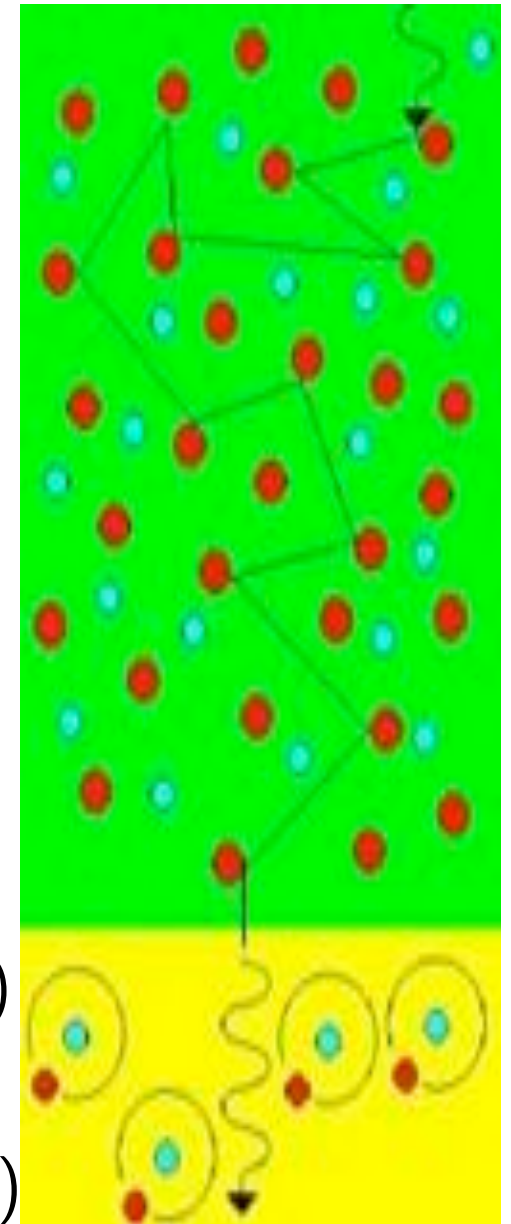
$$T = \frac{T_0}{a(z)} = 3K(1 + z)$$

$$z_{LSS} \simeq 1100 \rightarrow T_{LSS} \simeq 3000K$$



a história do Universo: passado denso e quente

- ▶ Houve uma fase onde o fluido **matéria–radiação** (composto por bárions e fótons interagindo via espalhamento Thomson) estava em **equilíbrio termodinâmico**, e agia como se fosse um fluido só (photon-baryon fluid); $\eta \equiv \frac{n_\gamma}{n_b} \simeq 10^9$.
- ▶ Ao expandir-se o Universo resfria e o fluido alcança uma temperatura crítica que produz o desacoplamento **matéria–radiação**: $T \simeq 3000 \text{ K} \simeq 0.3 \text{ eV}$.
- ▶ Esses fótons livres (de ser espalhados pelos elétrons) constituem uma radiação relíquia do Universo primordial, chamada **Radiação Cósmica de Fundo** (RCF)



1962



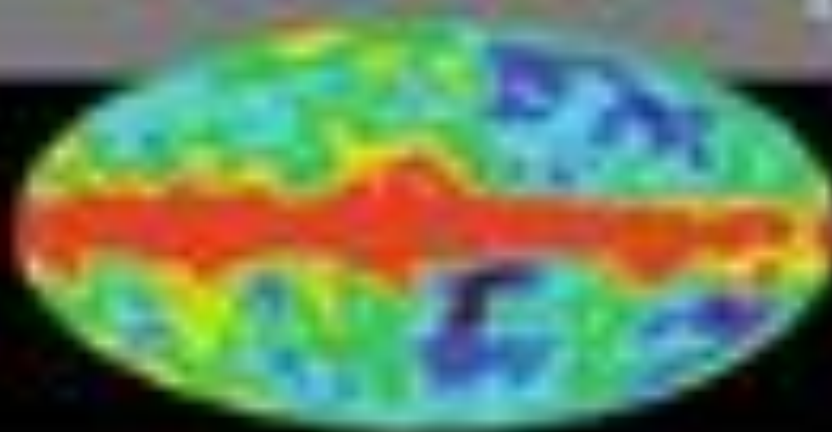
Purcell and
Williams



1964



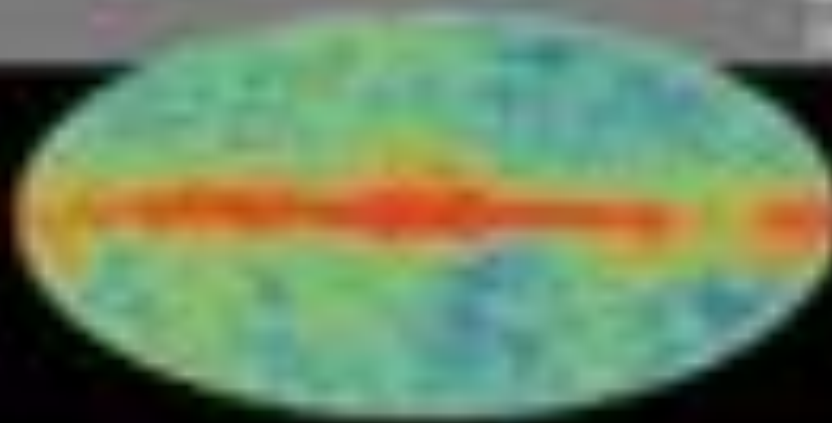
1969



1971

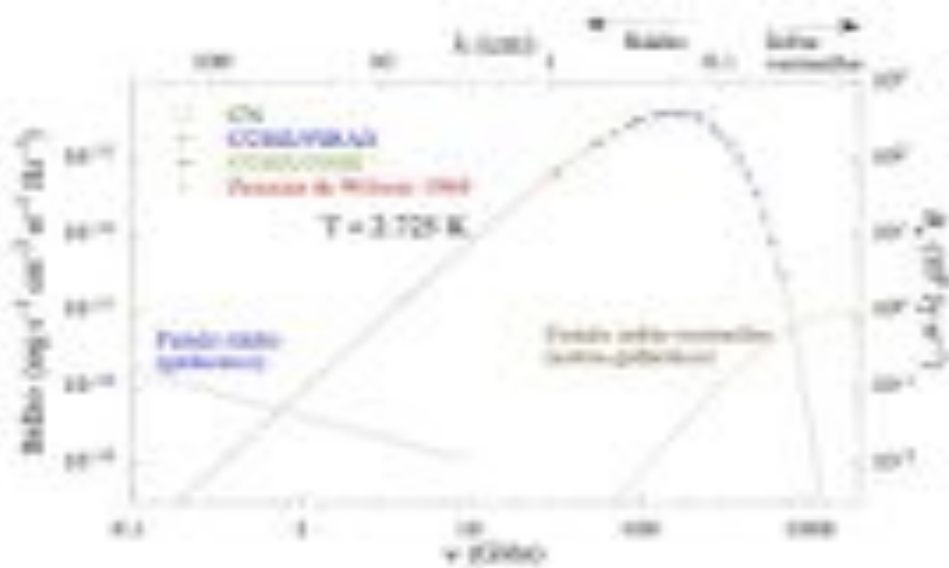


1974
Department



R_{CF}: espectro de corpo negro à temperatura $T_{\text{Planck}} = (2.725 \pm 0.001)\text{K}$

1

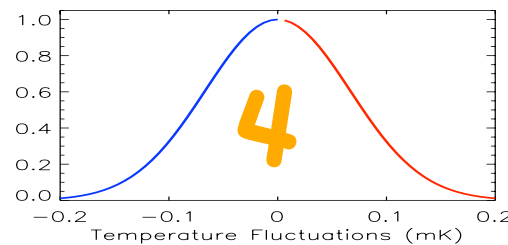
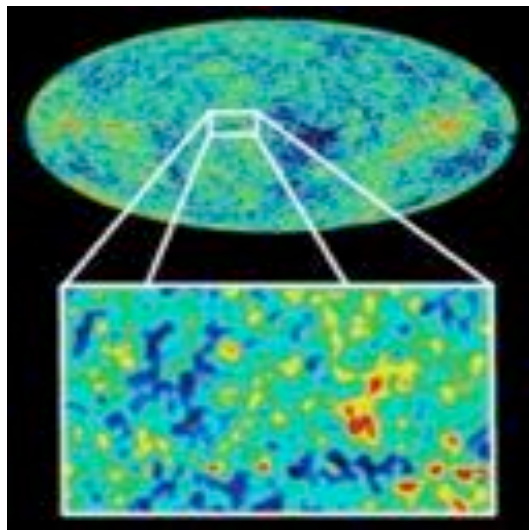


1965 – 1992

2



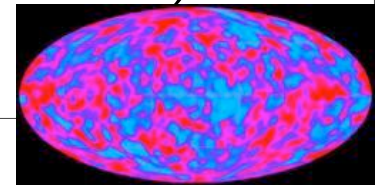
3 Em 1992 verificou-se que ao redor da $T_{\text{Planck}} \exists$ pequenas flutuações positivas $\Delta T > 0$ e negativas $\Delta T < 0$, da ordem $\frac{\Delta T}{T_{\text{Planck}}} \sim 10^{-5}$



→ $\Delta T \sim (-200\mu\text{K}, 200\mu\text{K})$

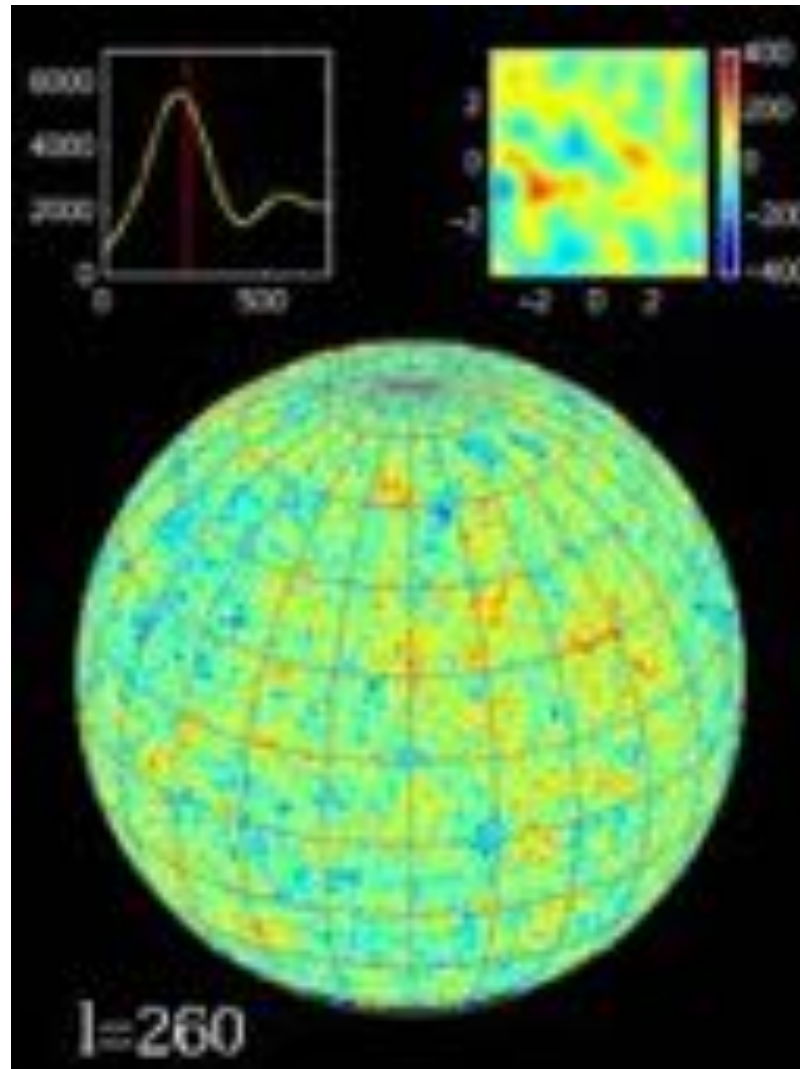
Estas flutuações de temp. ΔT ficam visíveis neste mapa depois de retirar da RCF as componentes monopolo (2.725K) e dipolo (3.346mK)

5

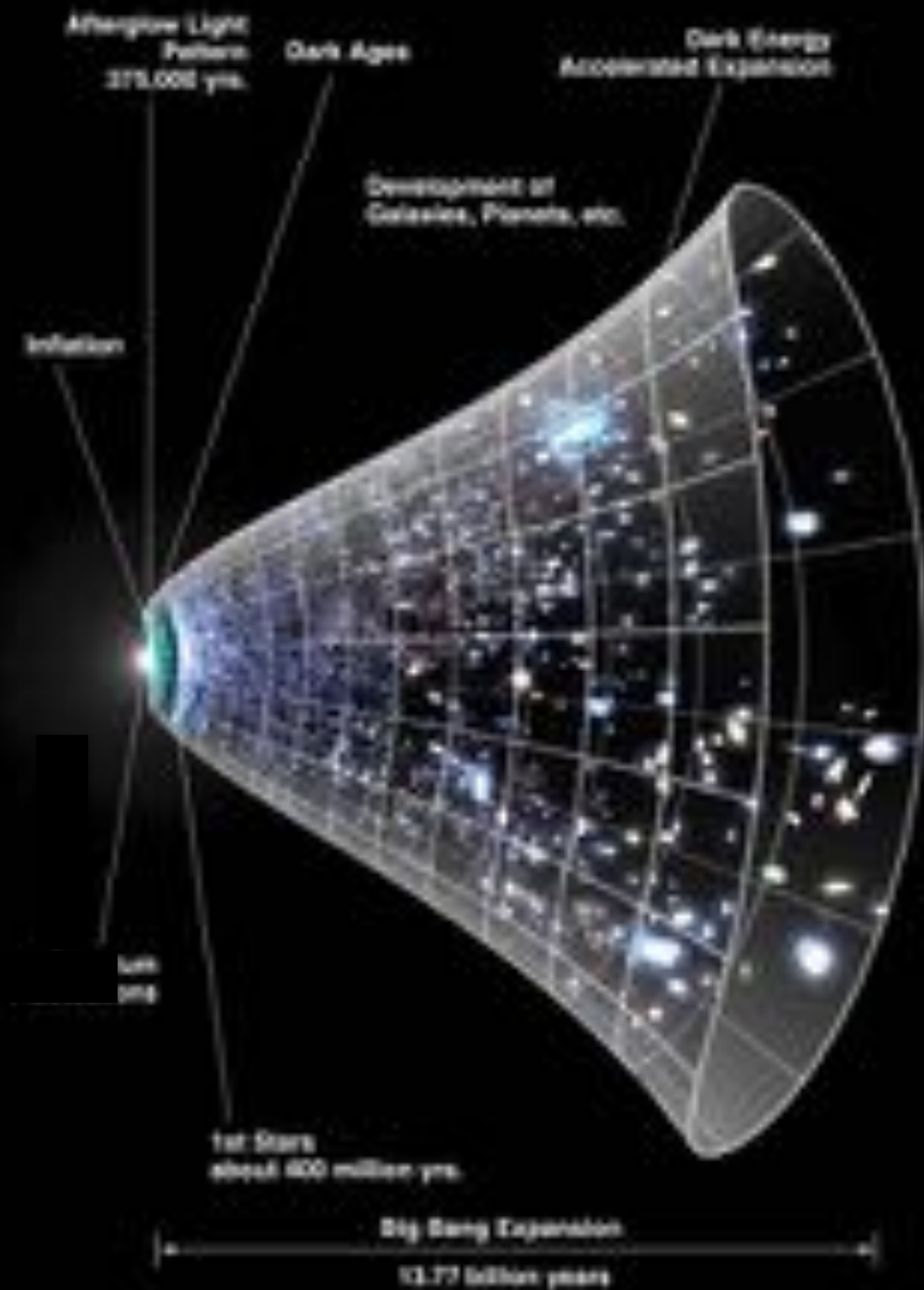


Harmonic Multipoles and the CMB sky: <http://spud.spa.umn.edu/~pryke/logbook/20000922/>

http://spud.spa.umn.edu/~pryke/logbook/20000922/cumulative_cmb.html



Large Scale Structure



Modern Observational Probes:

- ▶ Acceleration of the Universe  1998
- ➡ BAO: baryon acoustic oscillations  2005
- ➡ Growth of cosmic structures  2005-today
- ▶ Probes of stat. homogeneity & isotropy  2000-today
- ▶ CMB lensing, evidences of DM, etc.  2010-today  2000-today

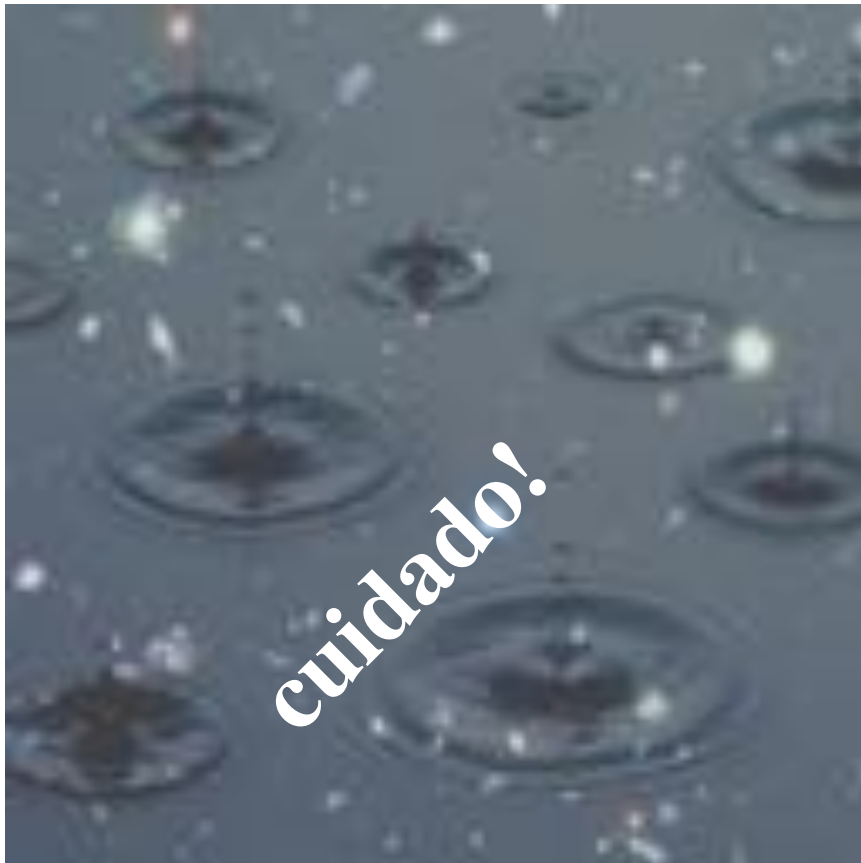
Modern Observational Probes:

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- ▶ Probes of stat. homogeneity & isotropy  2000-today
- ▶ CMB lensing, evidences of DM, etc.
 2010-today  2000-today

BAO: a standard ruler



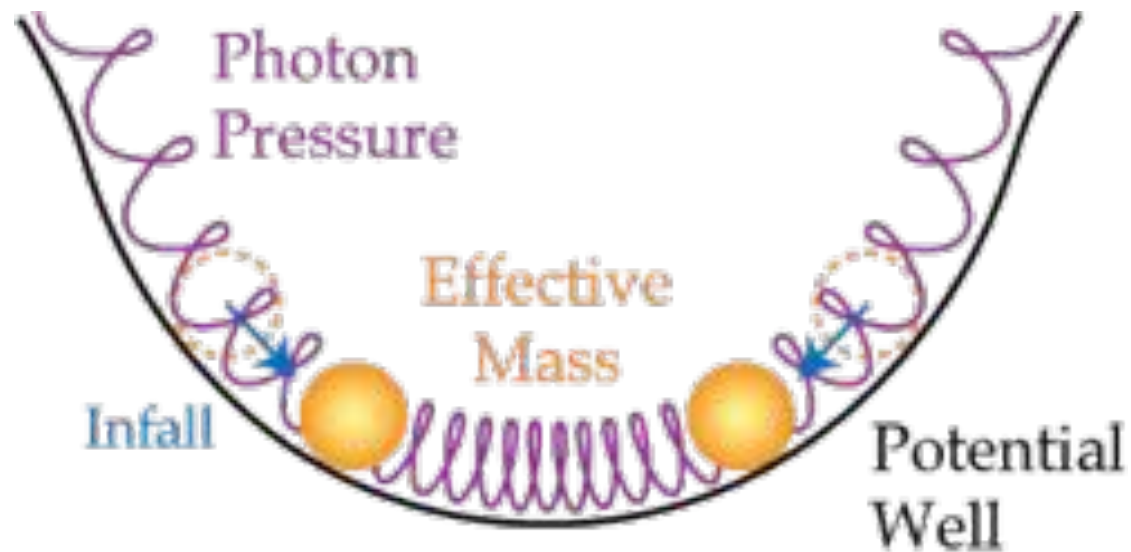
Perturbations in the primordial plasma produced: 3D Sound Waves



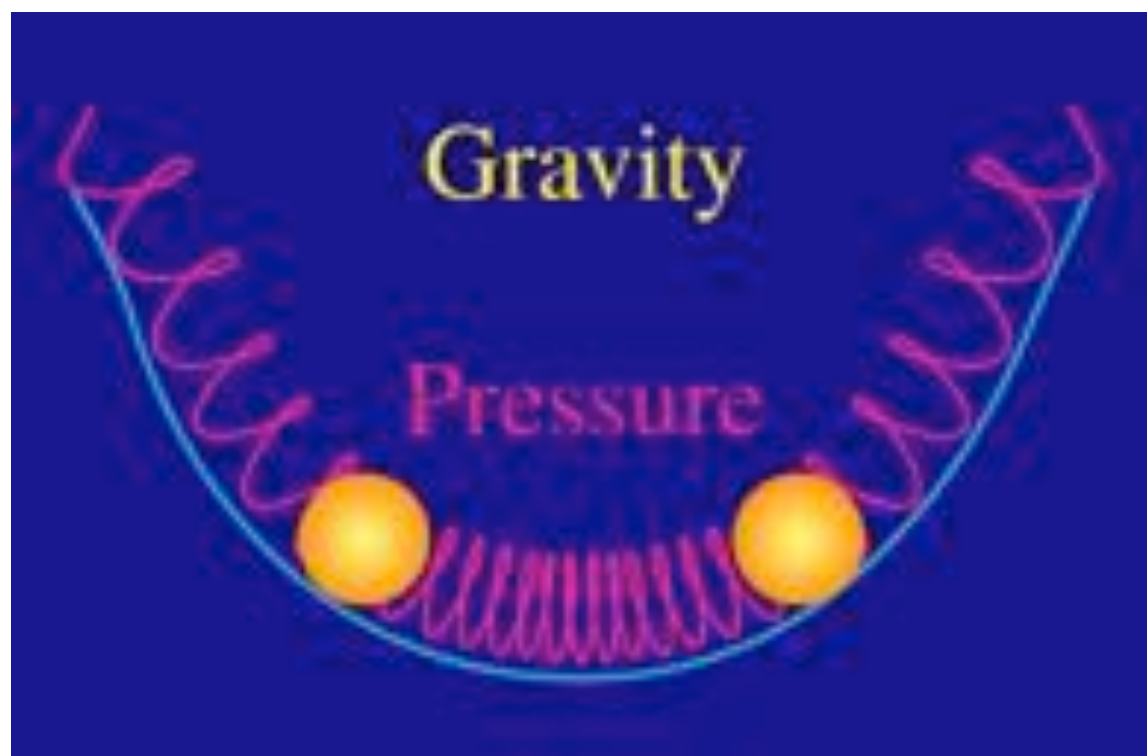
<https://www.youtube.com/watch?v=jpXuYc-wzk4>

Nature of [CMB+Baryons] temperature fluctuations

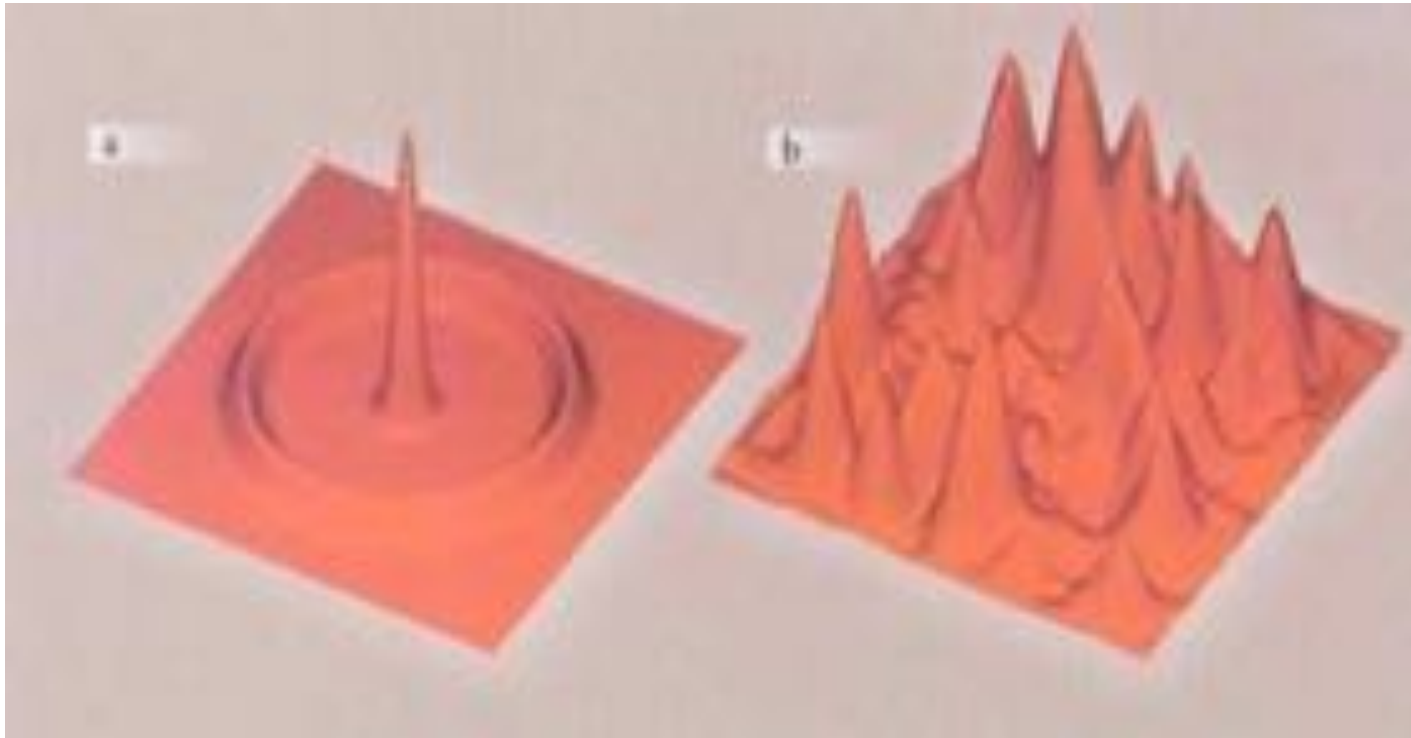
BAO originate because a tightly coupled matter-radiation fluid interacts with dark matter potential wells

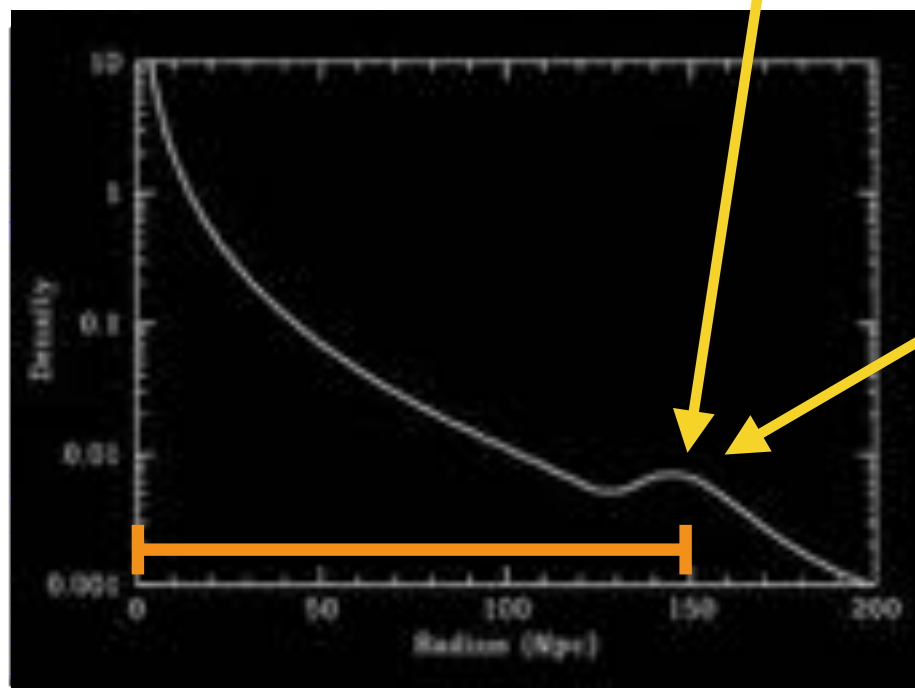
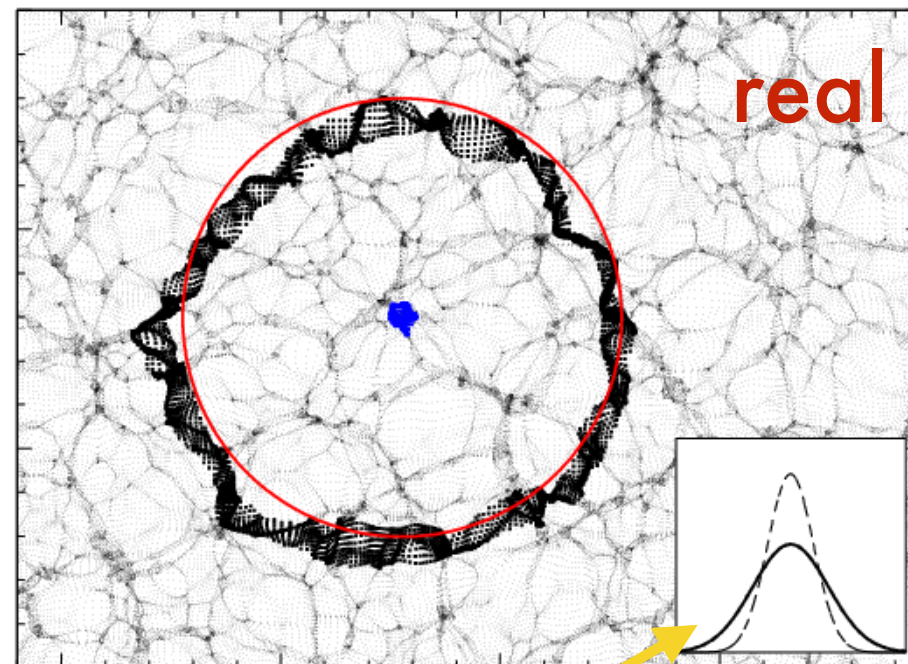
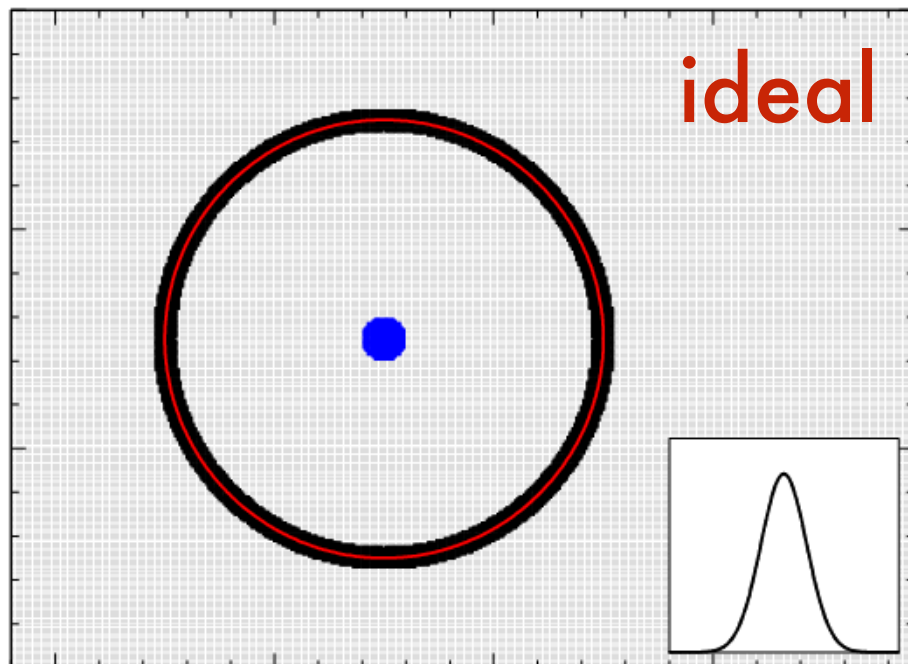


Denser is hotter: $\delta\rho_{\gamma b}(t, \mathbf{r}) \sim \delta T(t, \mathbf{r})$



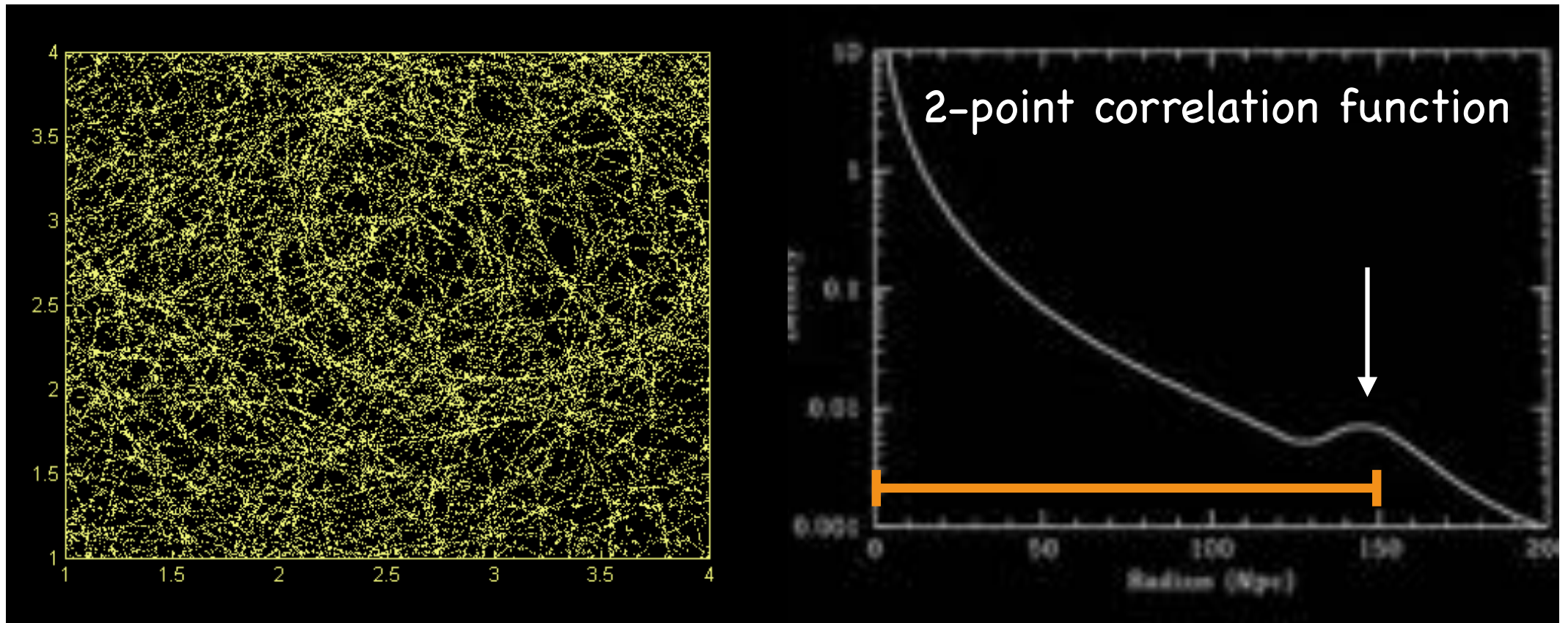
BAO: baryon acoustic oscillations



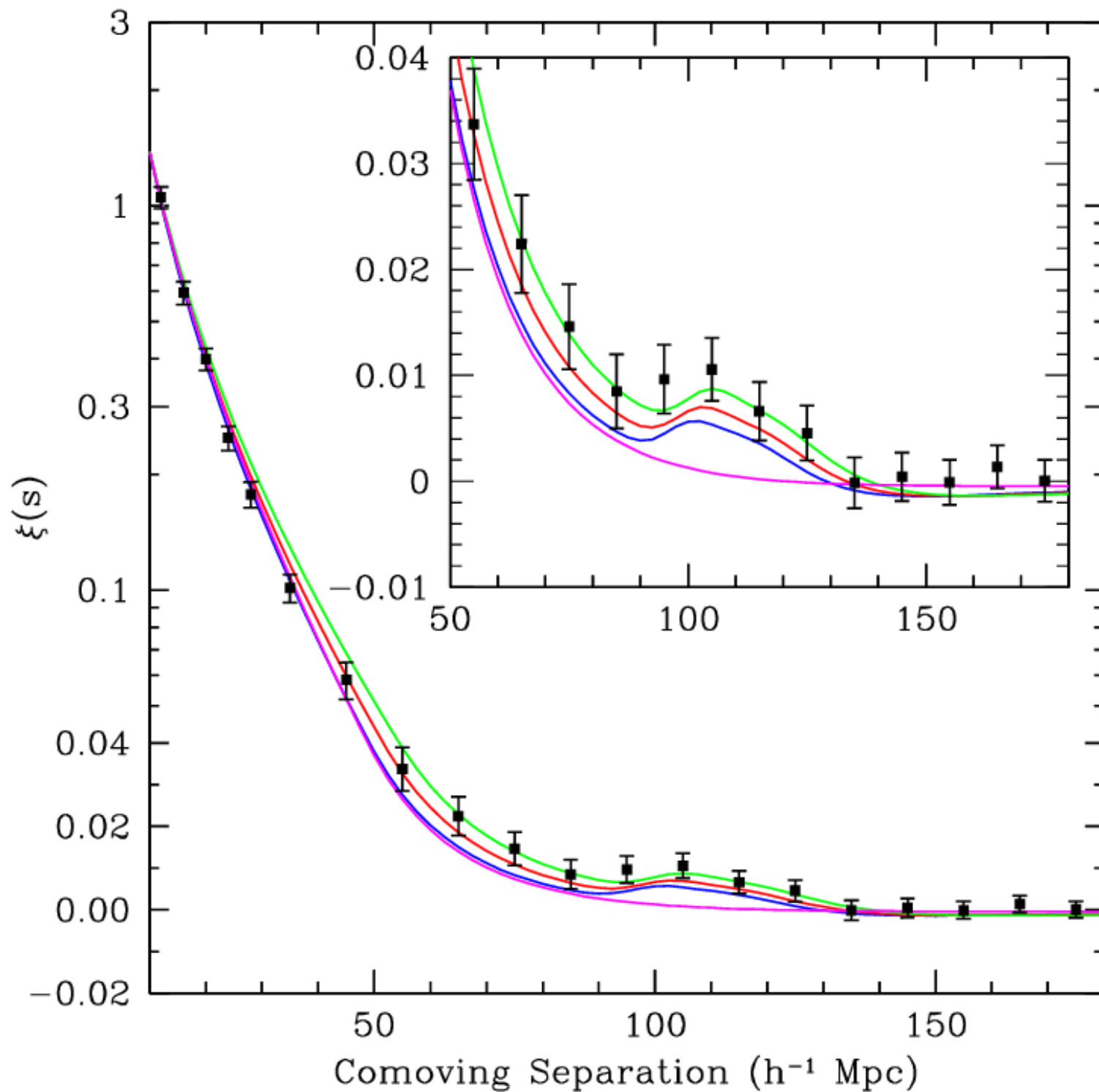


BAO: standard cosmological ruler

- Small but detectable signal



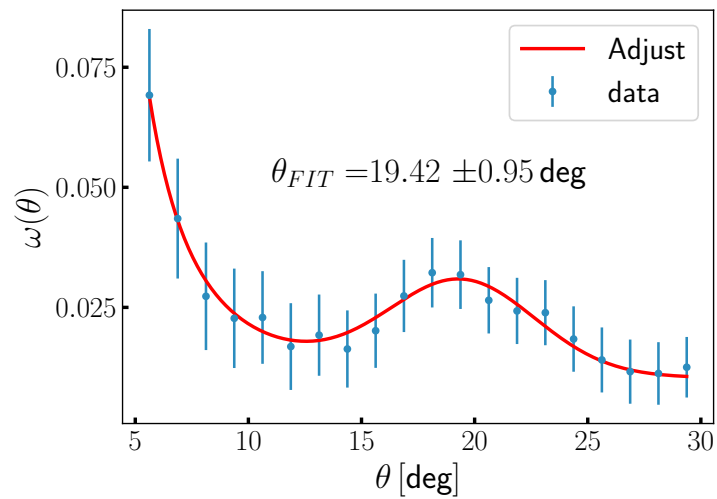
<https://www.youtube.com/watch?v=jpXuYc-wzk4>



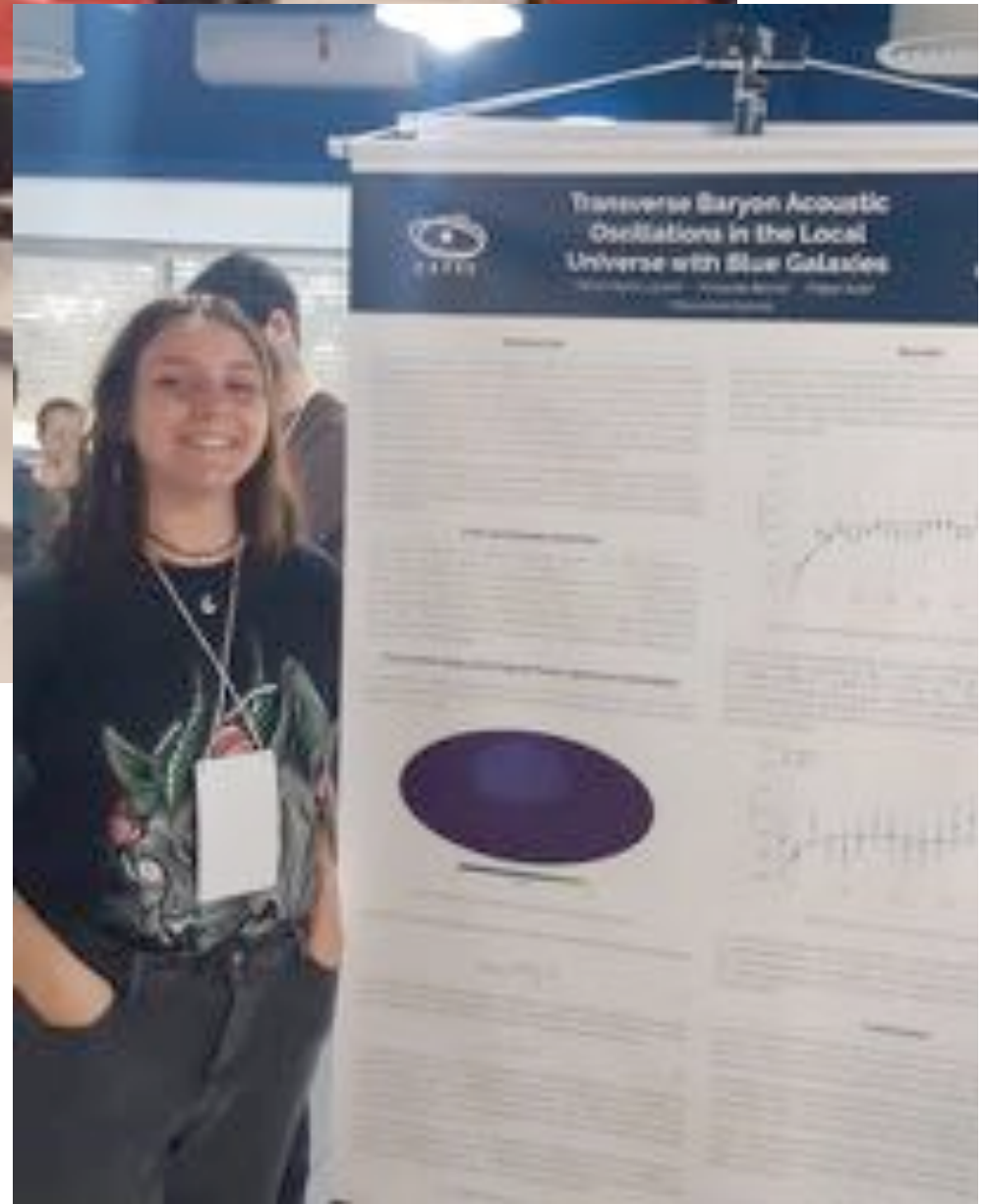
2-point
correlation
function

BAO 3D

Eisenstein et al.
(SDSS), 2005



2PACF
w/blue
galaxies

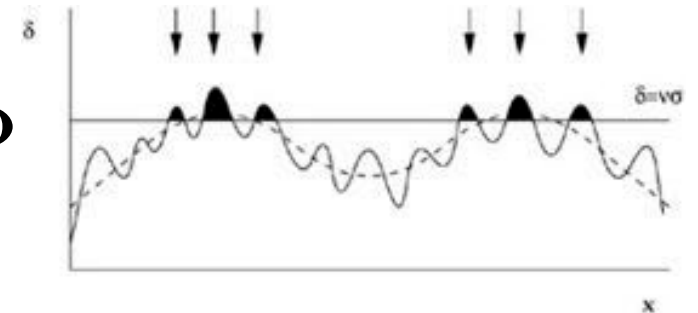


Modern Observational Probes:

- ▶ Acceleration of the Universe  1998
- ▶ BAO: baryon acoustic oscillations  2005
- ▶ **Growth of cosmic structures**  2005-today
- ▶ Probes of stat. homogeneity & isotropy  2000-today
- ▶ CMB lensing, evidences of DM, etc.  2010-today  2000-today

Spacetime density fluctuations:

$$\delta\Phi \Longrightarrow \delta T_{\mu\nu} \Longrightarrow \delta g_{\mu\nu} \Longrightarrow \delta\Phi$$



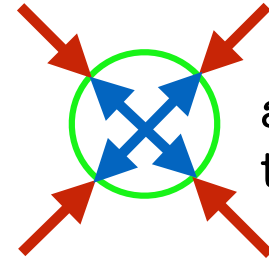
➡ Perturbed Einstein eqs.: Continuity, Euler, Laplace

Structures formation: evolution of the perturbations (gravitational instability)

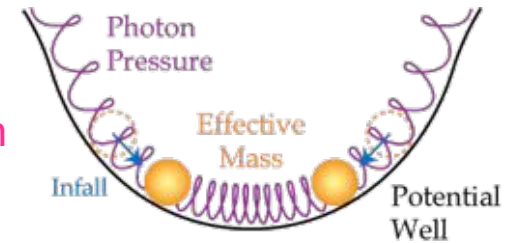
$$\ddot{\delta}_k + 2\frac{\dot{a}}{a}\dot{\delta}_k + \left(\underbrace{\frac{c_s^2 k^2}{a^2}}_{\text{pressure repulsion}} - \underbrace{4\pi G \bar{\rho}}_{\text{gravitational attraction}} \right) \delta_k = 0$$

pressure repulsion

gravitational attraction

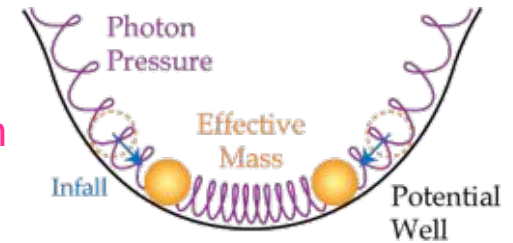


action of
two effects



Structures formation: evolution of the perturbations (gravitational instability)

$$\ddot{\delta}_k + 2\frac{\dot{a}}{a}\dot{\delta}_k + \left(\underbrace{\frac{c_s^2 k^2}{a^2}}_{\text{pressure repulsion}} - \underbrace{4\pi G \bar{\rho}}_{\text{gravitational attraction}} \right) \delta_k = 0$$



MD: After matter-radiation decoupling, $z < 1100$, this eq. converts into

$$\ddot{\delta}_k + 2\frac{\dot{a}}{a}\dot{\delta}_k - 4\pi G \bar{\rho} \delta_k = 0$$

it has two solutions: δ^+ , δ^- , the second one decreases!

$$\delta^+(t) = \delta_0 t^{2/3} \propto a(t)$$

this solution form gravitational potential wells that are the seeds to form structures (by gravitational instability)!

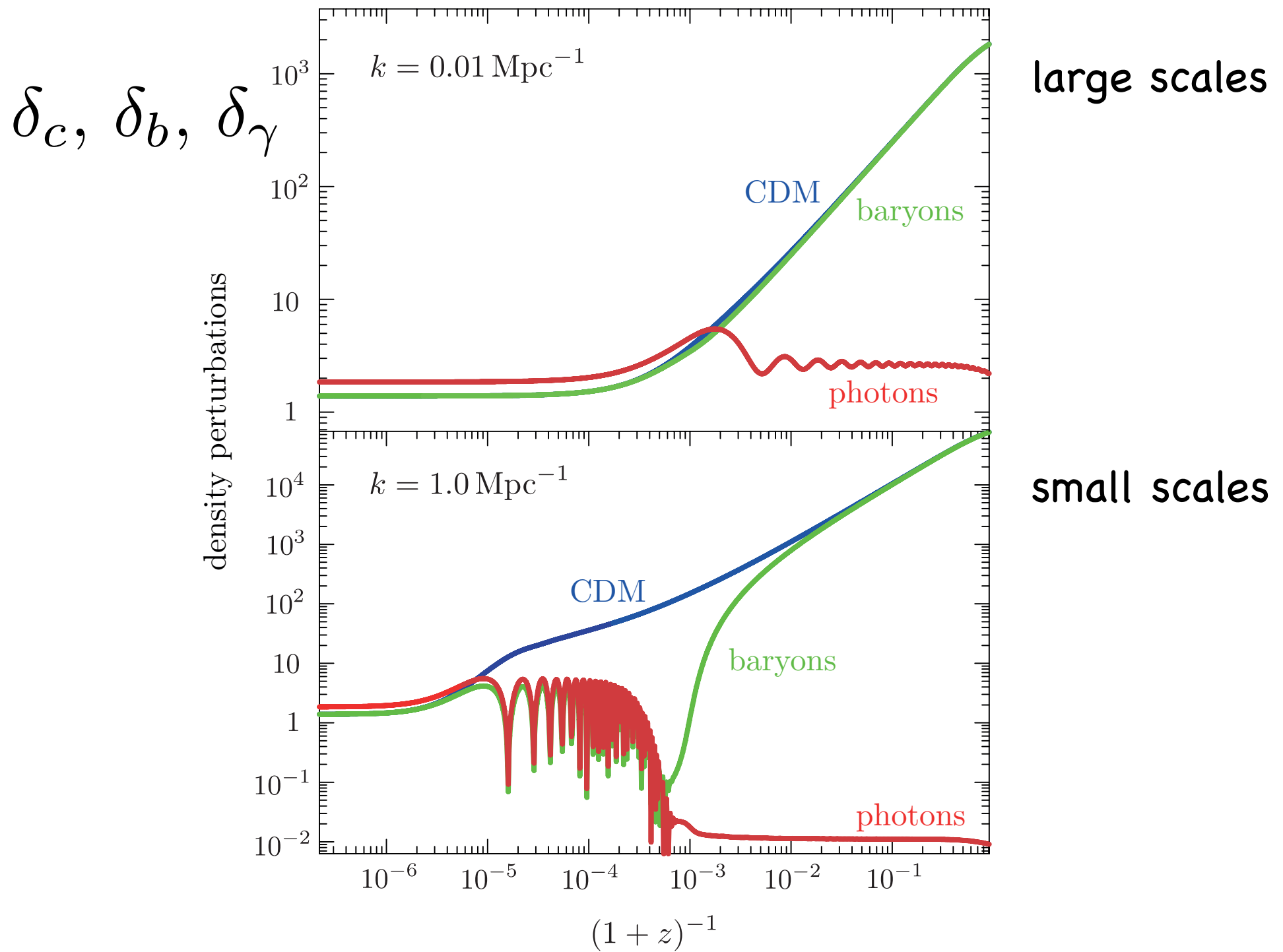
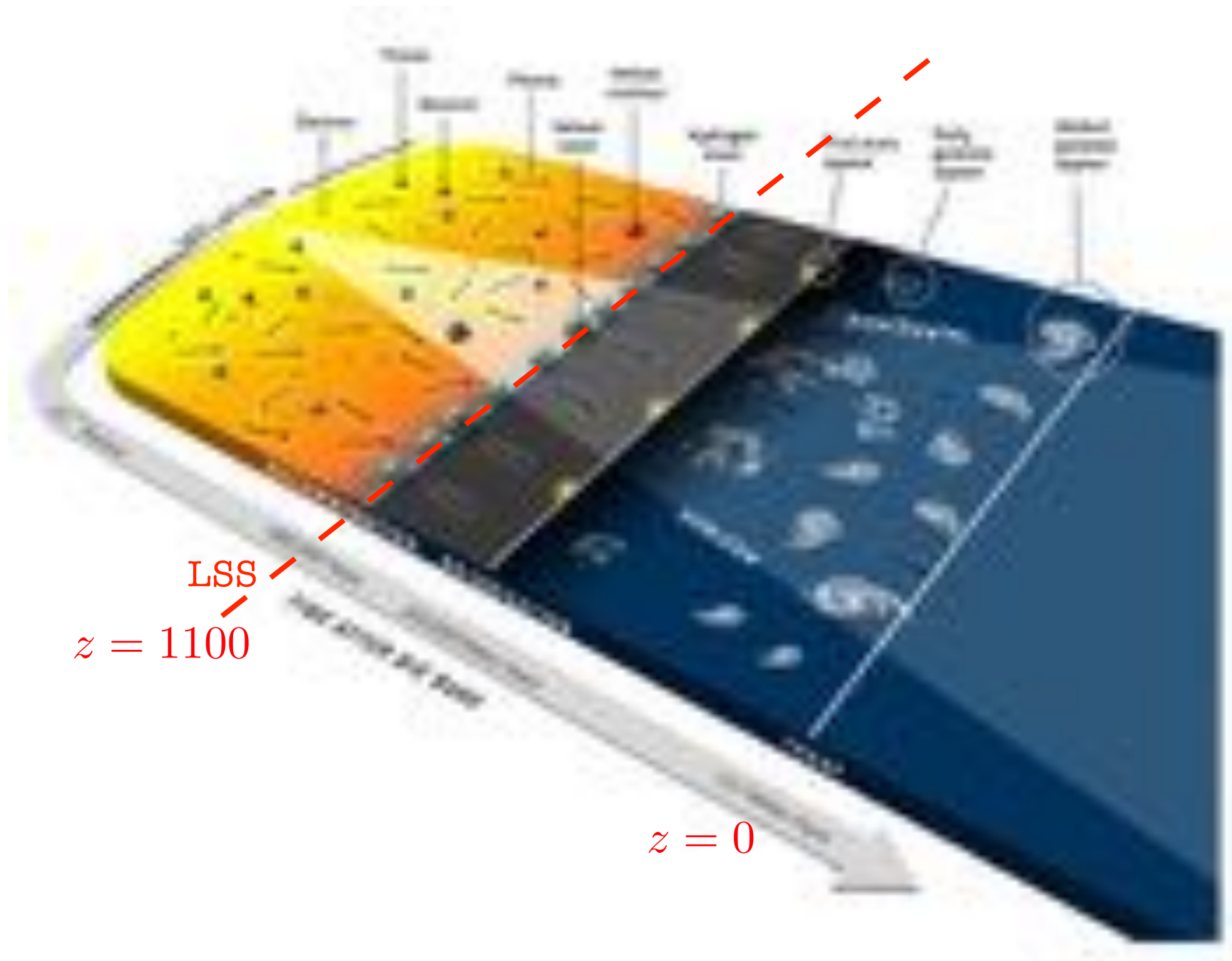


Figure 5.5: *Evolution of photons, baryons and dark matter.*



LSS

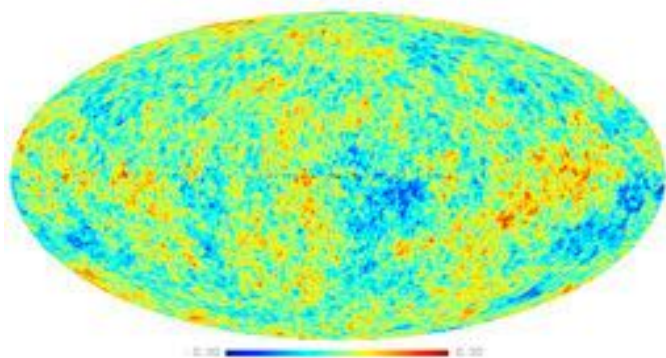
$$z = 1100$$

$$z = 0$$

density contrast:

$$\delta_{LSS} = ? \quad \begin{array}{l} \nearrow \delta_{b/LSS} = ? \\ \searrow \delta_{cdm/LSS} = ? \end{array}$$

$$\delta_{cdm/LSS} \sim a(z) = \frac{1}{1+z}$$



$$\delta_{b/LSS} \equiv \frac{\delta\rho_b}{\bar{\rho}_b} \sim \frac{\Delta T}{T_0} \sim 10^{-5}$$

$z = 1100$

$$a(z = 1100) \simeq 10^{-3}$$

$$\delta_{b/LSS} \simeq 10^{-5}$$

$$\delta_{cdm/LSS} \simeq 10^{-2} - 10^{-3}$$

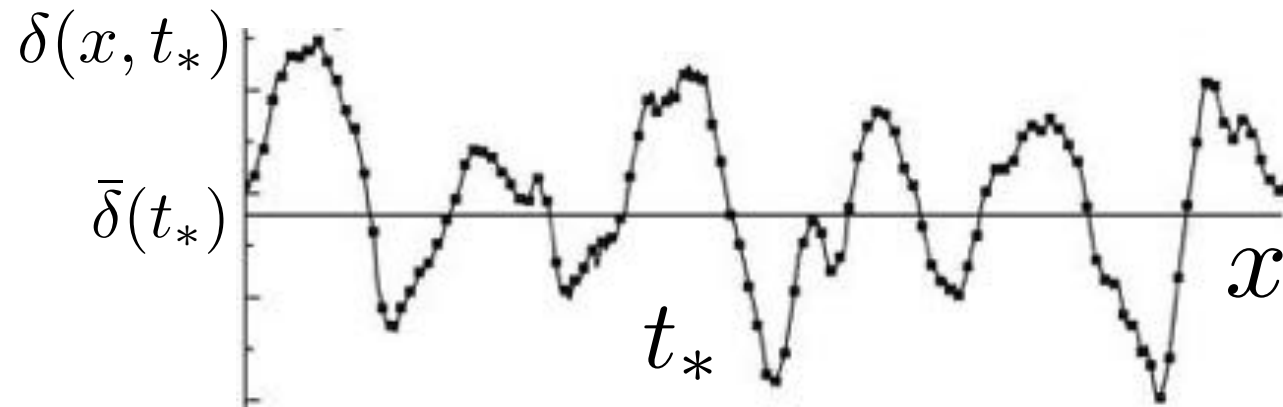
$z = 0$

$$a(z = 0) = 1$$

$$\delta_{b+cdm/today} \simeq 1$$

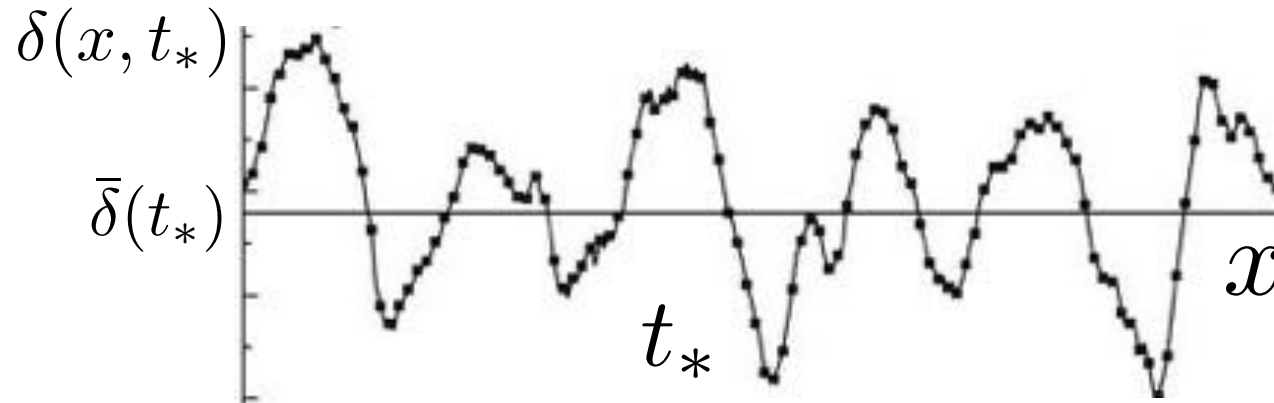


density contrast $\delta(x, t_*) \equiv \frac{\rho(x, t_*) - \bar{\rho}(t_*)}{\bar{\rho}(t_*)}$



$$\delta(x, t_0) = \sum_i c_i \lambda_i(x, t_0)$$

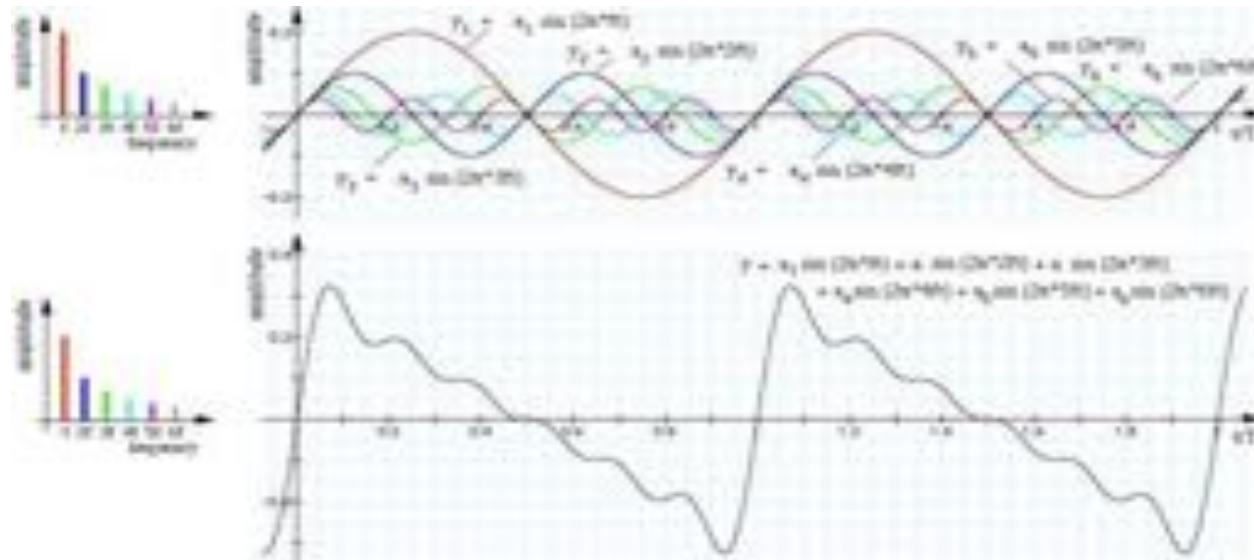
density contrast $\delta(x, t_*) \equiv \frac{\rho(x, t_*) - \bar{\rho}(t_*)}{\bar{\rho}(t_*)}$



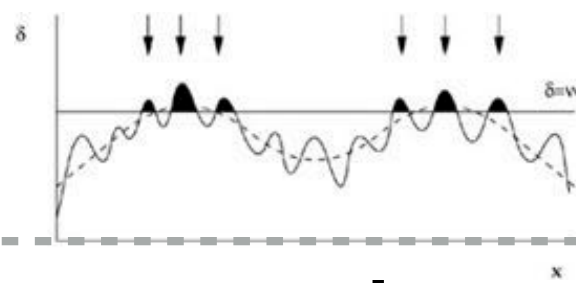
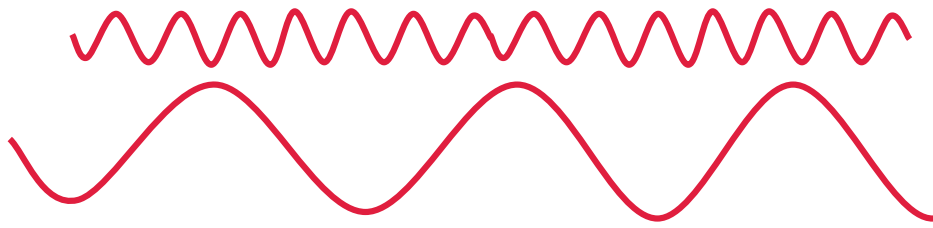
$$\delta(x, t_0) = \sum_i c_i \lambda_i(x, t_0)$$

Harmonic analyses in 1-d

A vibrating string with fixed boundaries: it can vibrate in **fundamental harmonics (FH)**: 1st harm., 2nd harm., etc. Then, an arbitrary **perturbation** of the string can be represented as a superposition of the **FH**:

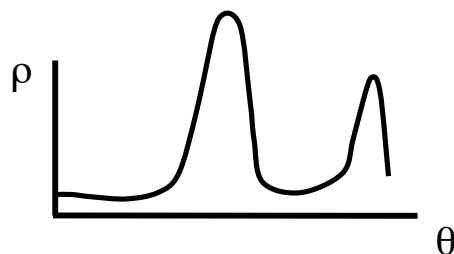
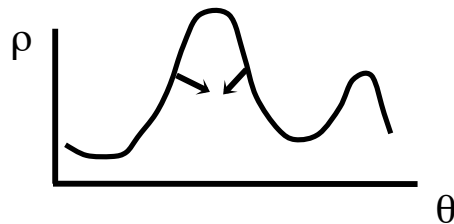
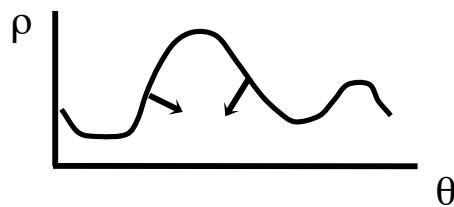


the amplitude for each frequency = **spectrum of the perturbation**

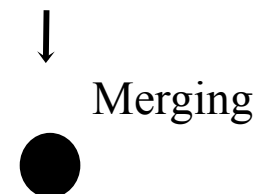
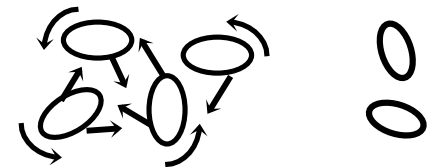
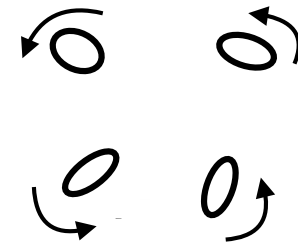
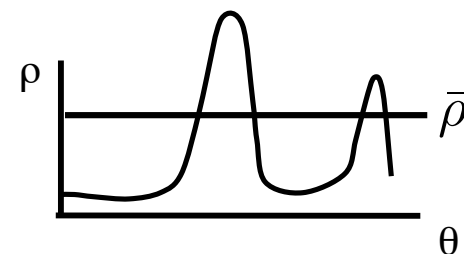
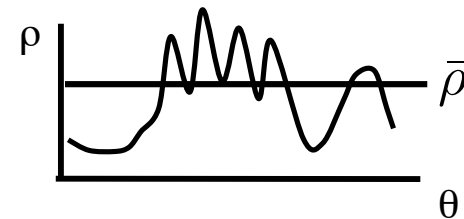
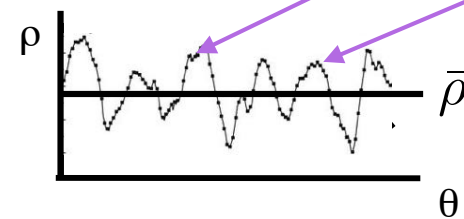


Two collapse scenarios:

Initial collapse
(top down)



Hierarchical merging
(bottom up)

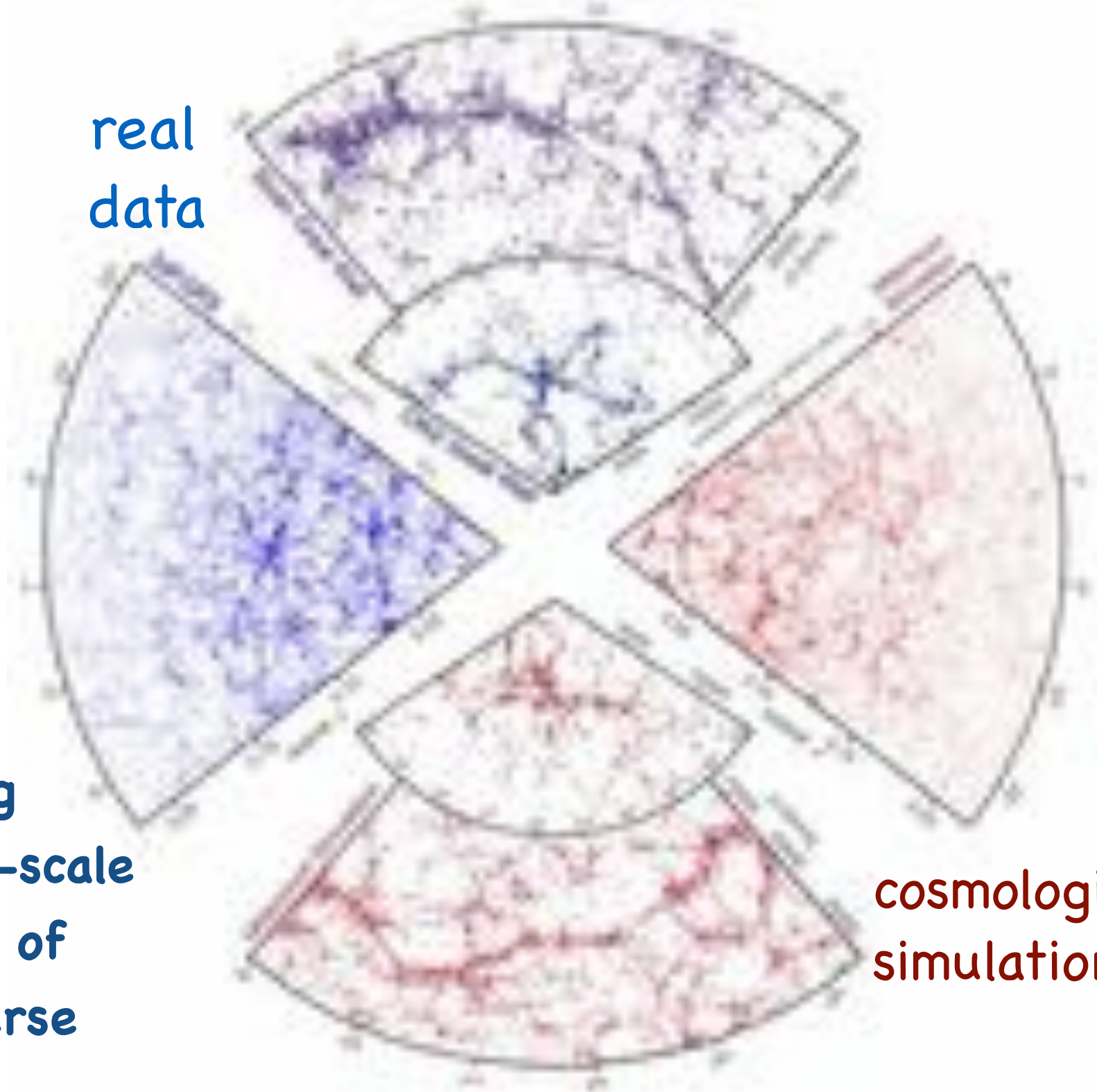


The Future:
cosmological
simulations

real
data

Simulating
the large-scale
structure of
the Universe

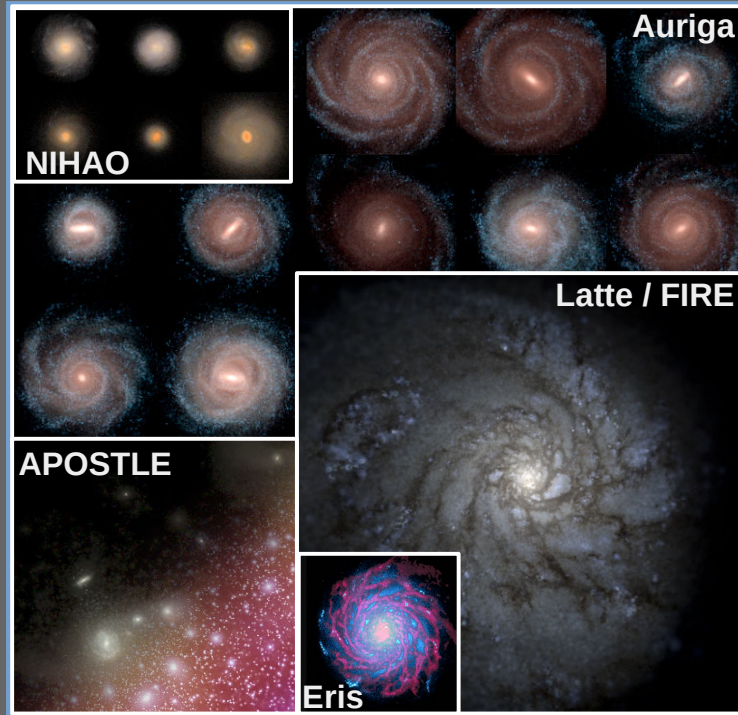
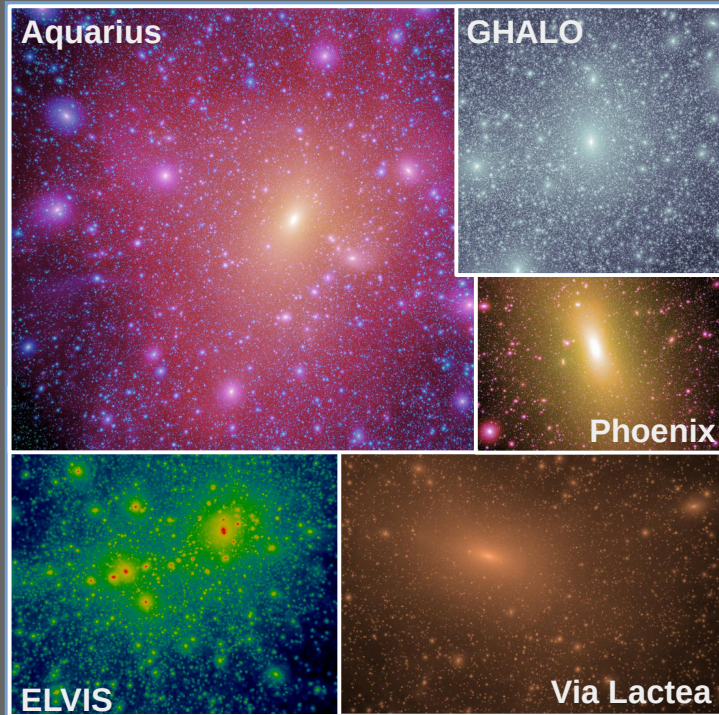
cosmological
simulation



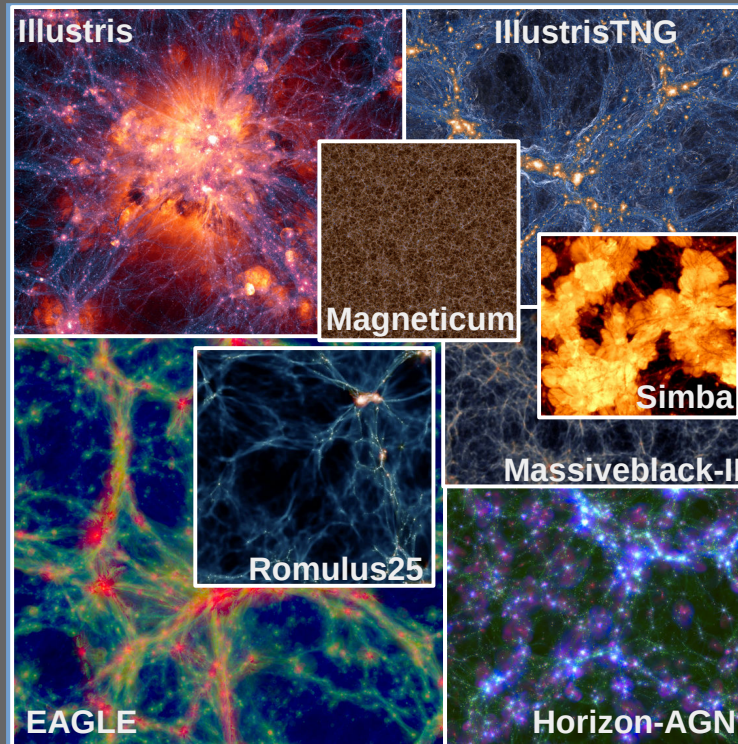
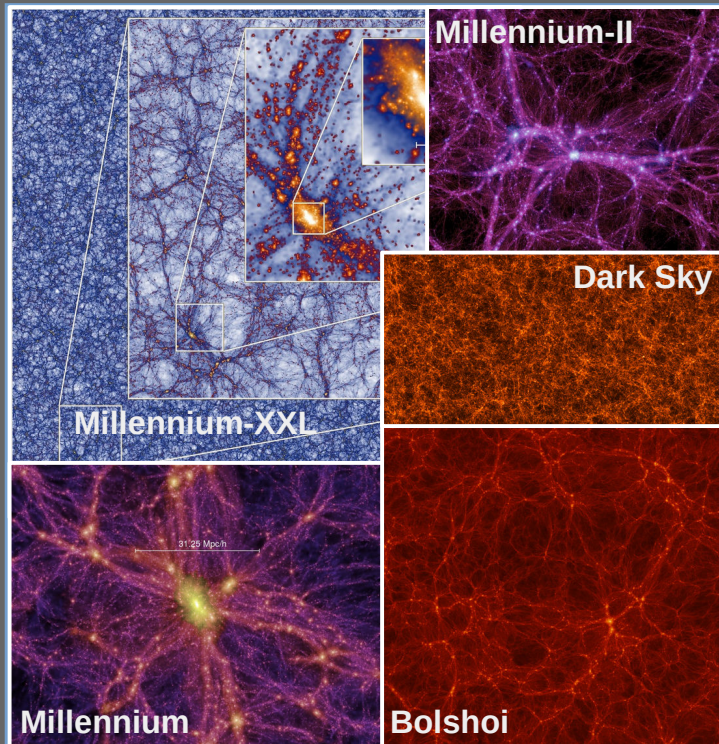
dark matter-only (N -body)

dark matter + baryons (hydrodynamical)

zoom (details)



large volume (statistics)

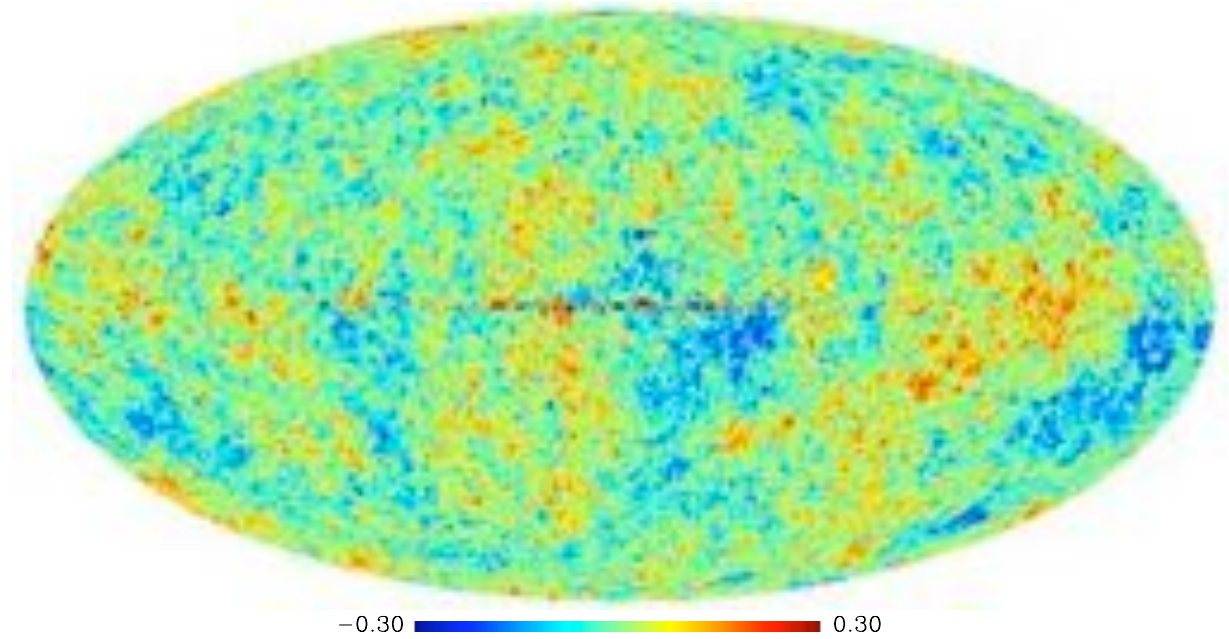
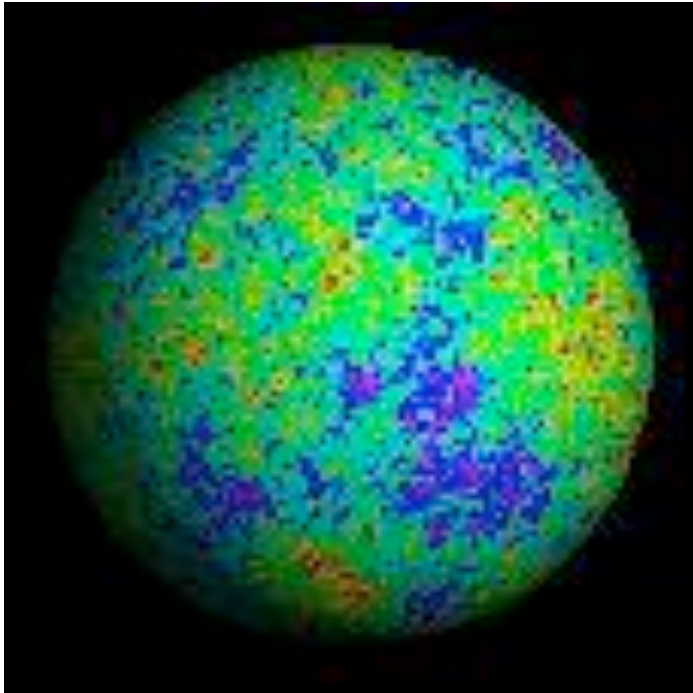


Modern Observational Probes:

- ▶ **CMB temperature fluctuations:**
what is the shape of the Universe?

Do we live in an isotropic Universe?

CMB sphere?



Esfera S^2

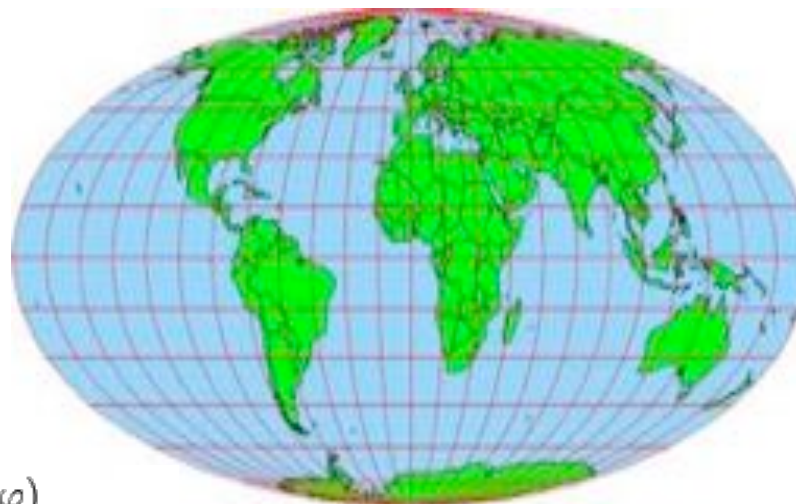
Projeção Mollweide sobre um plano



$$x = \frac{2\sqrt{2}}{\pi} \lambda \cos(\theta),$$

$$y = \sqrt{2} \sin(\theta),$$

$$2\theta + \sin(2\theta) = \pi \sin(\varphi)$$

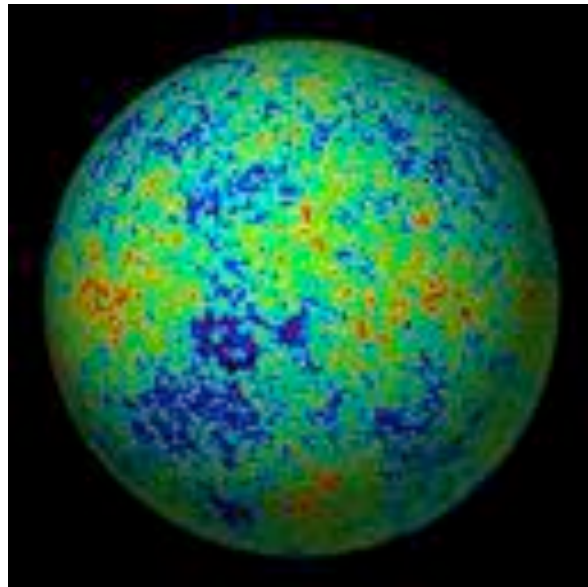


K. Mollweide (1774-1825)
Matemático

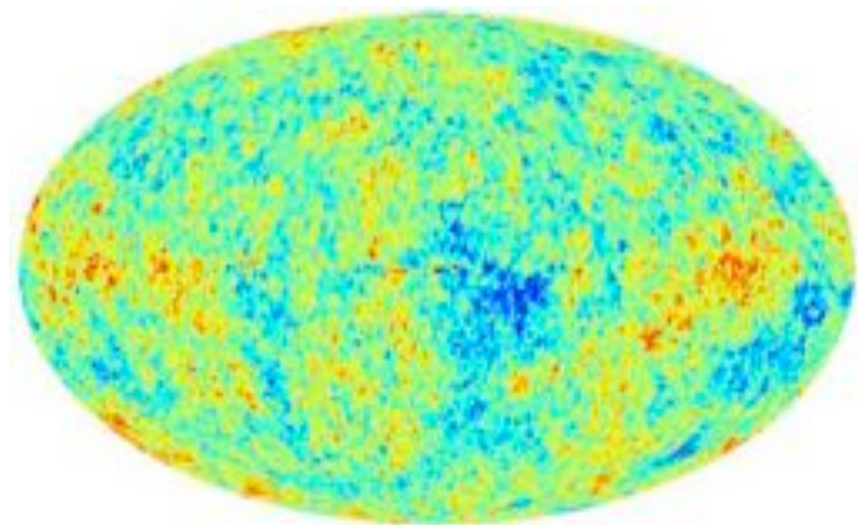
Esfera S^2



Projeção Mollweide sobre um plano



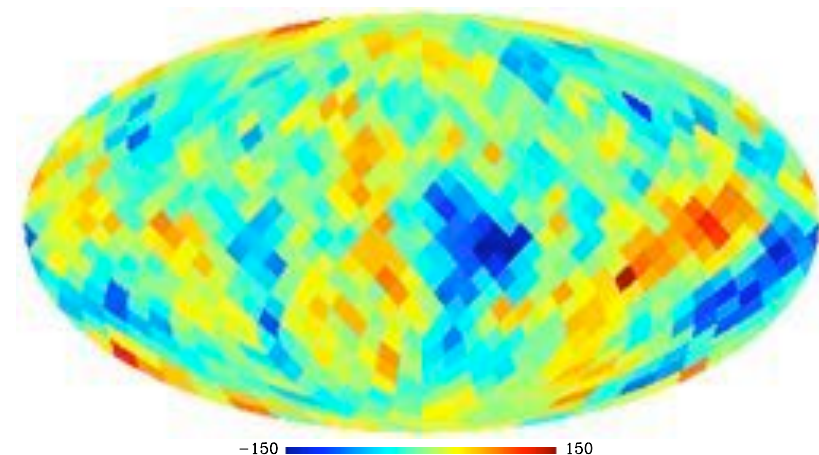
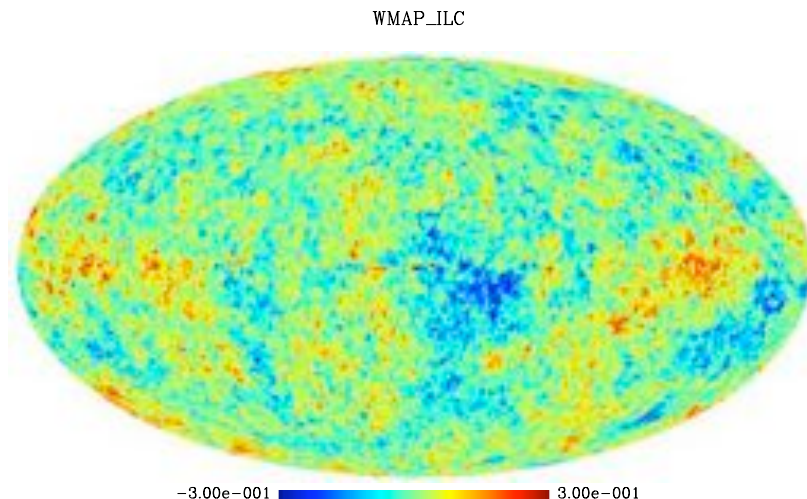
WMAP_ILC



-3.00e-001 3.00e-001

Mapas da Radiação C3smica de Fundo

- ▶ a esfera celeste 3 dividida em N pixels da mesma 3rea
- ▶ as flut. de temp. da RCF ΔT representam-se usando uma escala linear de cores: azul (= m3n.), verde ($\simeq 0$), e vermelho (=m3x.). Representamos: $\frac{\Delta T(\theta, \phi)}{T_{Planck}} = \sum_{\ell, m} a_{\ell m} Y_{\ell m}(\theta, \phi)$.
- ▶ os pixels s3o t3o pequenos que os mapas parecem um cont3nuo de manchas coloridas, mas ... basta degradar o mapa para observar eles:

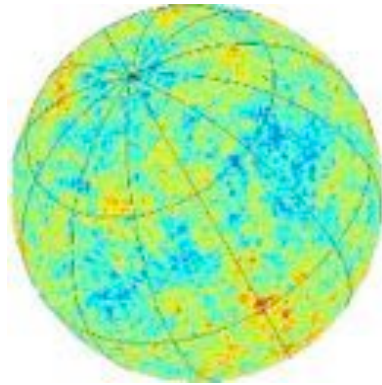


- ▶ a esfera celeste é dividida em N pixels, todos de igual área, seguindo o esquema de pixelização (HEALPIX)



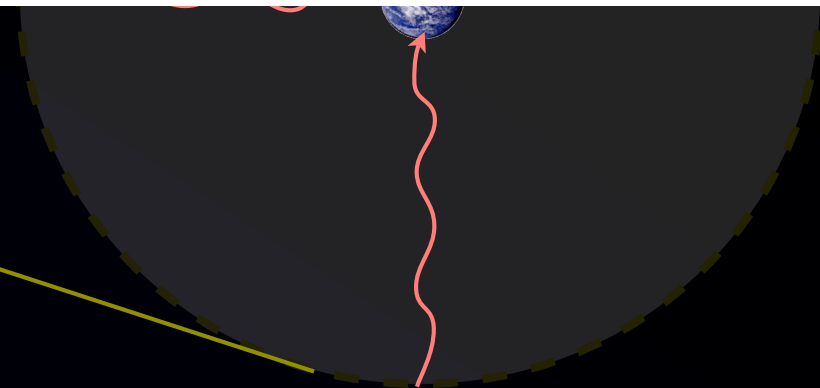
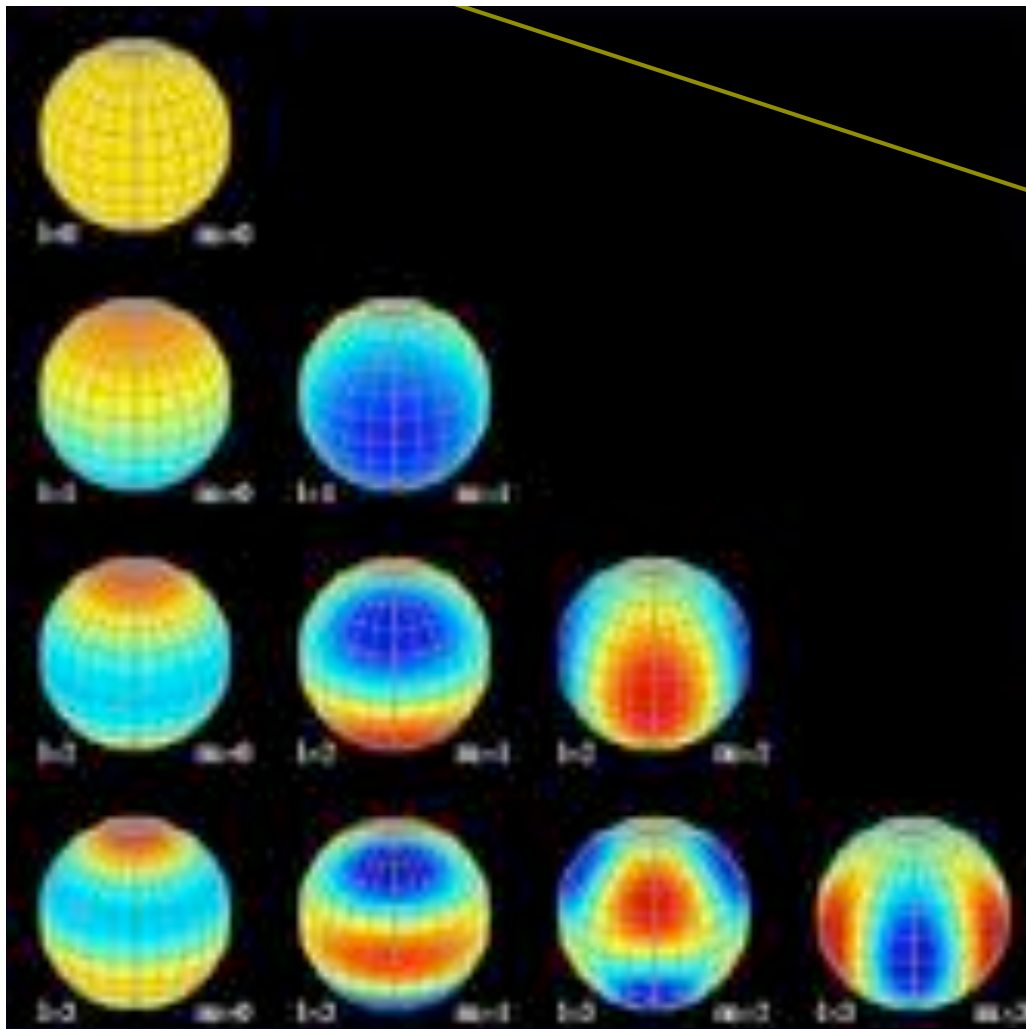
Harmonic analyses in 2-d

Analogously, on the spherical surface S^2 any function $\Delta T = \Delta T(\theta, \varphi)$ can be represented as a combination of the spherical harmonics $Y_{\ell m}$



$$= \frac{\Delta T(\theta, \phi)}{T_o} = \sum_{\ell, m} a_{\ell m} Y_{\ell m}(\theta, \phi)$$

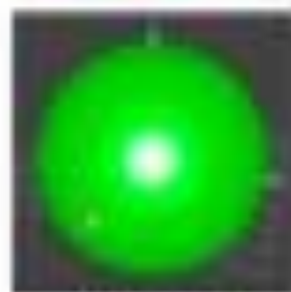
where the coefficients $a_{\ell m}$ have the complete information about the spectrum perturbation ΔT , where the variable ℓ (also called multipole order) is associated to the angular scale θ ($\sim \pi/\ell$) and the variable m is associated to the angular scale φ .



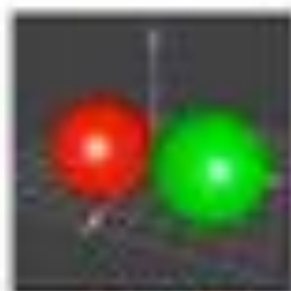
$$\delta T(\theta, \varphi) = \sum_{\ell, m} a_{\ell m} Y_{\ell}^m(\theta, \varphi)$$

$$C_{\ell} = \frac{1}{2\ell + 1} \sum_{m=-\ell}^{\ell} |a_{\ell m}|^2$$

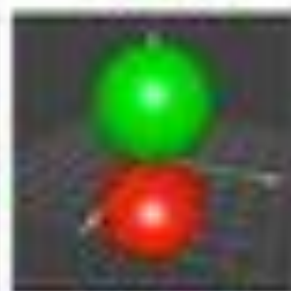
$Y_{\ell m}$



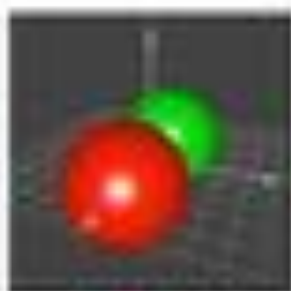
L0 M0



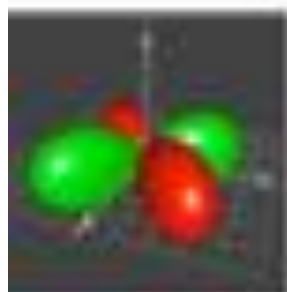
L1 M-1



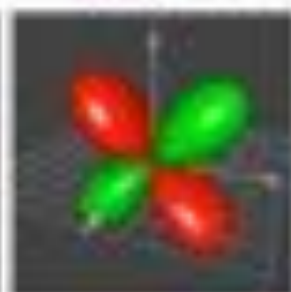
L1 M0



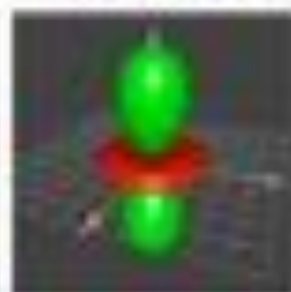
L1 M1



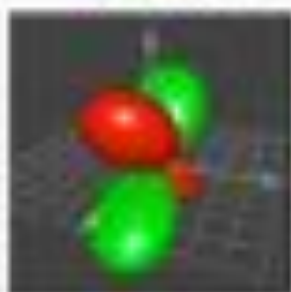
L2 M-2



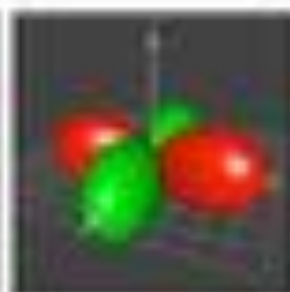
L2 M-1



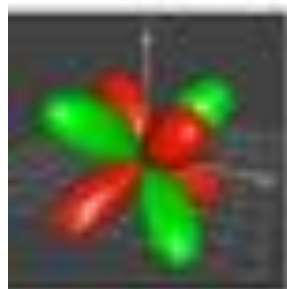
L2 M0



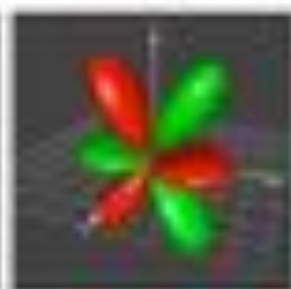
L2 M1



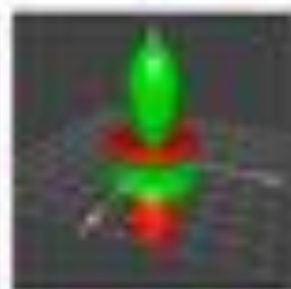
L2 M2



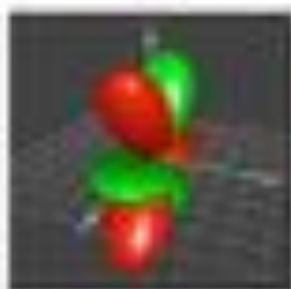
L3 M-2



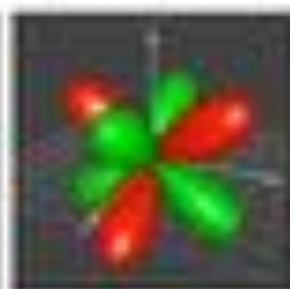
L3 M-1



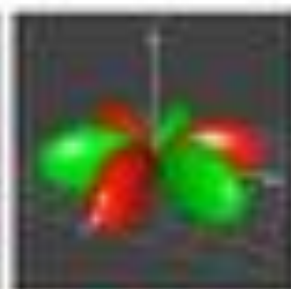
L3 M0



L3 M1



L3 M2

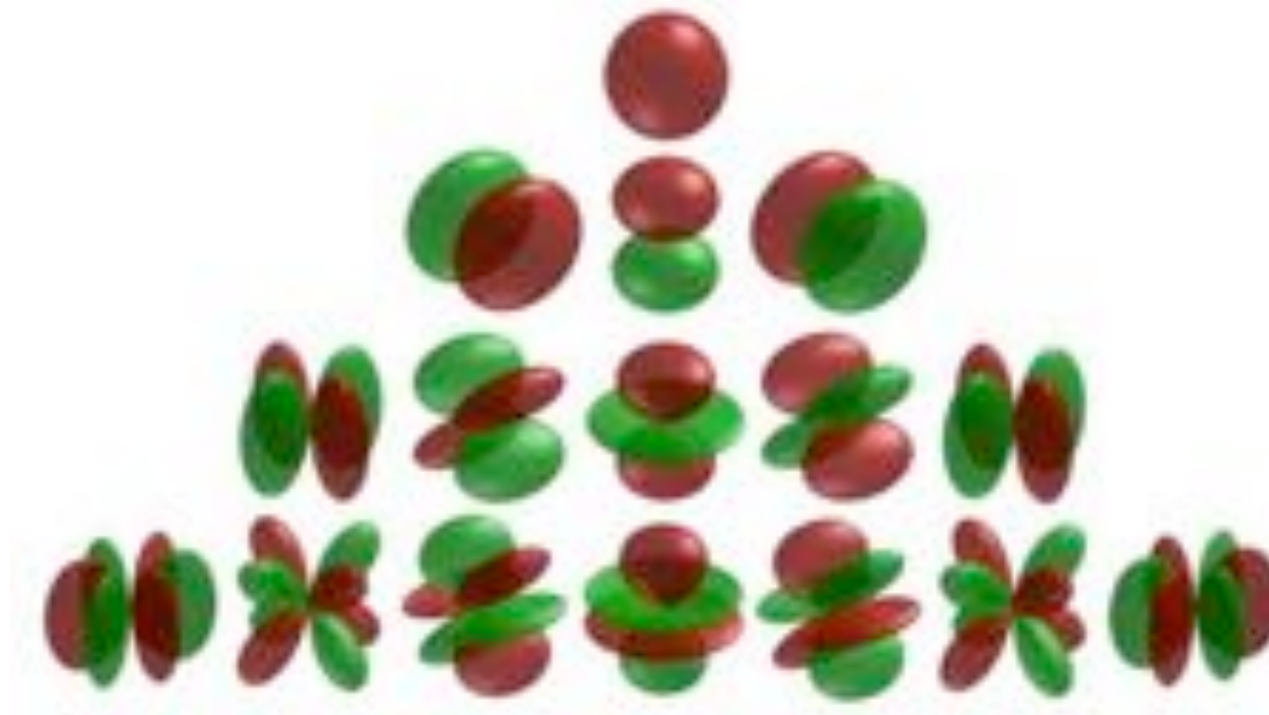


L3 M3

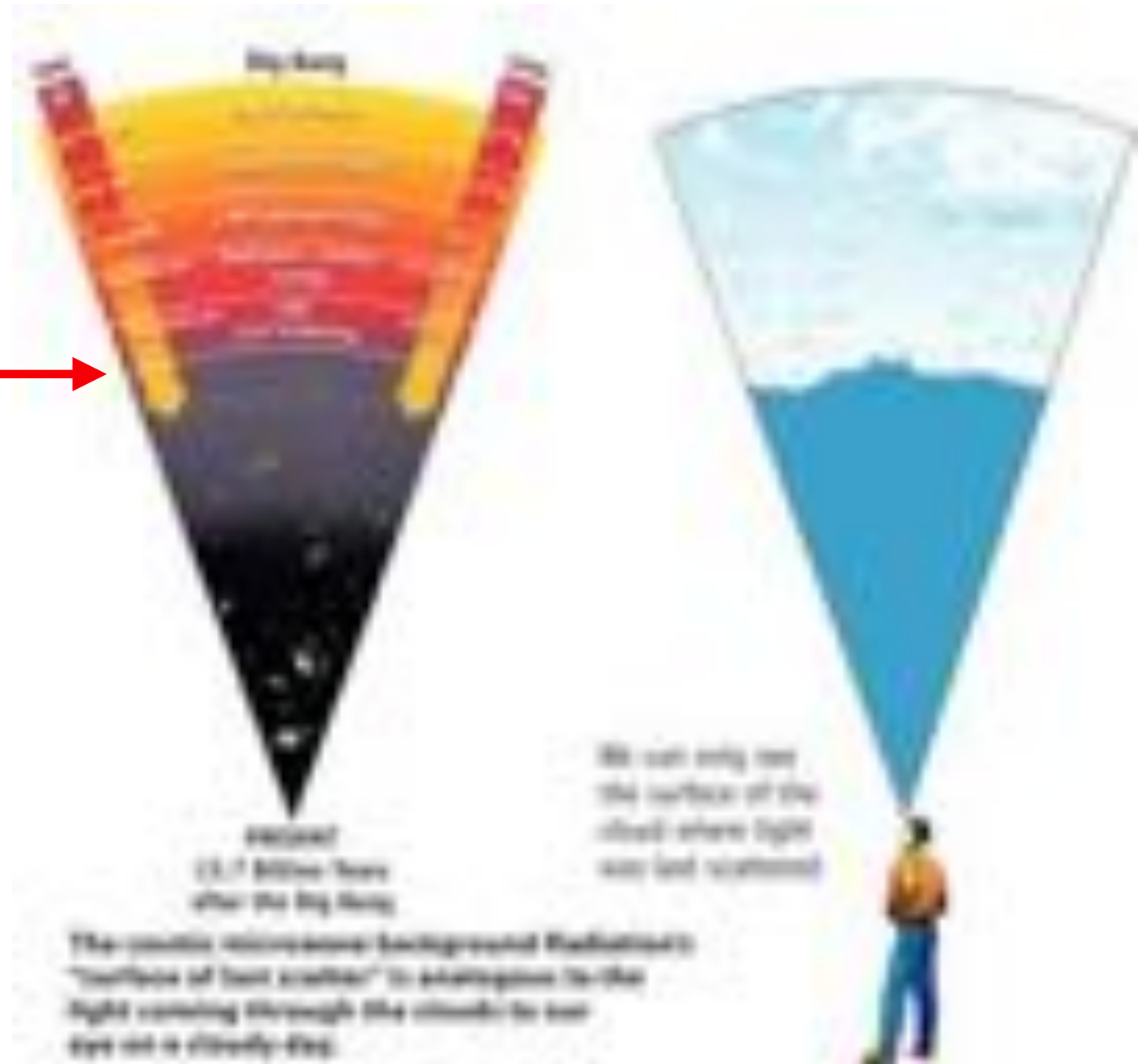
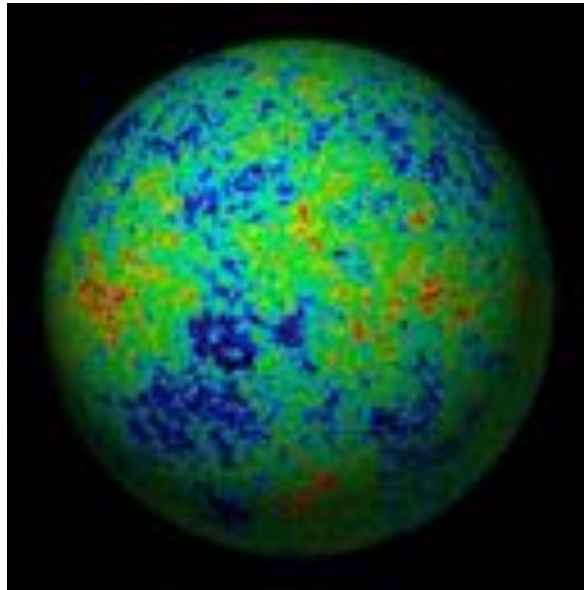
P.-S. Laplace

$$\nabla^2 V = \frac{\partial^2 V}{\partial x^2} + \frac{\partial^2 V}{\partial y^2} + \frac{\partial^2 V}{\partial z^2} = 0.$$

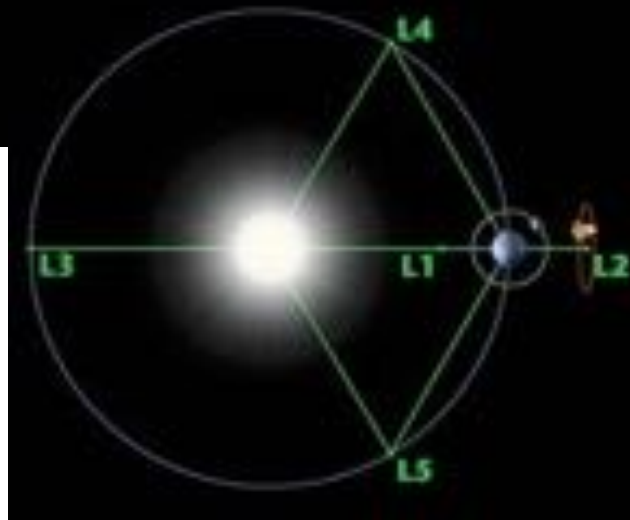
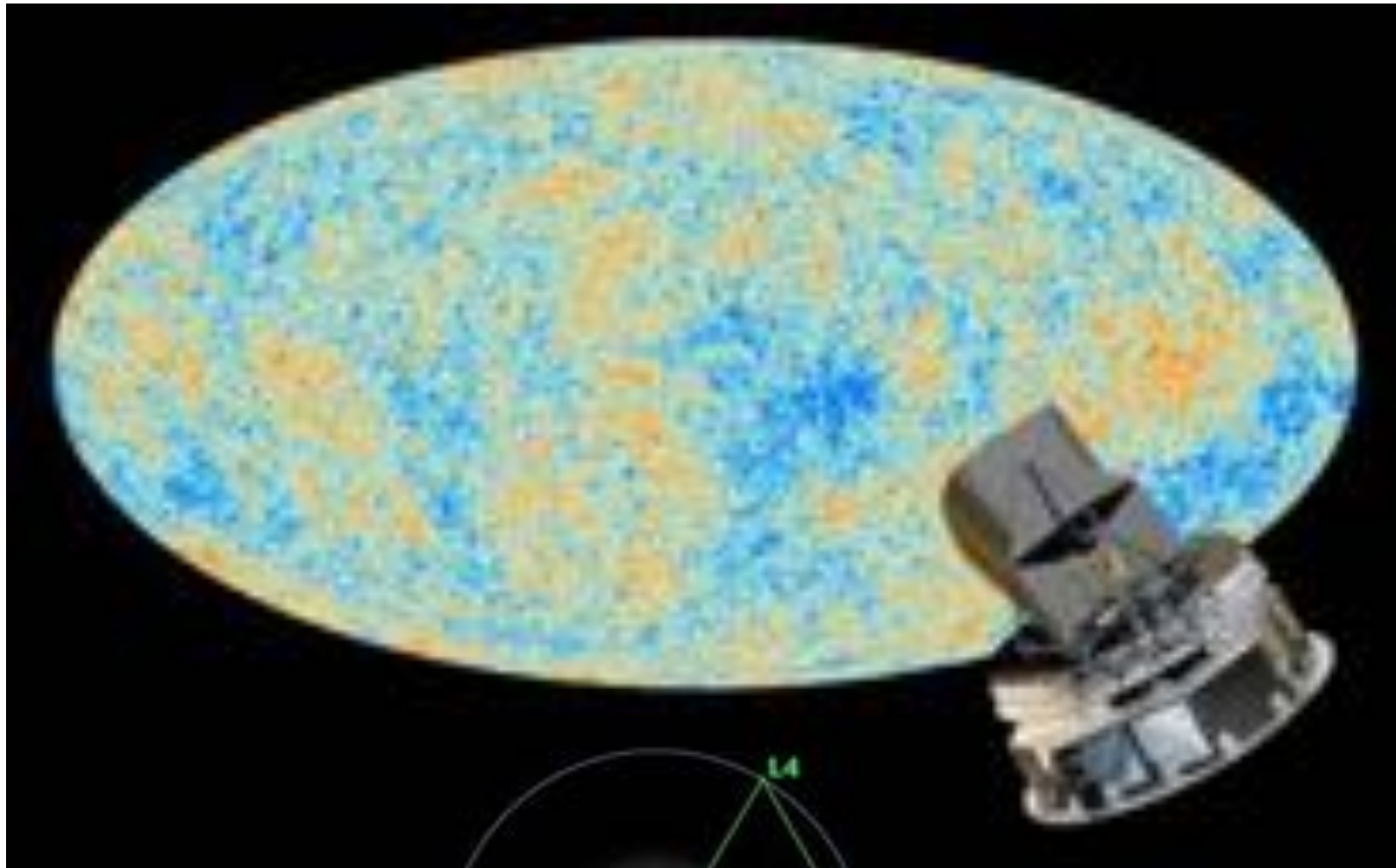
$$\nabla^2 f = \frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\partial f}{\partial r} \right) + \frac{1}{r^2 \sin \theta} \frac{\partial}{\partial \theta} \left(\sin \theta \frac{\partial f}{\partial \theta} \right) + \frac{1}{r^2 \sin^2 \theta} \frac{\partial^2 f}{\partial \varphi^2} = 0.$$



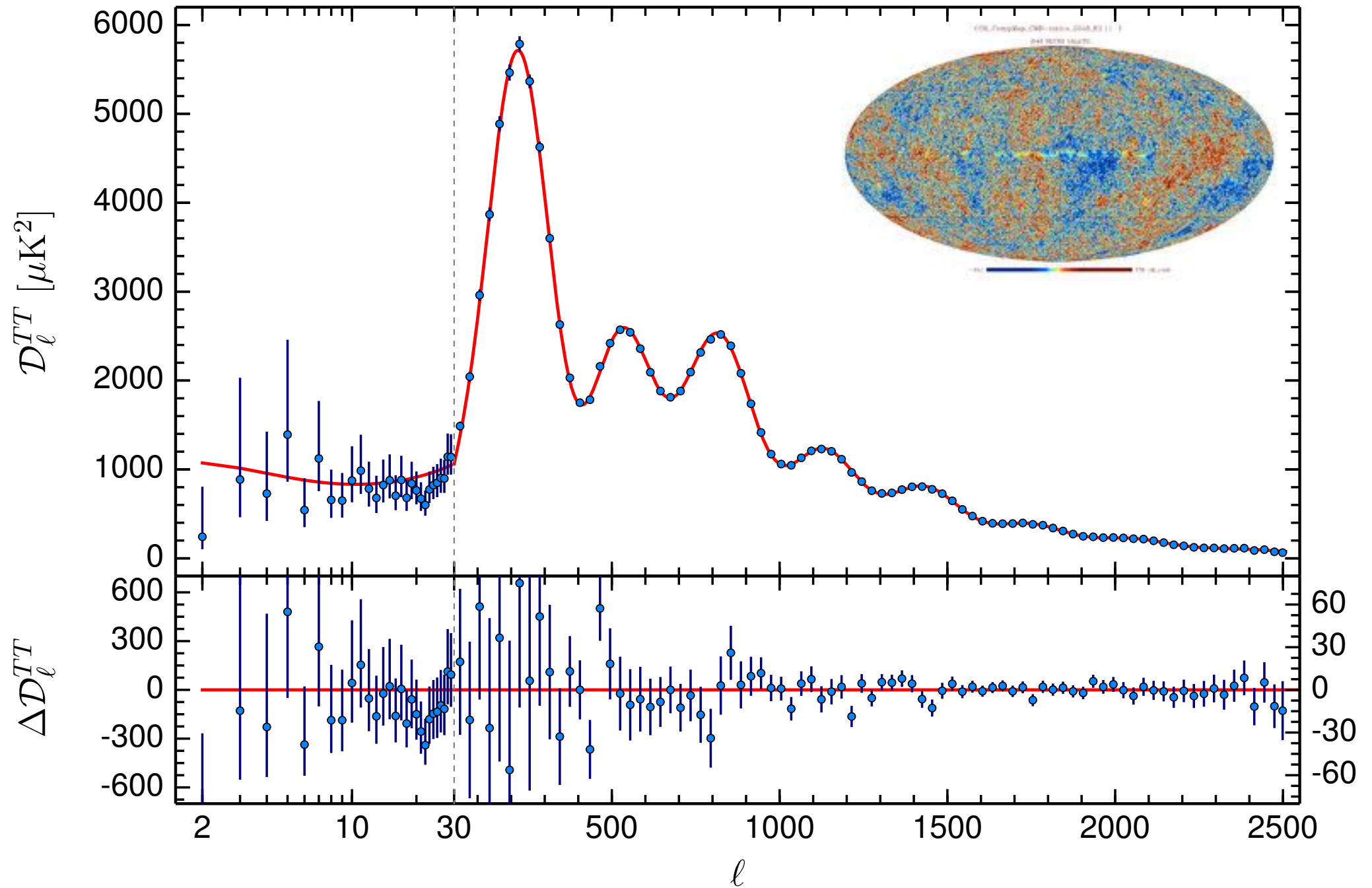
$$Y_{\ell}^m(\theta, \varphi) = N e^{im\varphi} P_{\ell}^m(\cos \theta)$$



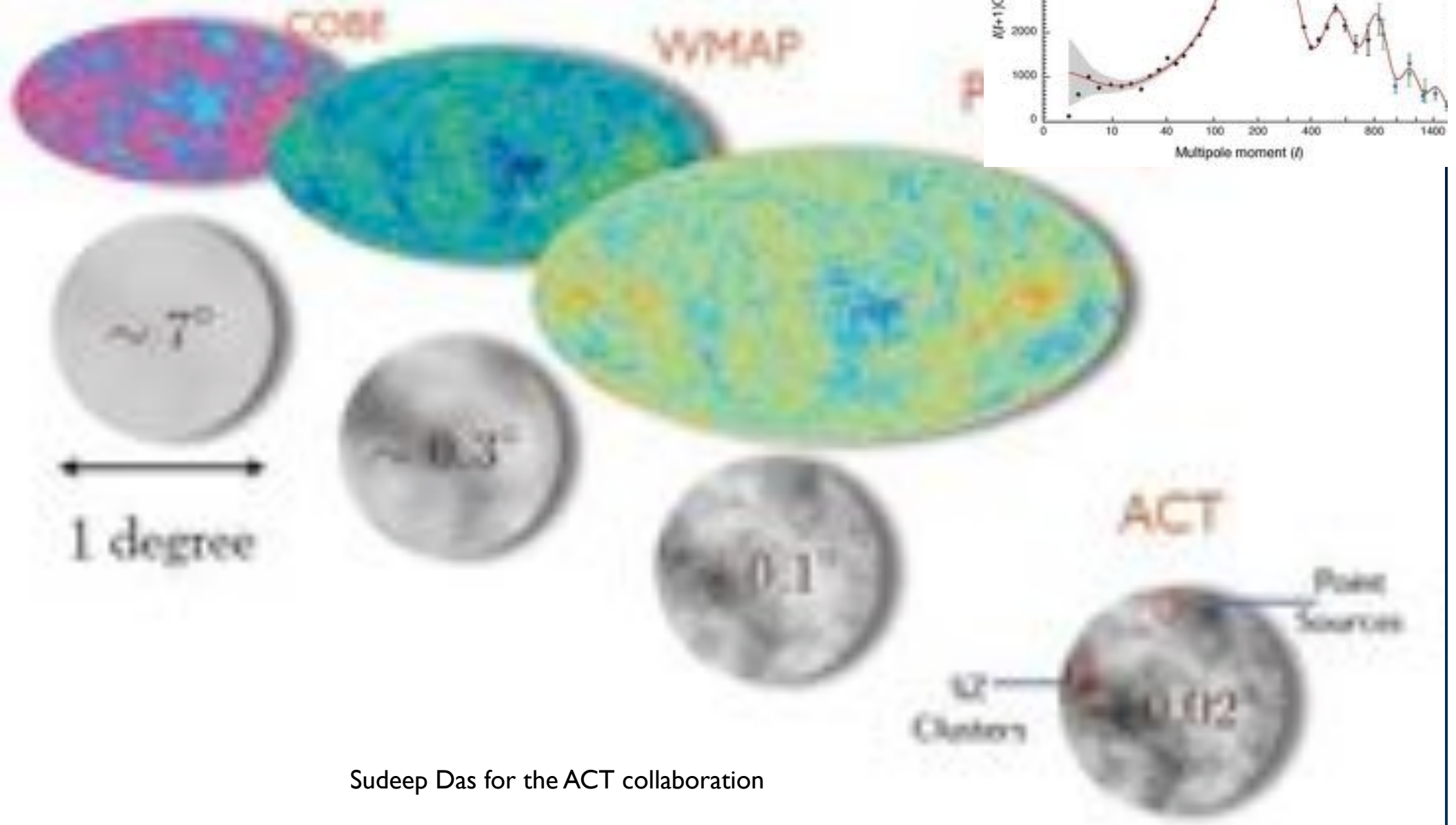
2018 Planck CMB data



CMB temperature fluctuations: Angular Power Spectrum



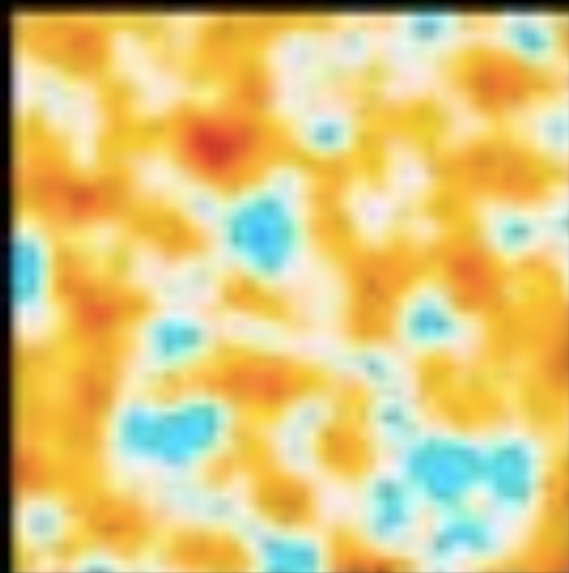
Going to small scales



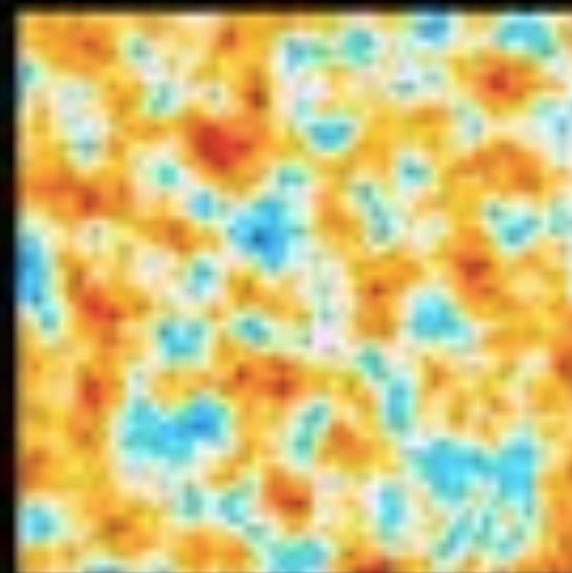
Sudeep Das for the ACT collaboration



COBE



WMAP

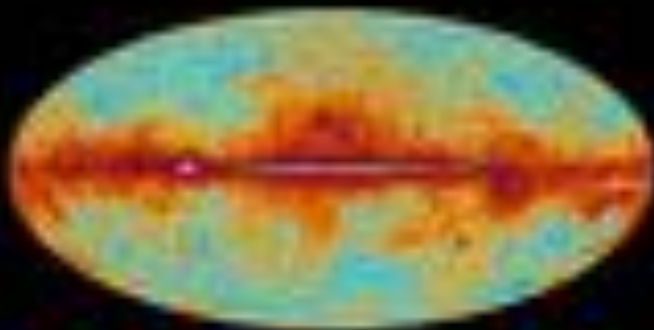


Planck

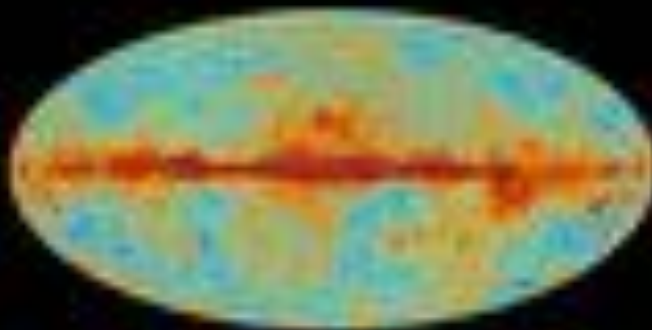


planck

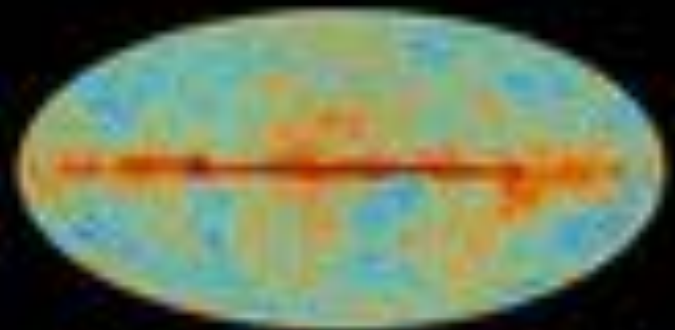
The sky as seen by Planck



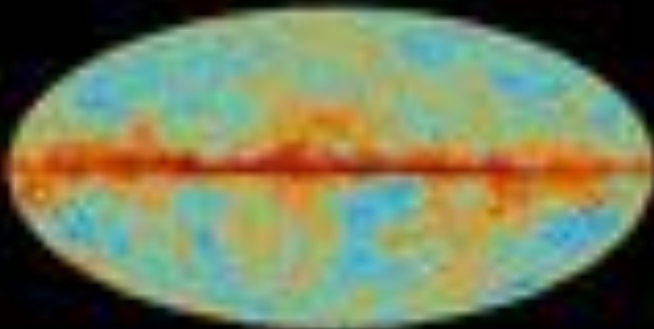
70 GHz



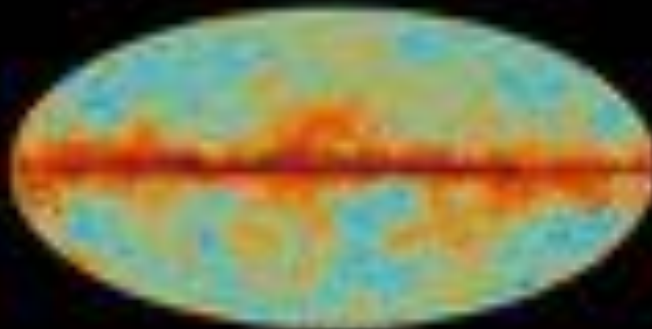
86 GHz



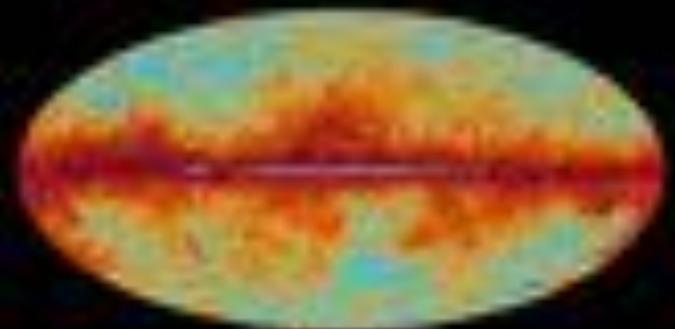
100 GHz



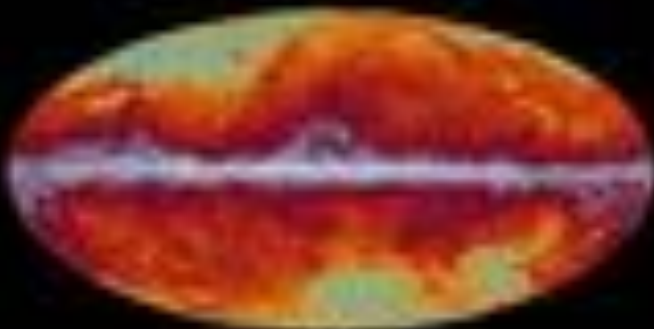
143 GHz



160 GHz



217 GHz



353 GHz



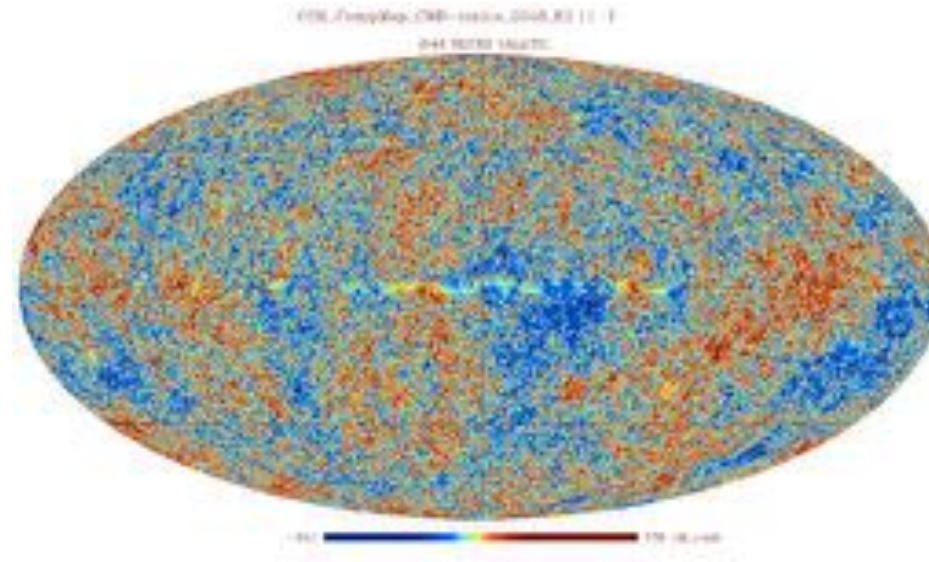
440 GHz



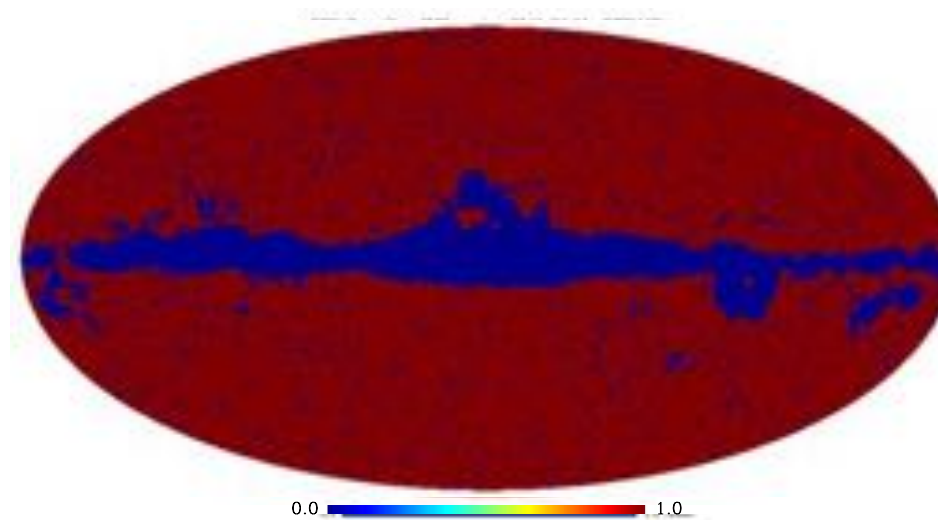
857 GHz

2018 Planck CMB data

SMICA



M82



Is the CMB field isotropic?

- Null hypothesis: “the observed universe is isotropic”. Does current observational data show evidence against this hypothesis?

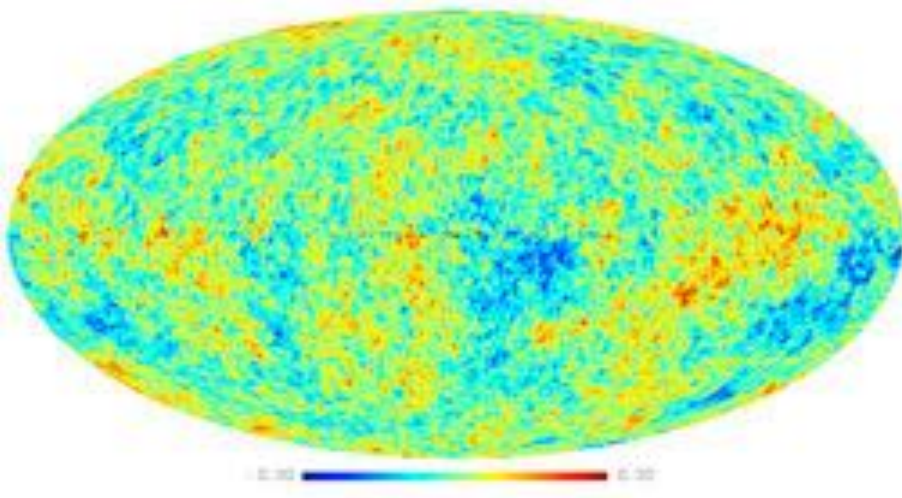
Em um universo estatisticamente isotrópico

$$\langle a_{\ell m} a_{\ell' m'}^* \rangle = C_{\ell} \delta_{m m'} \delta_{\ell \ell'} \longrightarrow C_{\ell} \equiv \frac{1}{2\ell + 1} \sum_m |a_{\ell m}|^2$$

Em um universo estatisticamente anisotrópico

$$\langle a_{\ell m} a_{\ell' m'}^* \rangle = C_{\ell m}^{\ell' m'} \quad \text{X} \quad C_{\ell} \equiv \frac{1}{2\ell + 1} \sum_m |a_{\ell m}|^2$$

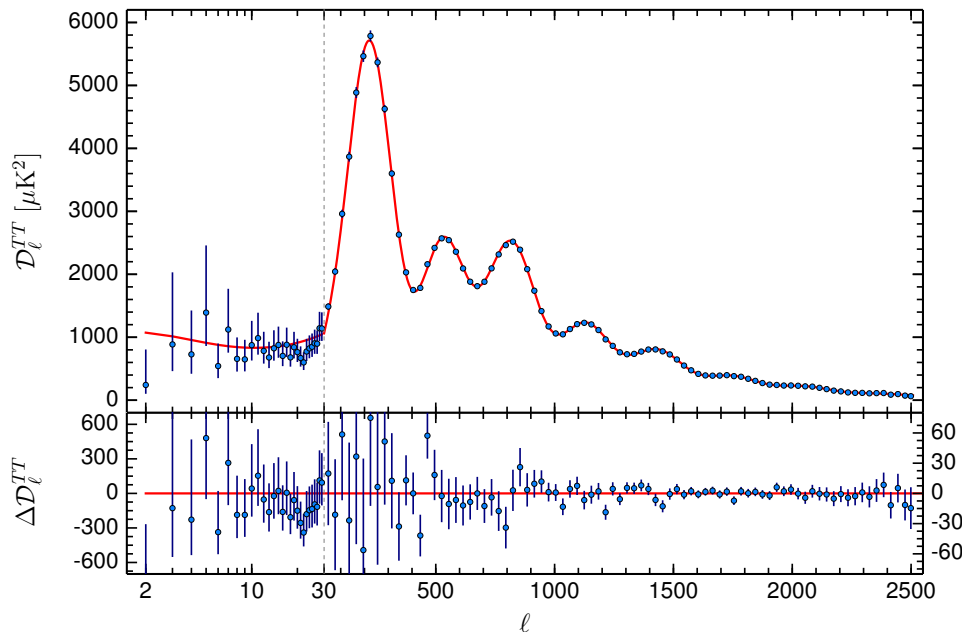
Como analisar dados sem assumir IE?



Is the CMB field isotropic?

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Em um universo estatisticamente isotrópico



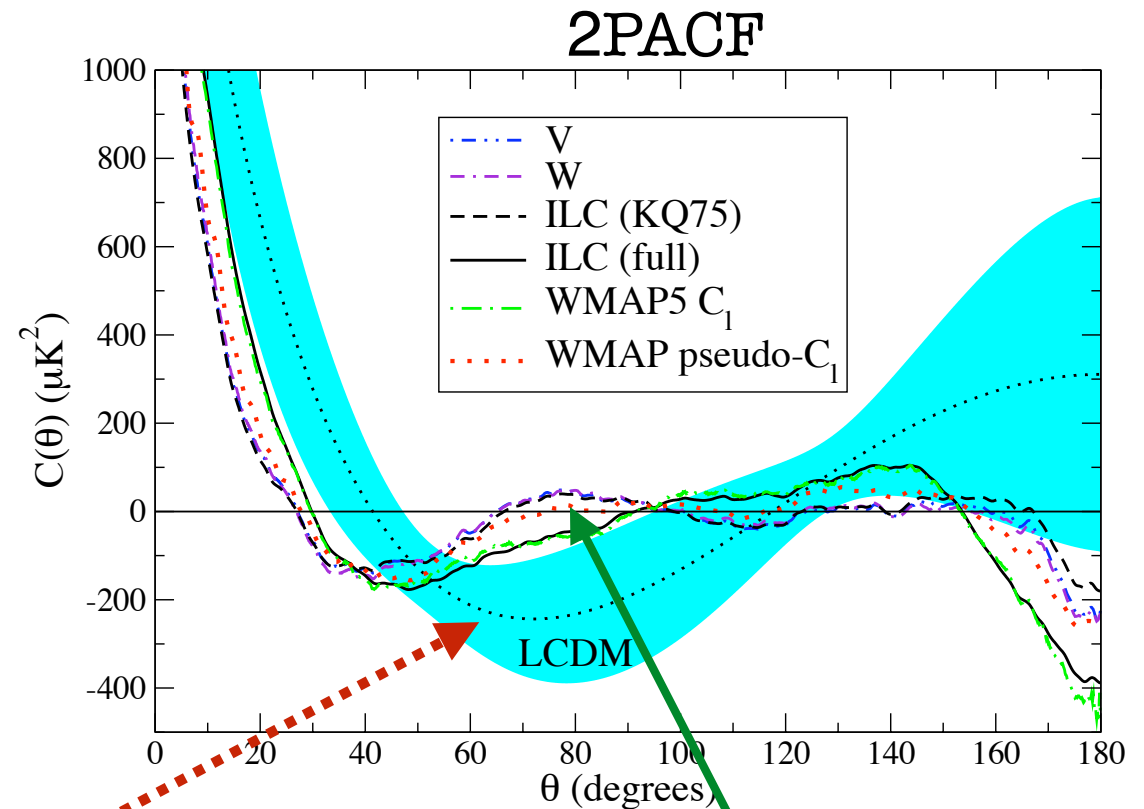
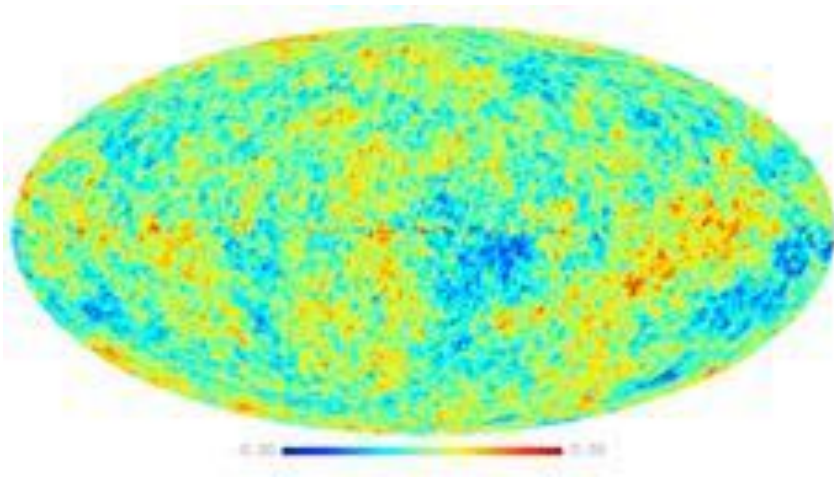
$$\langle a_{\ell m} a_{\ell' m'}^* \rangle = C_{\ell} \delta_{mm'} \delta_{\ell\ell'} \longrightarrow C_{\ell} \equiv \frac{1}{2\ell + 1} \sum_m |a_{\ell m}|^2$$

Em um universo estatisticamente anisotrópico

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Como analisar dados sem assumir IE?

Is the CMB field isotropic?



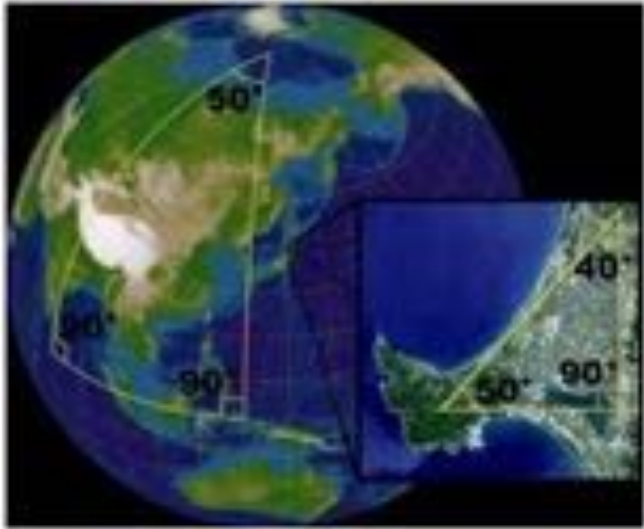
$$C_{exp}(\theta) = \sum_{\ell} \frac{2\ell + 1}{4\pi} C_{\ell} P_{\ell}(\cos \theta)$$

esta expressão assume
isotropia estatística

$$C_{obs}(\theta) \equiv \left\langle \frac{\Delta T}{T_0}(\varphi) \frac{\Delta T}{T_0}(\varphi + \theta) \right\rangle$$

esta expressão não assume
isotropia estatística

The form of the Universe



the geometry of the Universe?

local properties: angles,
distances, areas, parallelism,...



the topology of the Universe?

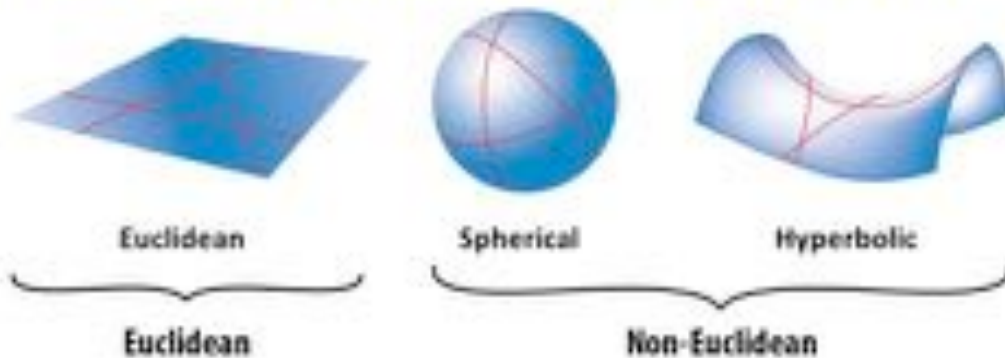
global properties:
without boundary, size, isometries,
simple vs. multi-connectedness,...

UNI-VERSO

3D geometry

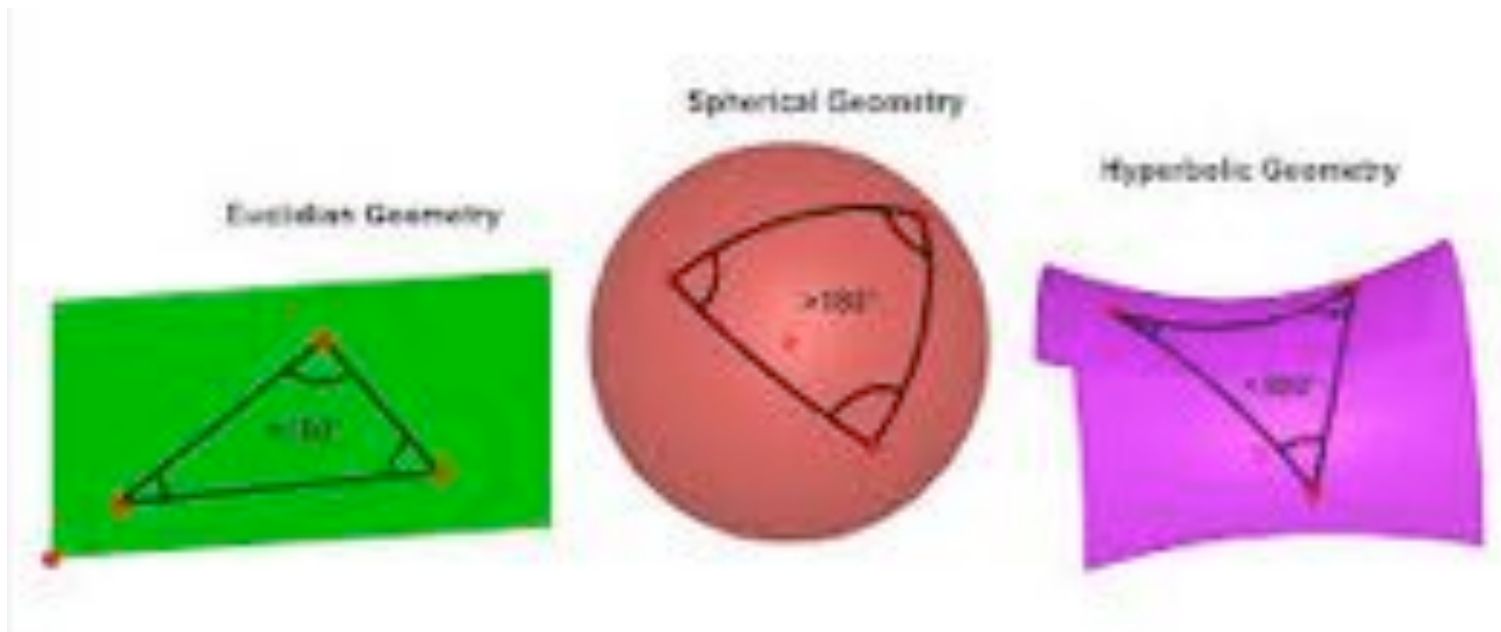
What is the relation between Euclides, Riemann, and Lobachevsky geometries?

WHAT DOES NON EUCLIDEAN GEOMETRY MEAN??



⇒ Euclidian Postulate #5

Attention: these are 2D exms.!



simple vs. multiple-connectedness

the cylinder: 1D compact 2D space $\mathbb{R} \times S^1$

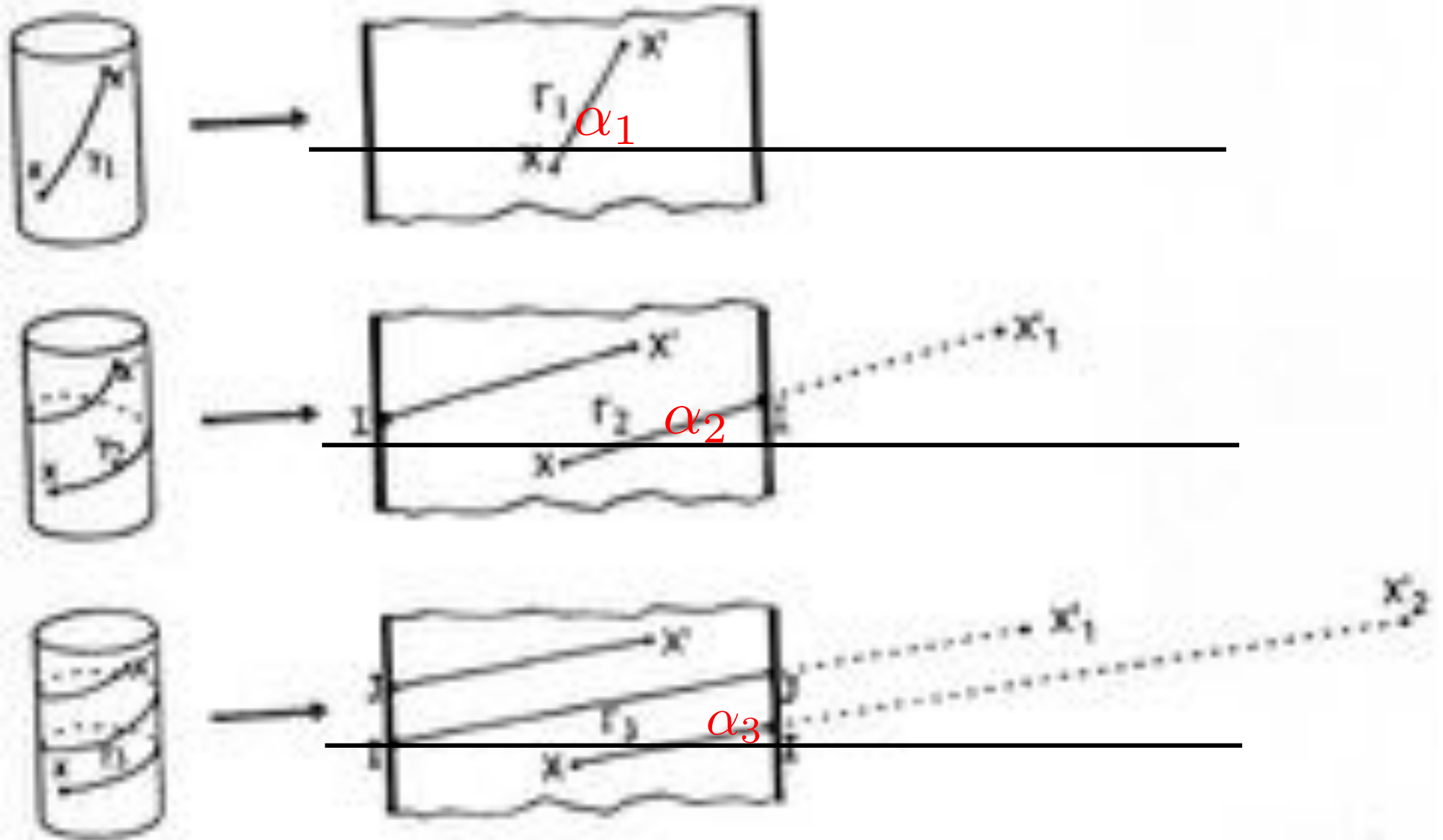


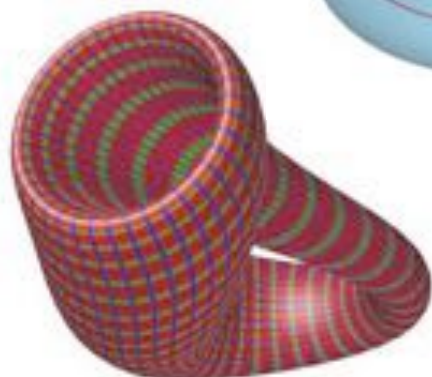
Fig. 1. Las geodésicas del cilindro

$\mathbb{R}^2$

3D topology

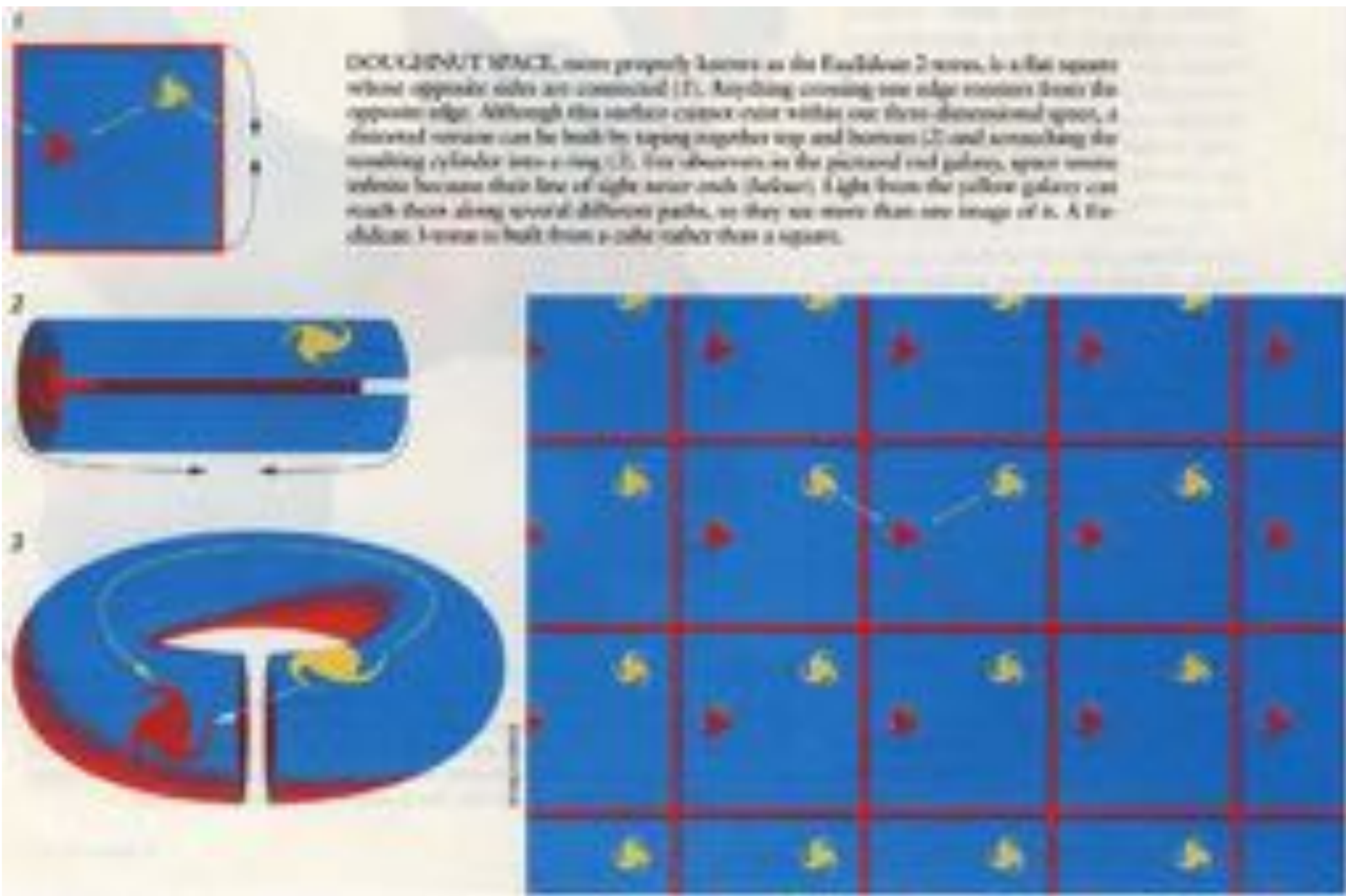


simple vs. multiple-connectedness

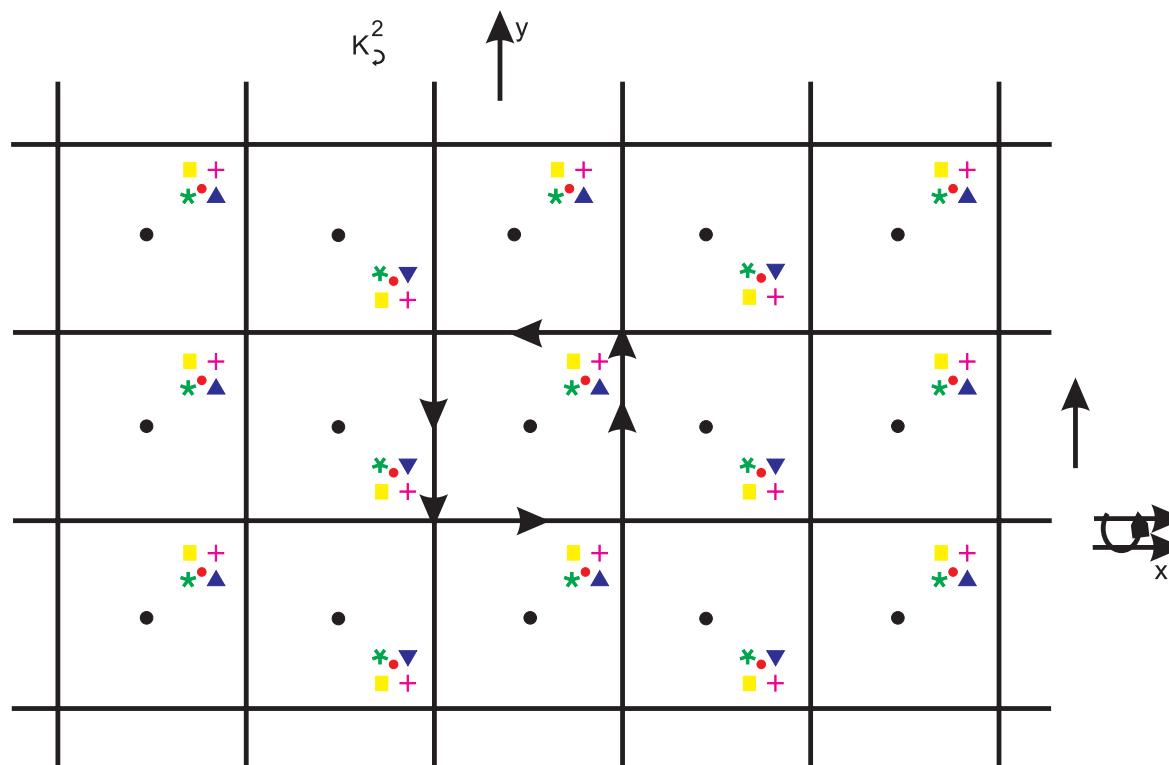
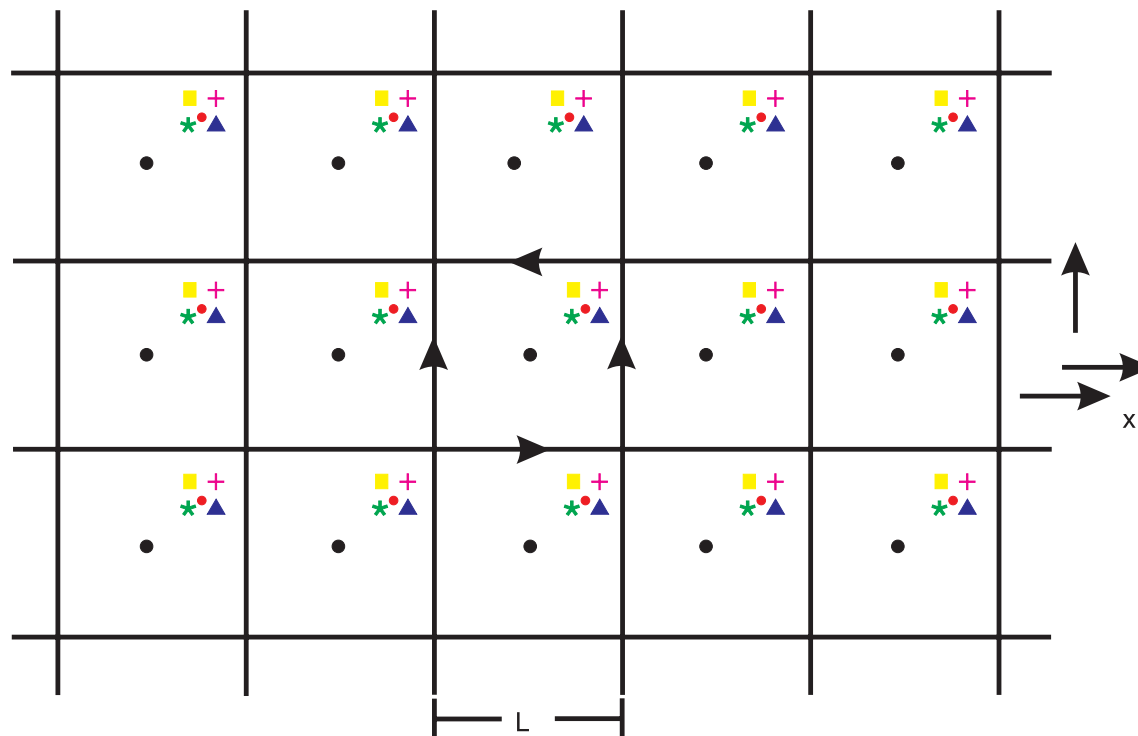
 $\mathbb{R} \times S^1$ 

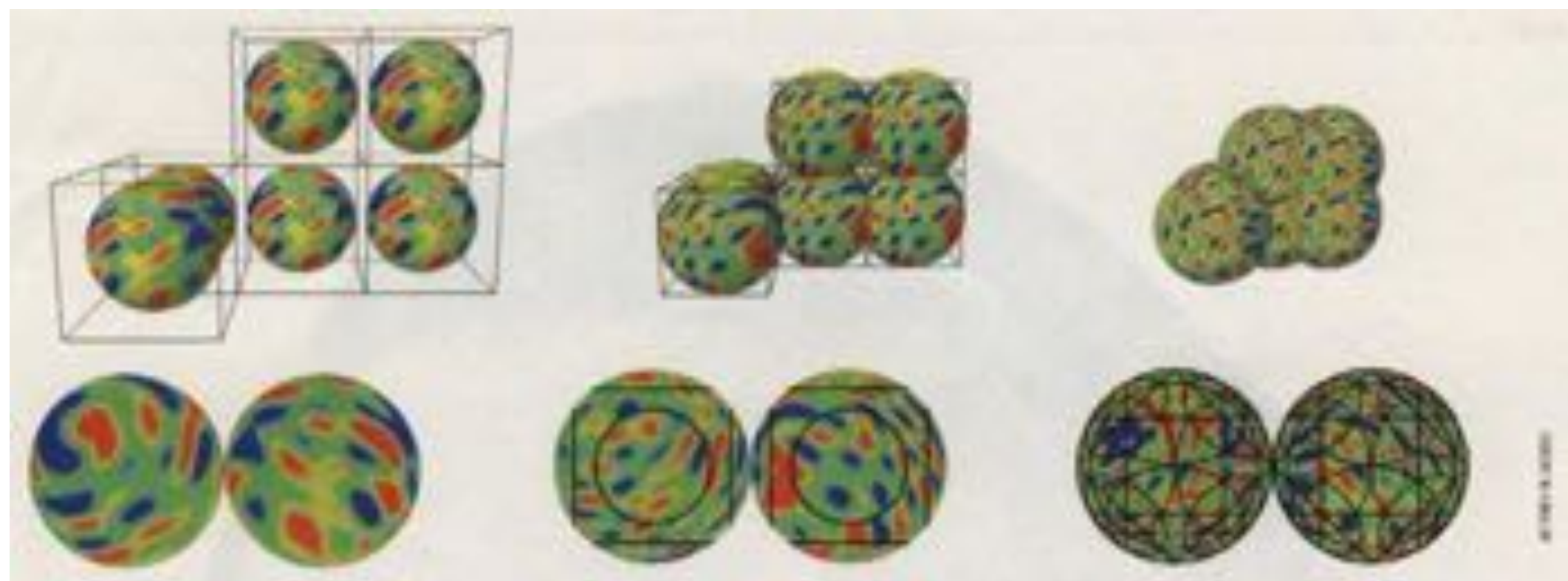
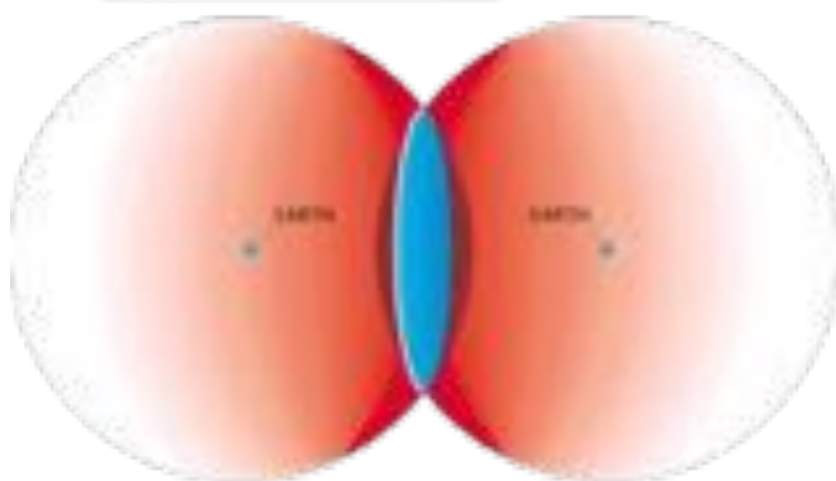
Name	Fundamental domain and identifications	Shape	Closed	Orientable
cylinder			NO	YES
Möbius band			NO	NO
torus			YES	YES
Klein bottle			YES	NO

simple vs. multiple-connectedness?



ISOMETRIES





- Few reports on breakdown of statistical isotropy of CMB at large angles (consistent for WMAP and Planck data):
 - Lack of correlation at large scales
 - Hemispherical asymmetry
 - Quadrupole-octopole alignment
 - Power spectrum asymmetry
 - Power spectrum deficit for large scales ($l < 50$)
 - Low variance
 - Point-parity asymmetry
 - The cold spot
 - ...

Pavel Bielewicz, 2016

“extraordinary claims require extraordinary evidence” C. Sagan

Anomalies $\Leftrightarrow > 3\sigma$

CMB anomalies $\Rightarrow$ anisotropic Universe?

Cosmic Topology

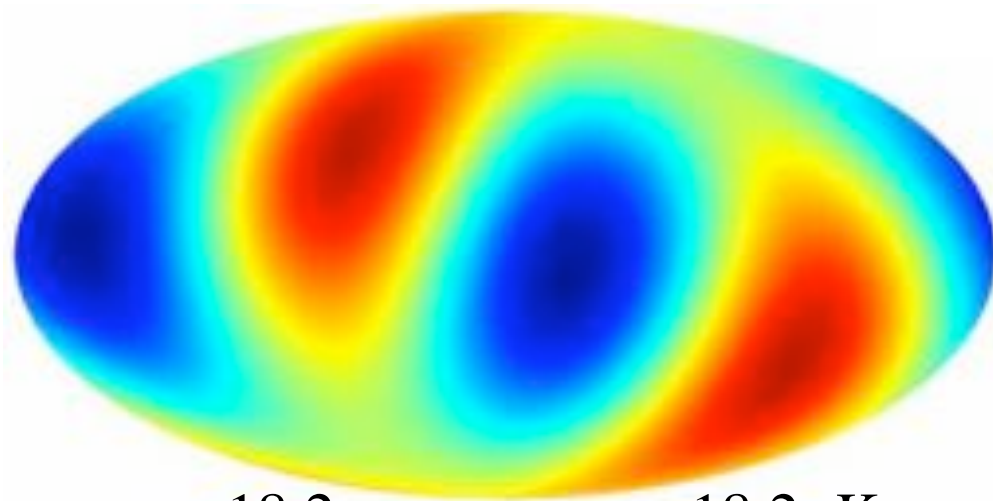
Is the CMB sphere anomalous?

- Quadrupole-Octopole alignment
 - Lack of large-angle correlations
- Hemispherical asymmetry
 - Low quadrupole: $C_2 \ll 1150 \text{ } \mu\text{K}^2_{\text{(LCDM)}}$
 $C_2 \in [1150/8, 1150/5]$

Is the CMB sphere anomalous?

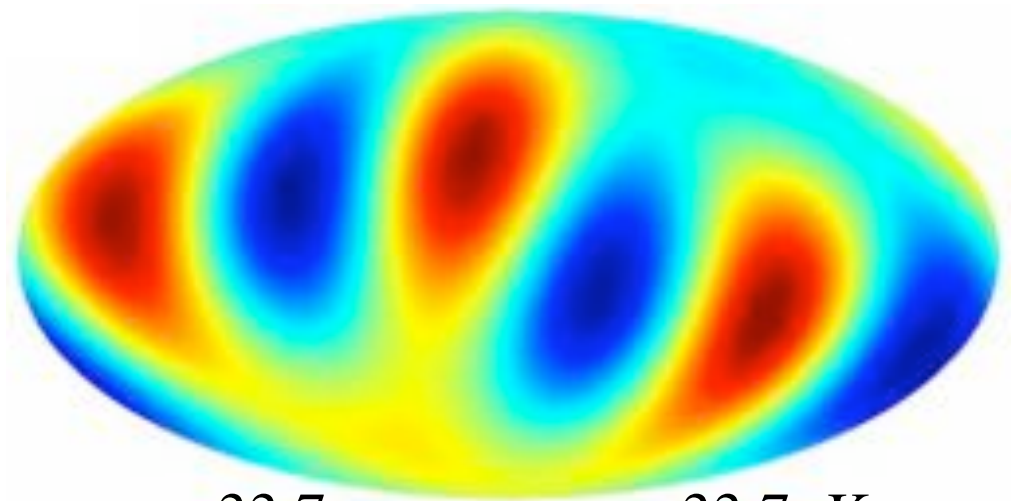
- Quadrupole-Octopole alignment
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 $C_2 \in [1150/8, 1150/5]$

Quadrupole-Octopole alignment



-18.2 ————— 18.2 μK

quadrupole



-33.7 ————— 33.7 μK

octopole

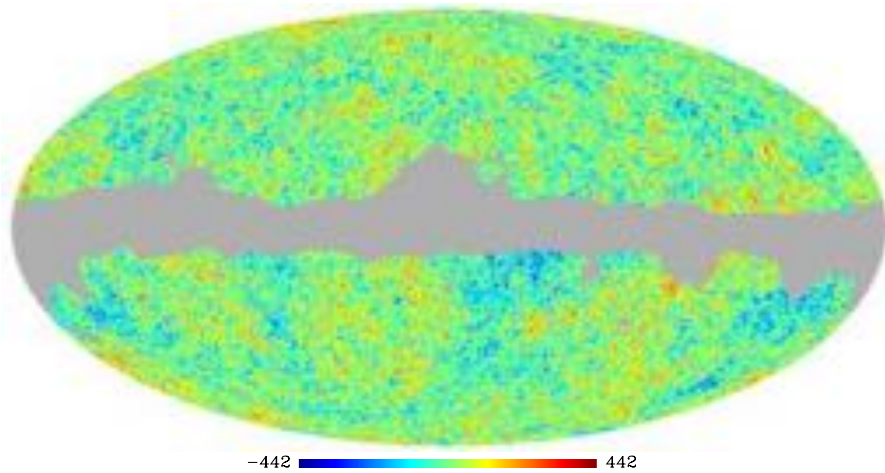
... planar and aligned

Why is this a CMB anomaly?

Is the CMB sphere anomalous?

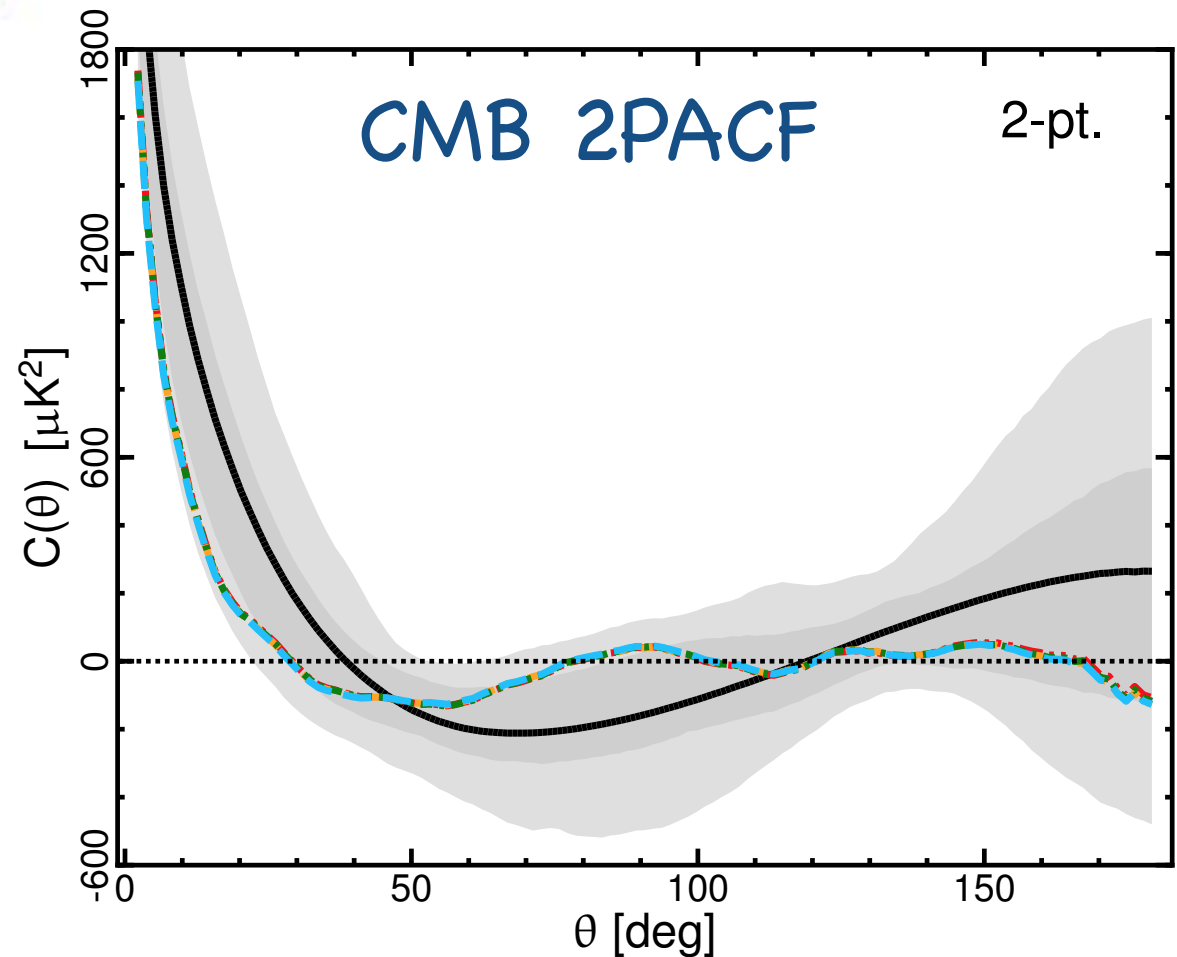
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 $C_2 \in [1150/8, 1150/5]$

Lack of correlation at large scales

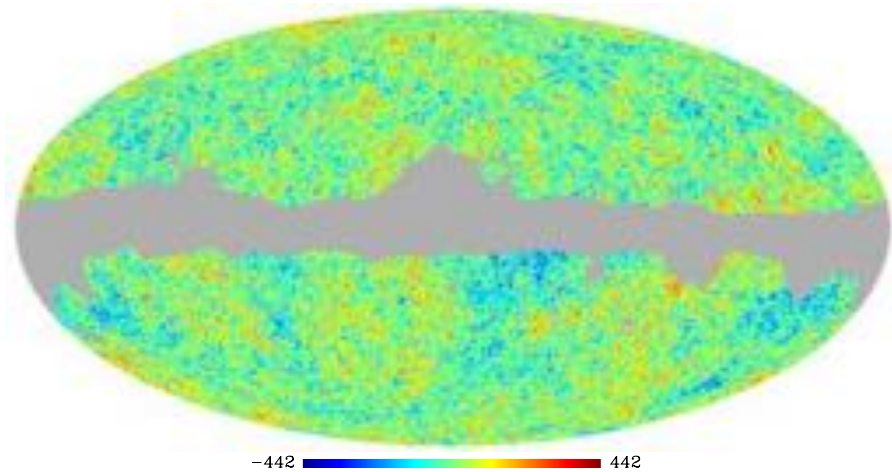


$$\hat{n} \cdot \hat{n}' = \cos(\theta)$$

$$C(\theta) \equiv \langle \Delta T(\hat{n}) \Delta T(\hat{n}') \rangle$$

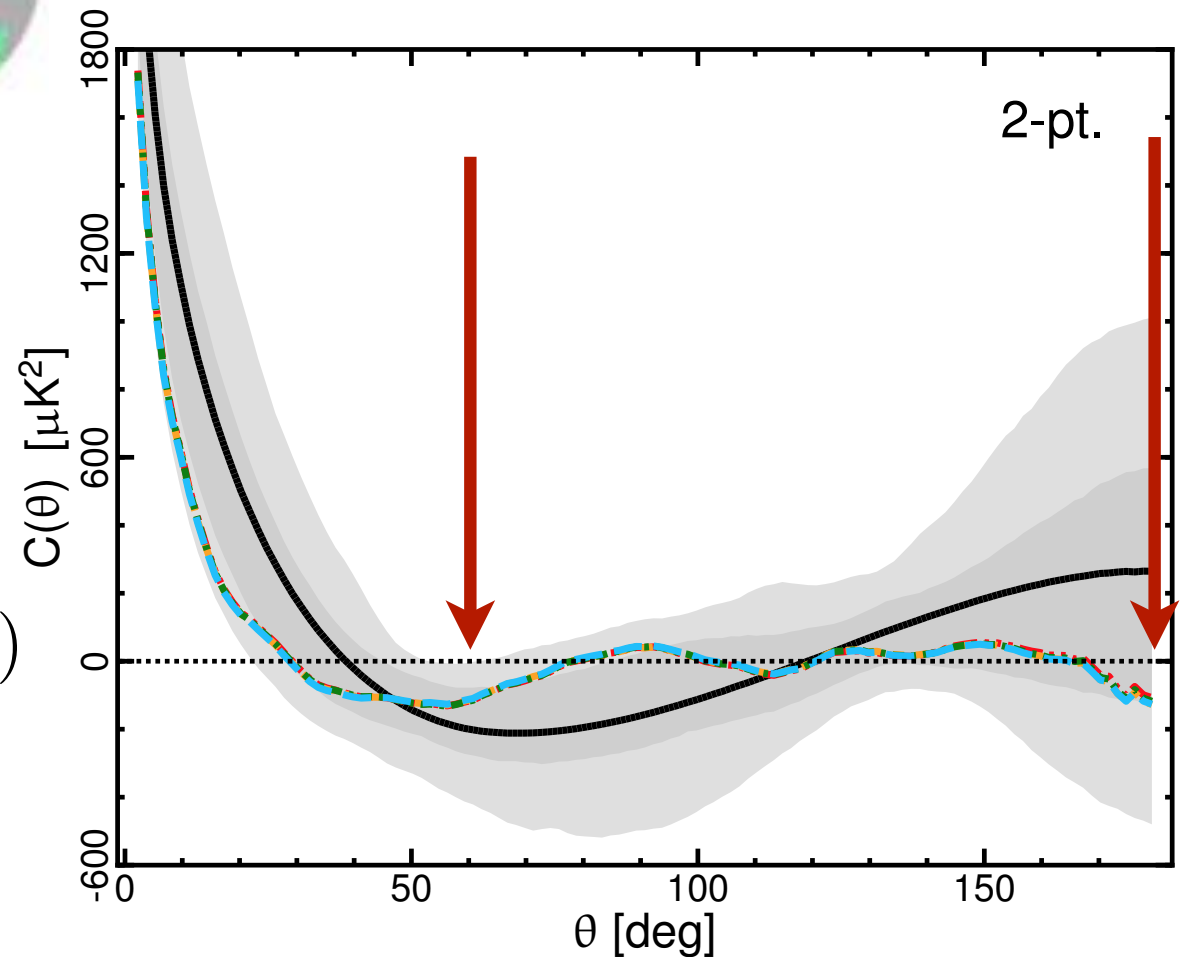


Why is this a CMB anomaly?



2PACF

$$\mathbf{C}(\theta) \equiv \langle \Delta T(\hat{n}) \Delta T(\hat{n}') \rangle$$



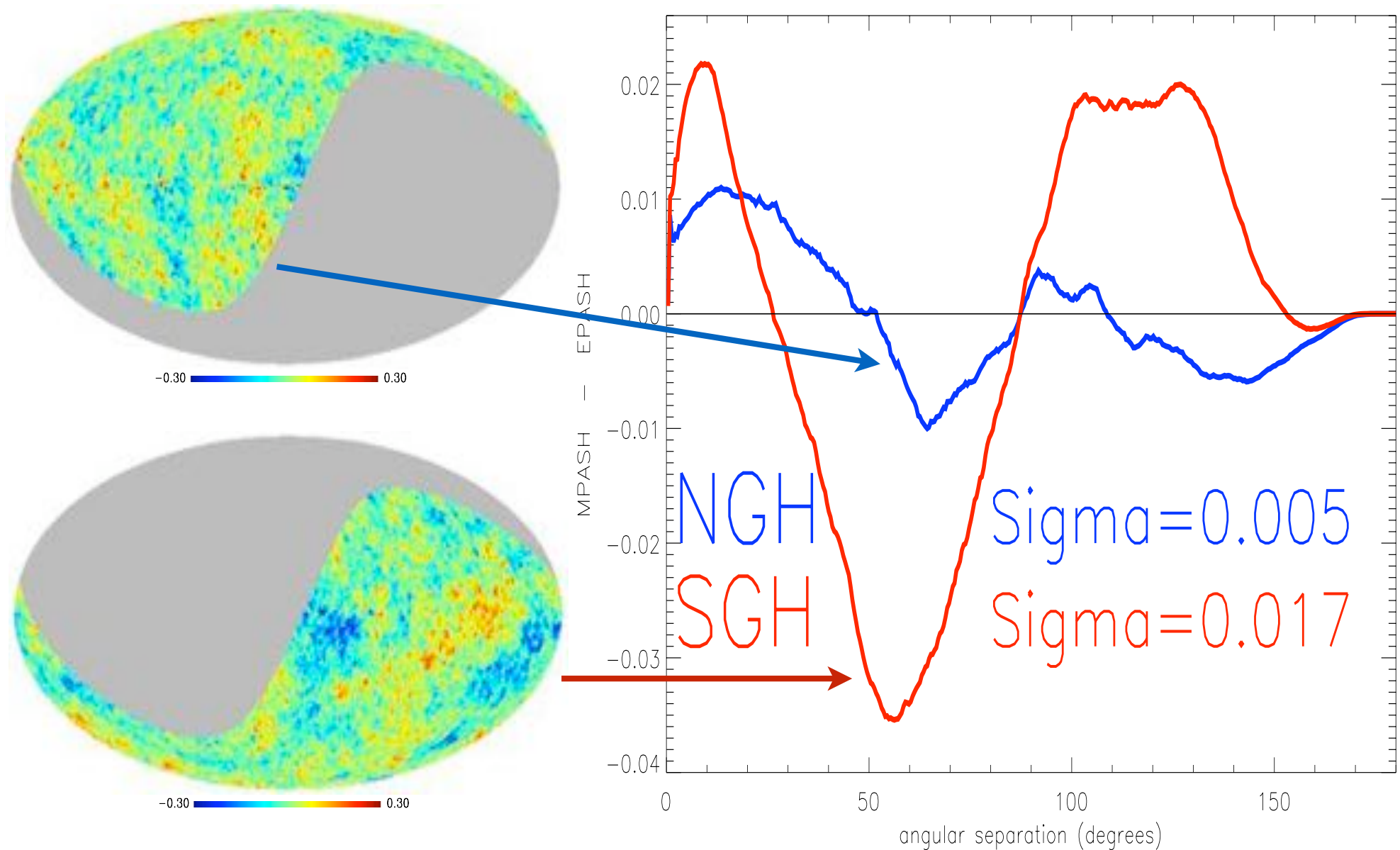
$$S_{1/2} \equiv \int_{-1}^{1/2} \mathbf{C}(\theta)^2 d(\cos \theta)$$

p-value: 0.3% - 1%

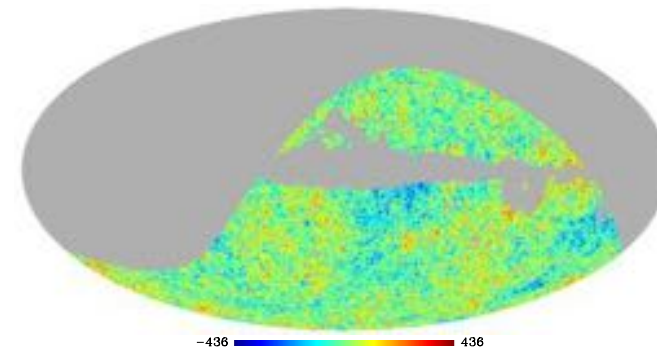
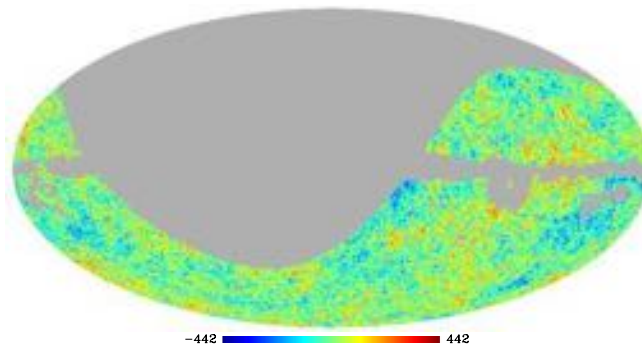
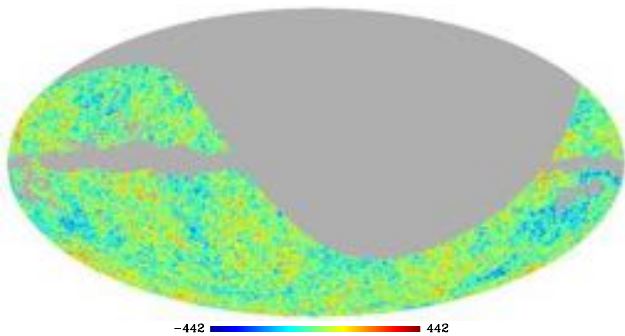
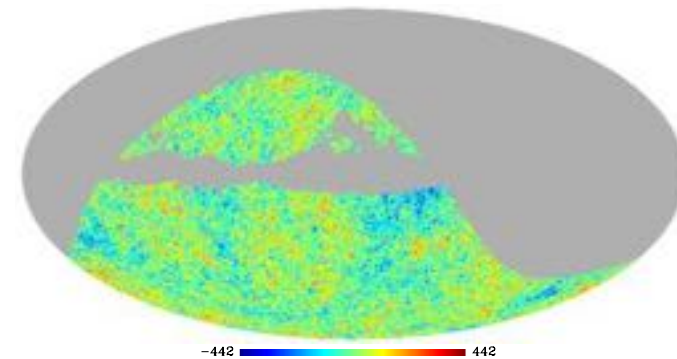
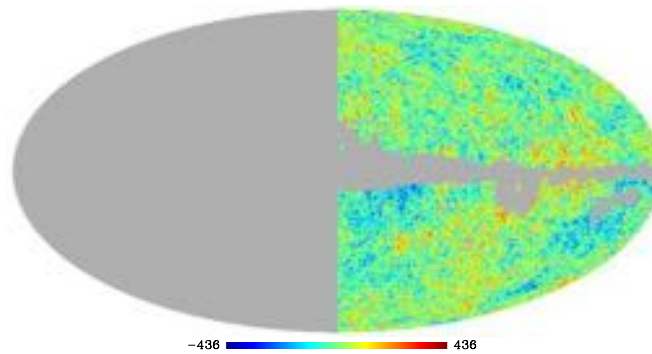
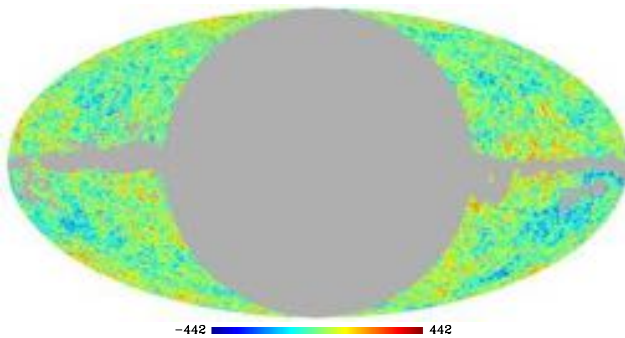
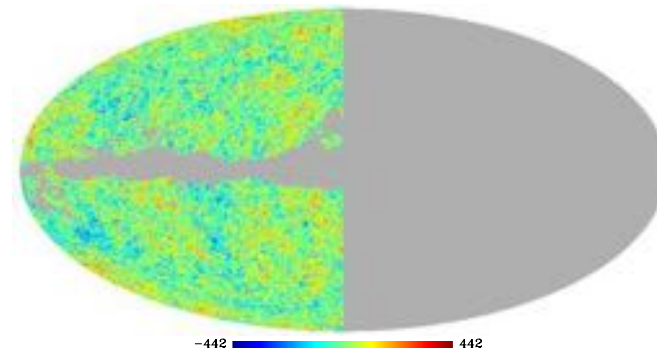
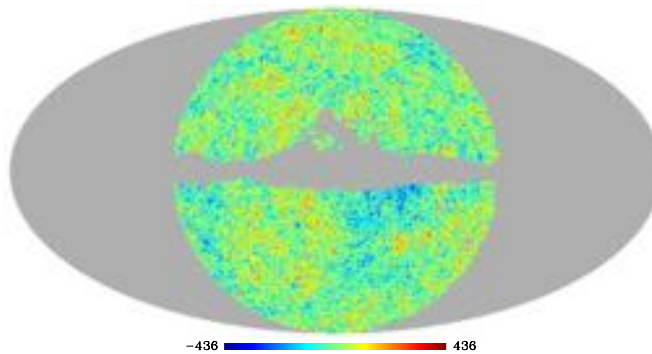
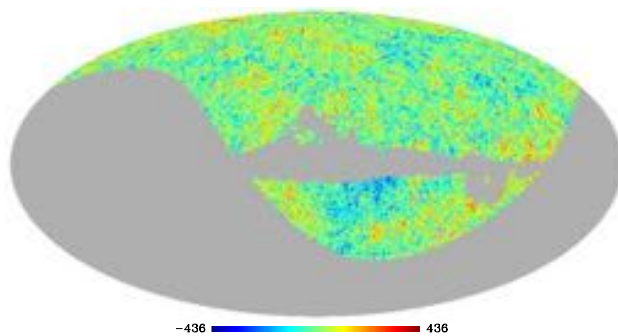
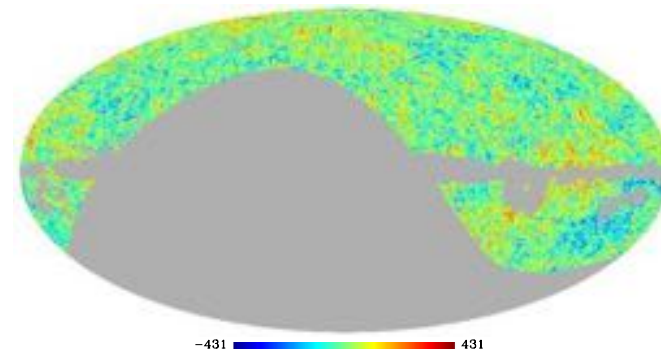
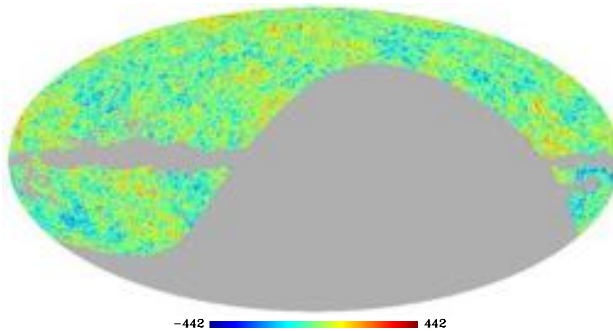
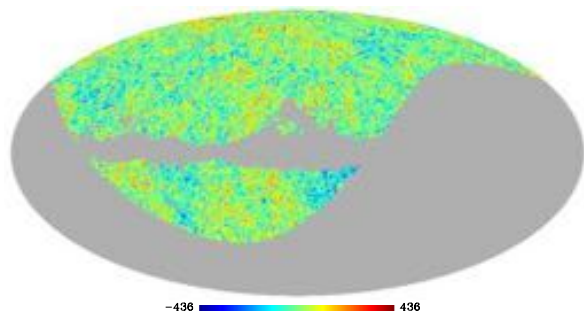
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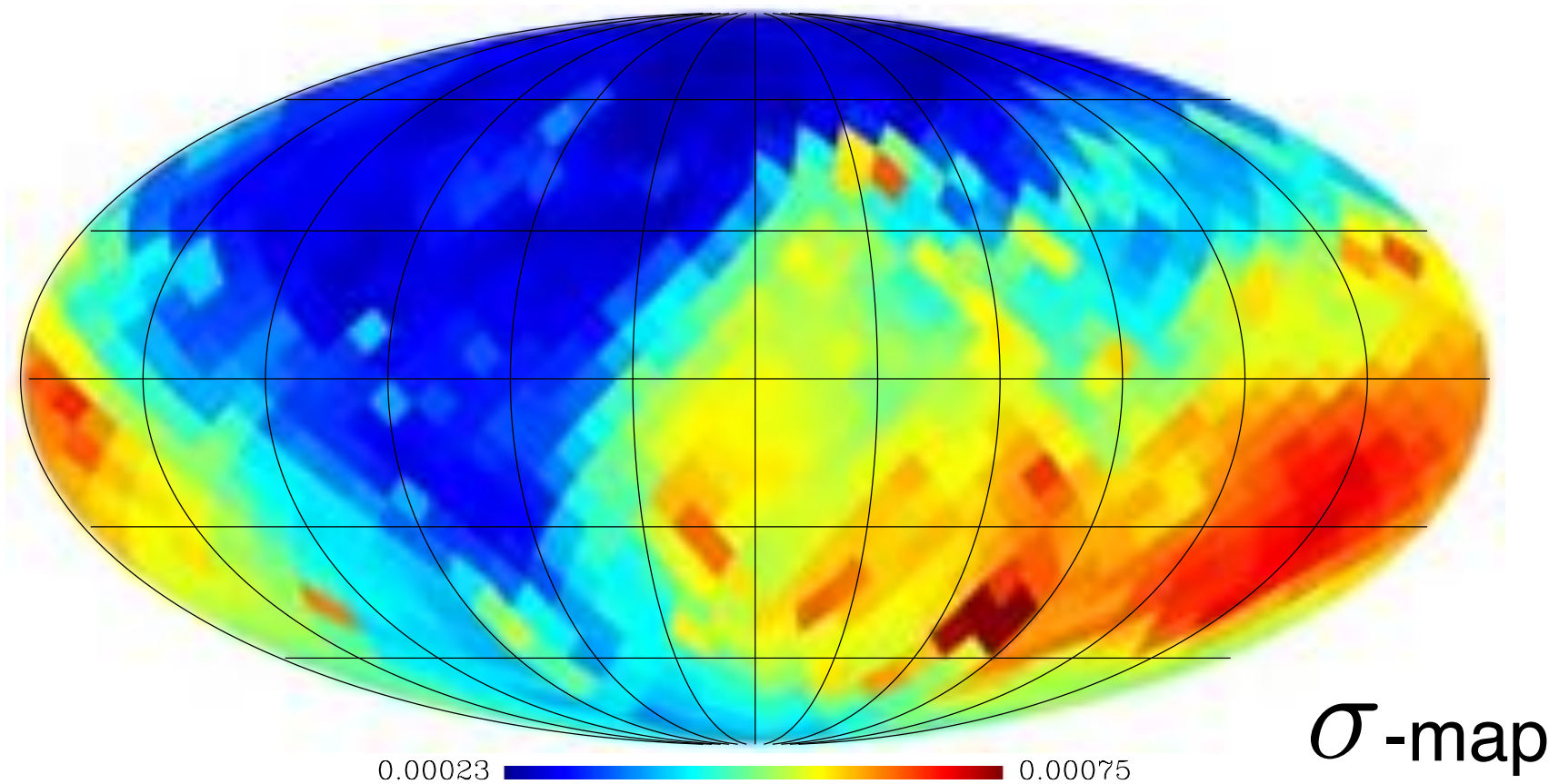
Hemispherical asymmetry



WMAP3, 2006



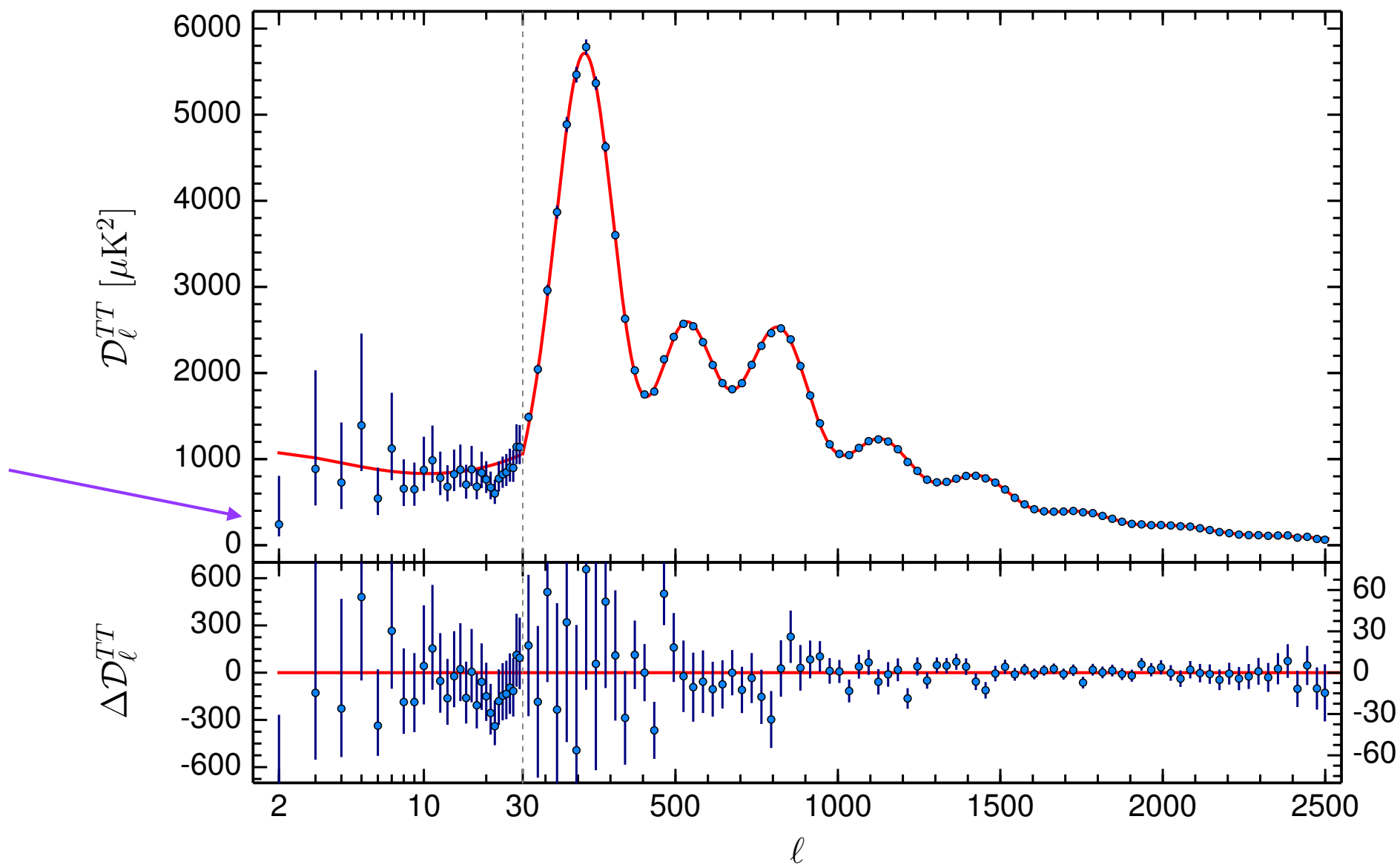
Hemispherical asymmetry



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 - Low quadrupole: $C_2 \ll 1150 \text{ } \mu\text{K}^2$ (LCDM)

$$C_2 \in [1150/8, 1150/5]$$



In the last ~ 23 years of CMB-anomalies literature:

- dozens of models (hypotheses, explanations,..)
- hundreds of papers (data analyses &/ models)
- thousands of citations

What we conclude:

- (1) the correct model/solution should explain all the CMB anomalies!
- (2) the model should provide one global preferred axis!

Suitability: cosmic topology provides manifolds with **one** global preferred axis, but...which one?

Motivation: B. Mota et al. astro-ph/0309371

“If the universe underwent an inflationary phase st:
 $|\Omega_0 - 1| = |\Omega_K| \ll 1$, then

“a generic detectable non-flat manifold is locally indistinguishable from either a cylindrical ($\mathbb{R}^2 \times S^1$) or toroidal ($\mathbb{R} \times T^2$) manifold, irrespective of its global shape, with the former being more likely”

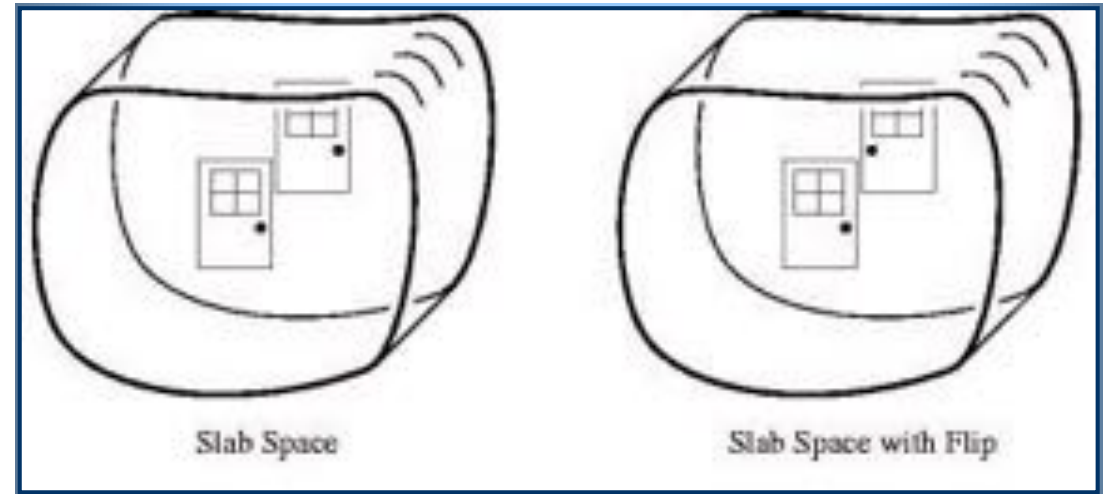
$$\mathbb{R} \times T^2$$

Current limit: $|\Omega_K| < 0.005$ Planck XIII, arXiv:1502.01589

Why not study features there ...

the slab-space (3d):

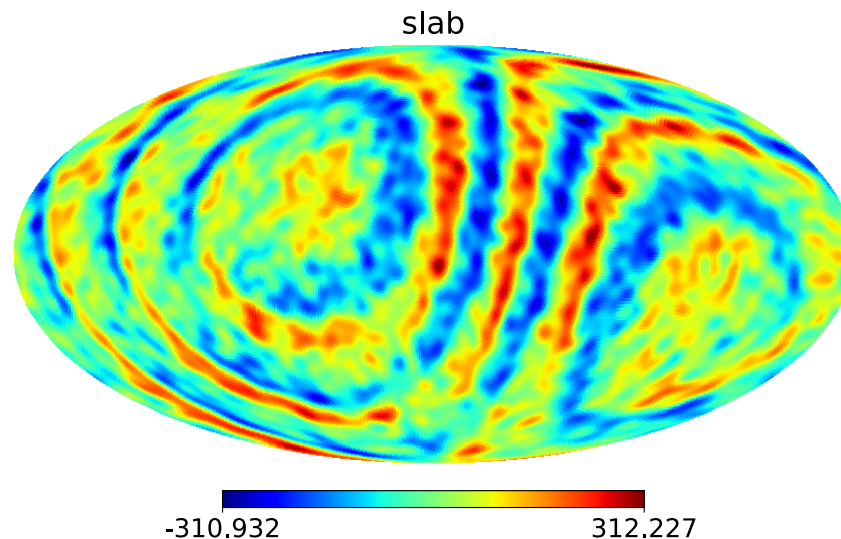
$$\mathcal{M}_3 = \mathbb{R}^2 \times S^1$$



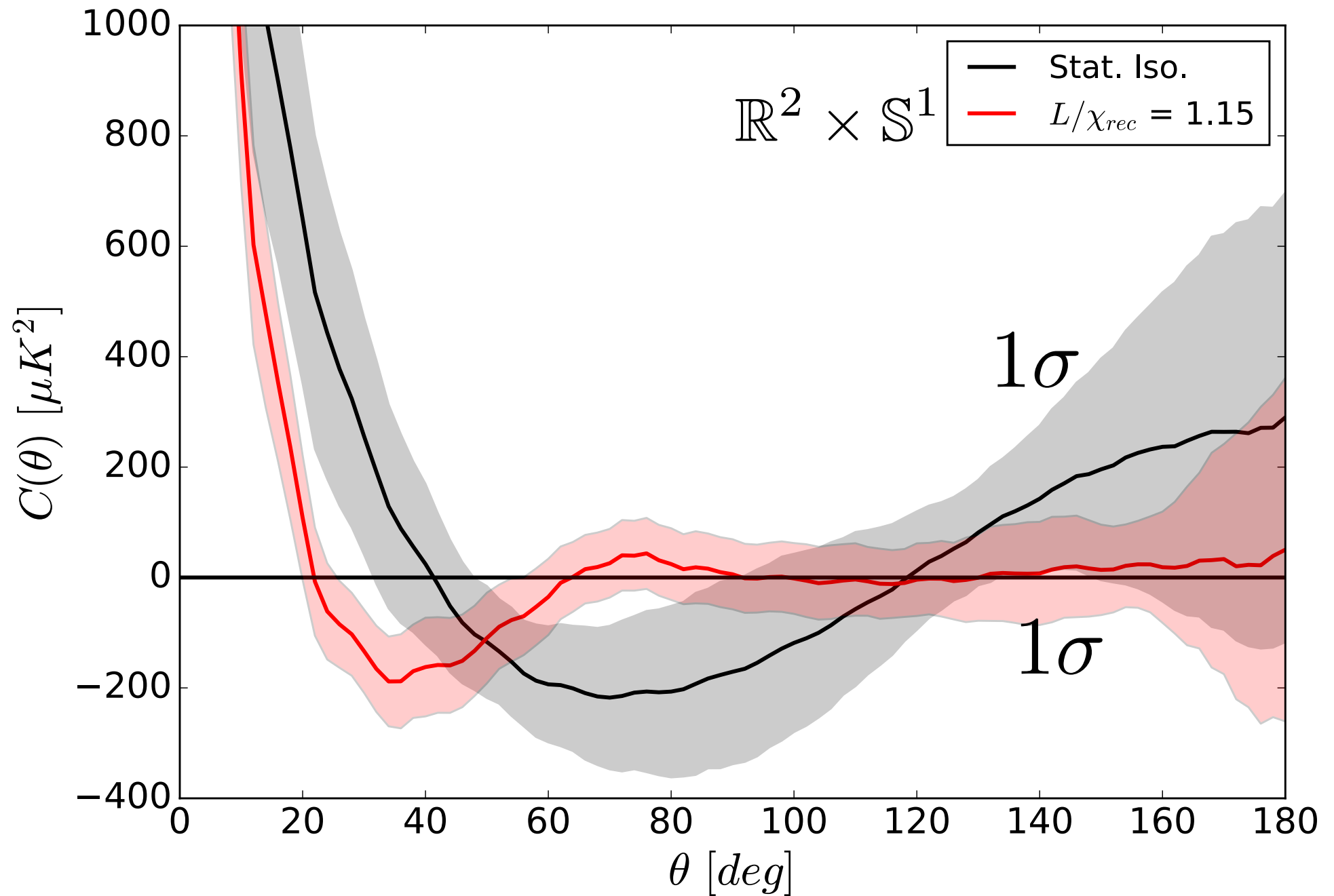
with the current limit: $L/\chi_{rec} > 1.12$

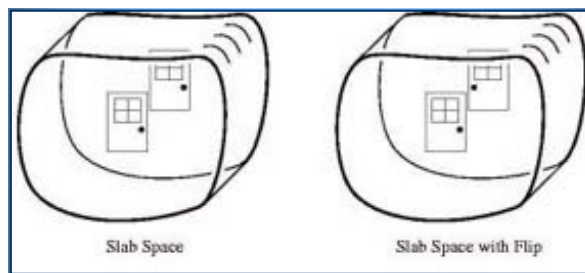
toy-slab:

$$L/\chi_{rec} = 0.5$$

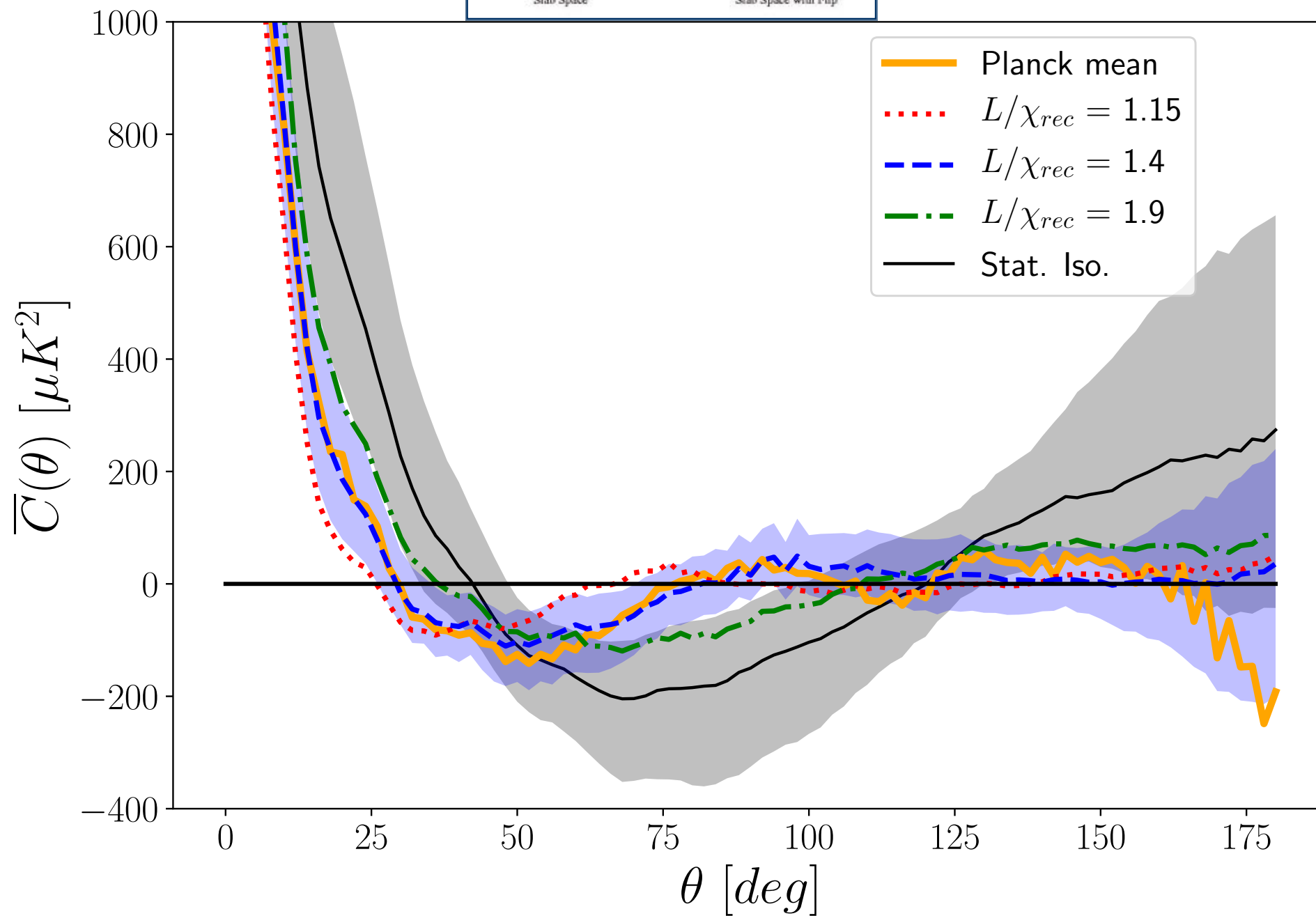


Proposal of solution: slab-space





$$\mathbb{R}^2 \times \mathbb{S}^1$$

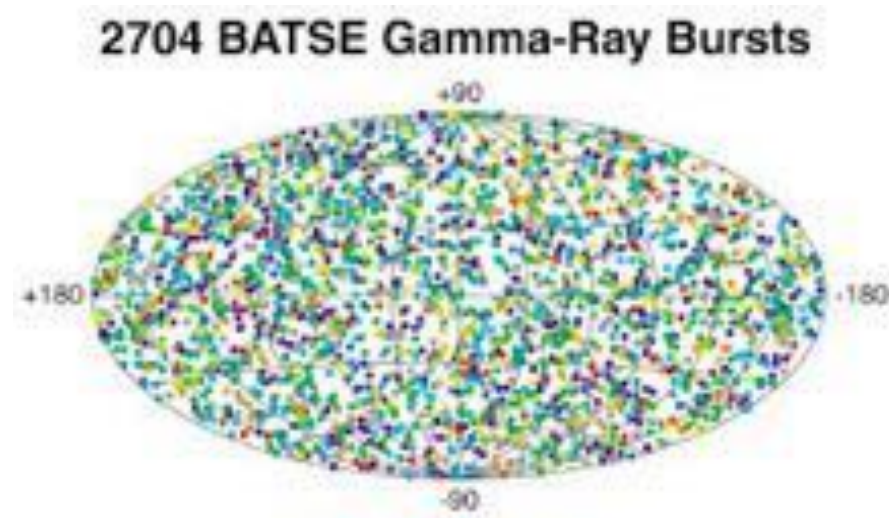


Para encerrar

Nossa profissão vive de ideias científicas!



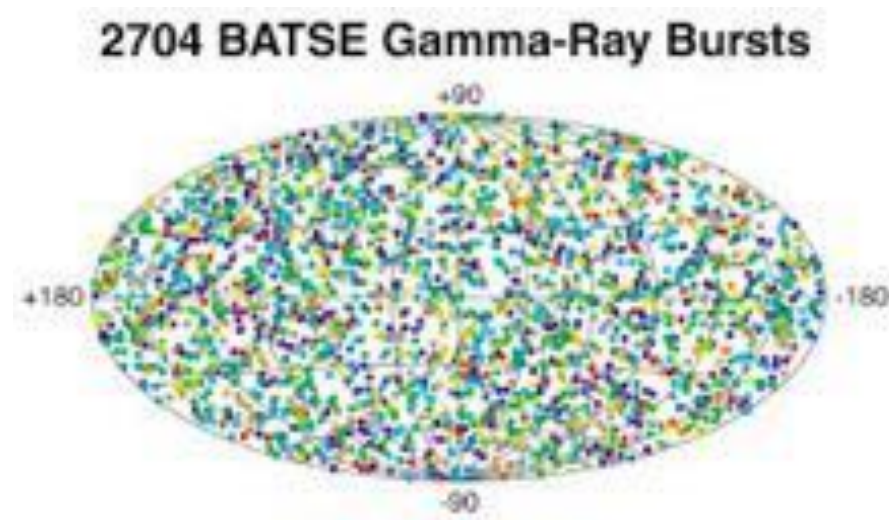
Isotropia estatística de GRBs



Nossa profissão vive de ideias científicas!



Isotropia estatística de GRBs



THE ASTROPHYSICAL JOURNAL, 673:968–971, 2008 February 1

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ON THE LARGE-SCALE ANGULAR DISTRIBUTION OF SHORT GAMMA-RAY BURSTS

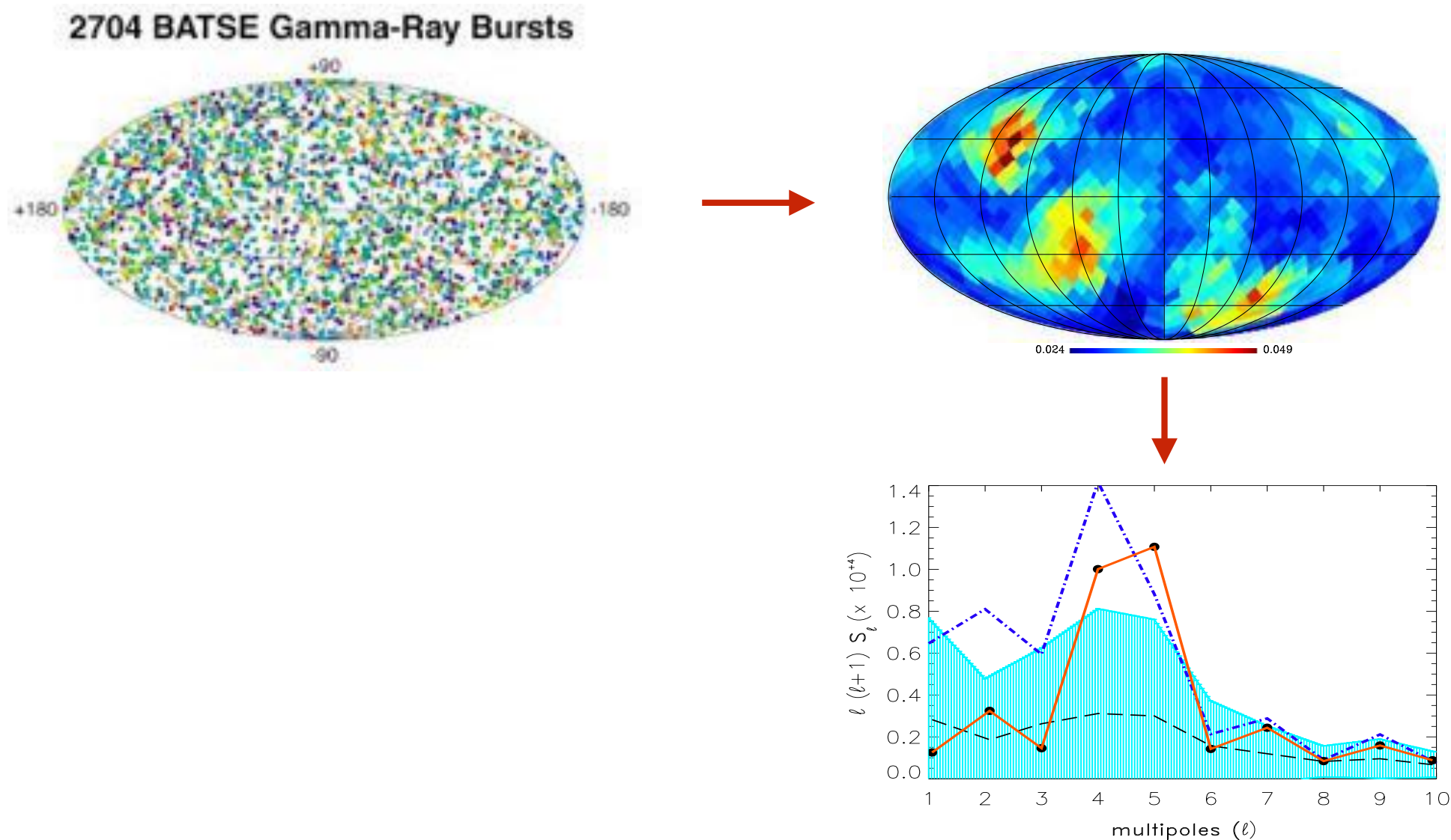
A. BERNUI, I. S. FERREIRA, AND C. A. WUENSCHÉ

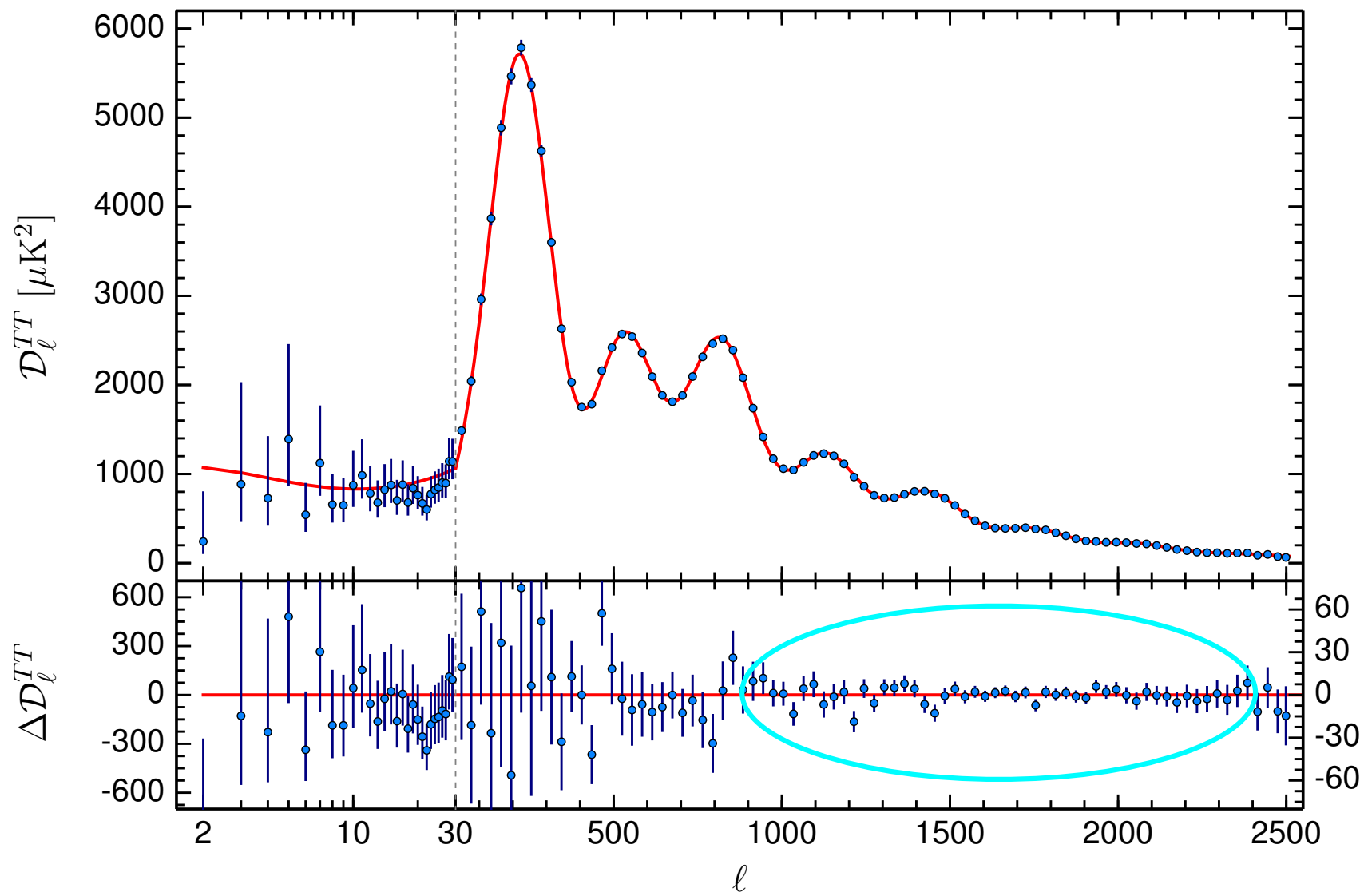
Instituto Nacional de Pesquisas Espaciais, Divisão de Astrofísica, Avenida dos Astronautas 1758, CEP 12227-010 São José dos Campos, SP, Brazil; bernui@das.inpe.br; ivan@das.inpe.br; alex@das.inpe.br

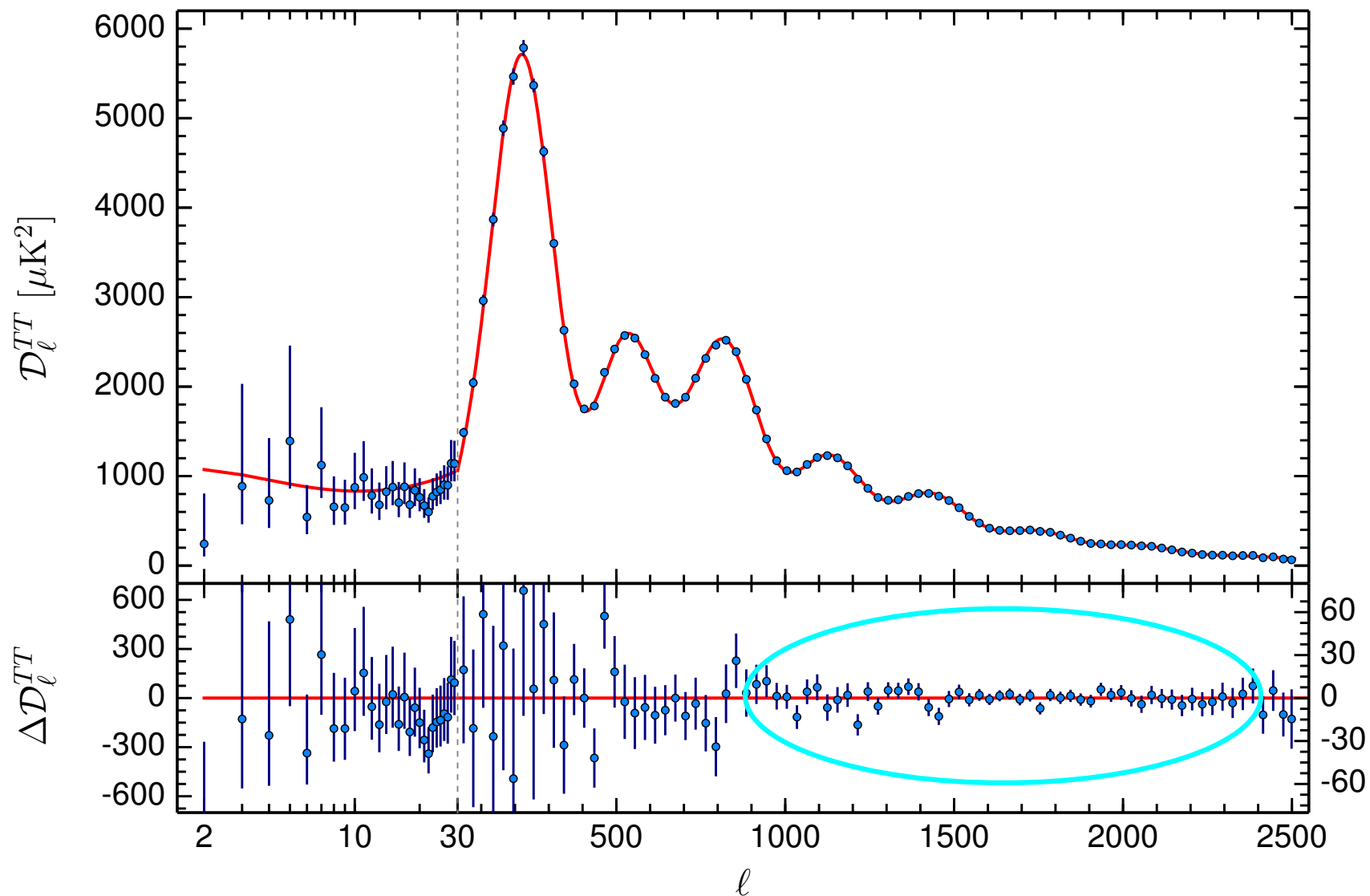
Received 2007 April 12; accepted 2007 October 8

Problema científico

Isotropía estadística de GRBs





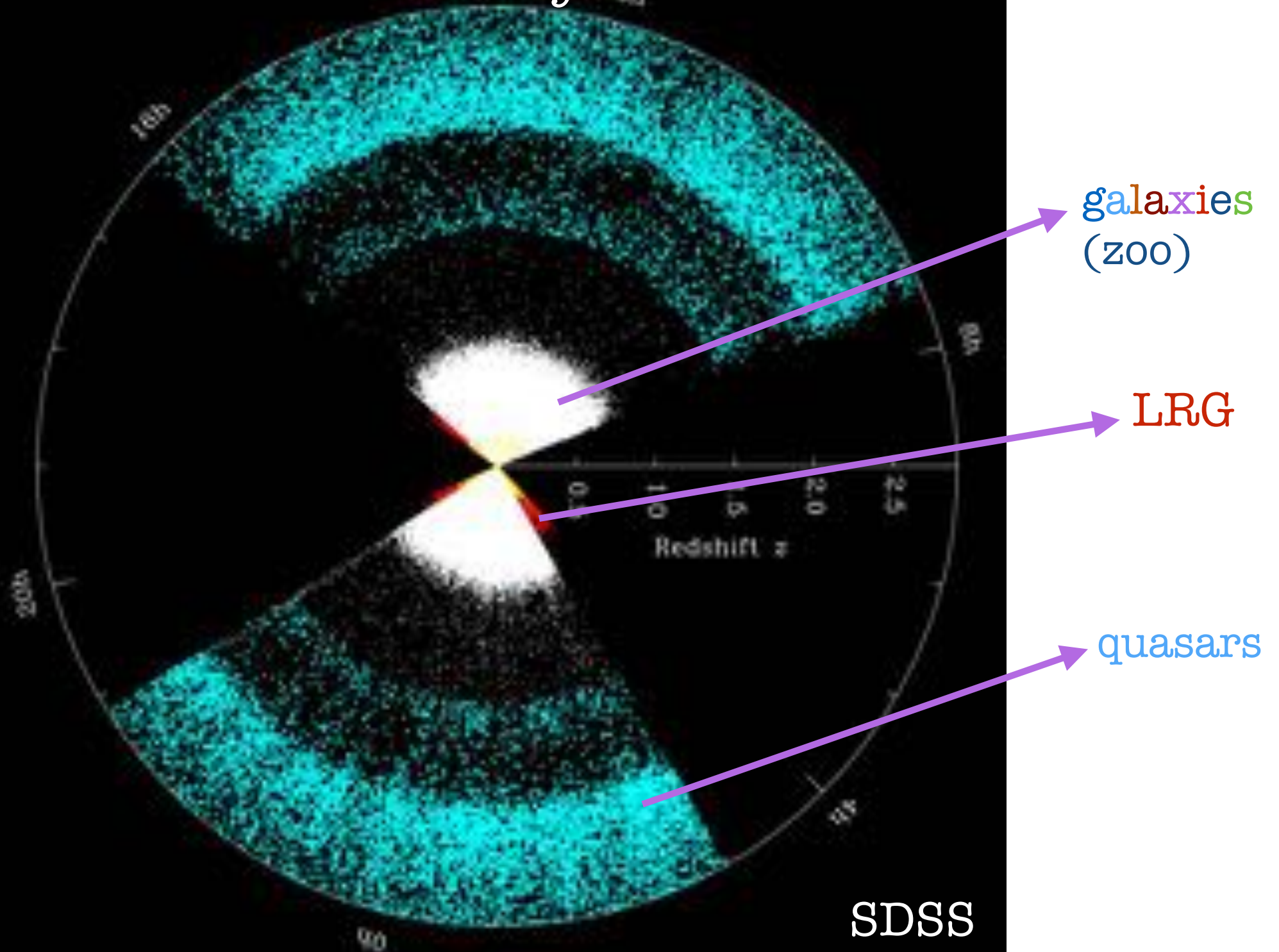


Journal of **C**osmology and **A**stroparticle **P**hysics
An IOP and SISSA journal

Excess of lensing amplitude in the Planck CMB power spectrum

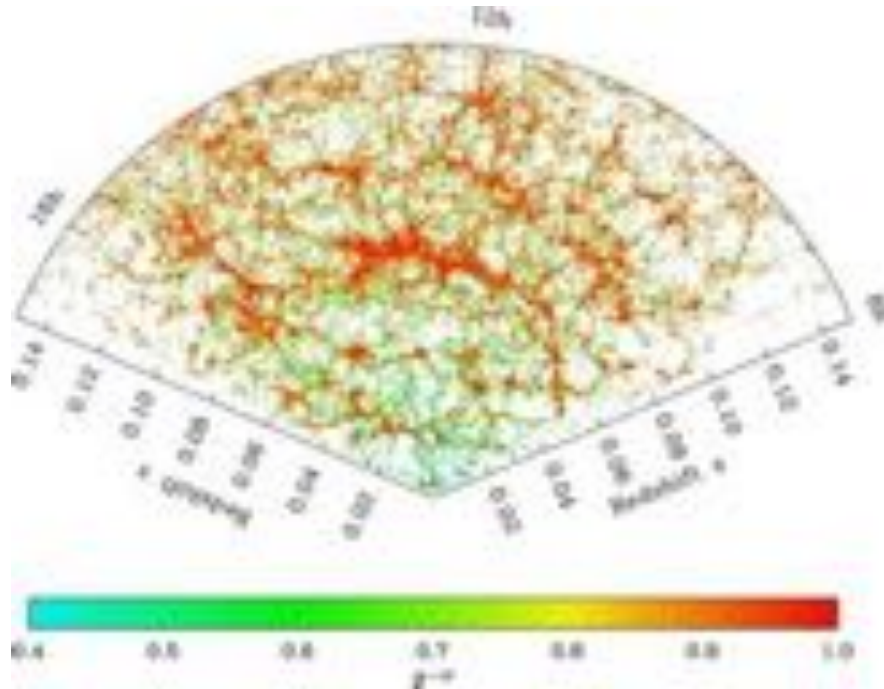
Rahima Mokeddem,^{a,*} Wiliam S. Hipólito-Ricaldi^b
and Armando Bernui^c

Cosmic Tracers: to study the Universe LSS



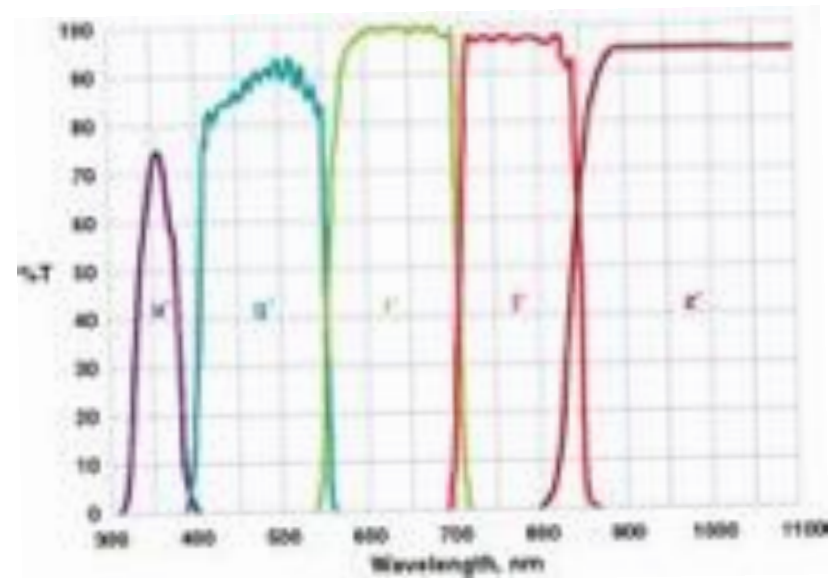
Cosmic Tracers: to study the large-scale structure

SDSS Main Galaxy Sample (MGS)



blue galaxies:

Local Universe



ugriz

Cosmologia observacional: estudamos o Universo em largas escalas...

Aprendemos de outras áreas da astrofísica quando utilizamos **diversos traçadores cósmicos**:

HI (ALFALFA), **blue galaxies** (SDSS+SPLUS), **LRG** (SDSS),
quasares (SDSS+SPLUS), GRB (Batse+Fermi), CMB (Planck)
LPM (Planck), galaxy clusters (Planck), SNe (Pantheon+),...

